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83T-10-82 S M HOLMES, D J HUNT, T W LAKE, P J MARRON, S F REDDAWAY, N WESTBURY and G M^{c}C HAWORTH:
ICL, Reading, RG1 8PN, UK. Primality-testing Mersenne Numbers. Preliminary Report.

$M_p = 2^p-1$, index p prime, is a Mersenne Number. Let $S_1 = 4$ and let $S_{n+1} = S_n^2-2 \bmod M_p$. The Lucas-Lehmer primality test (LLT) is "M_p prime $\Leftrightarrow$ residue $S_{p-1} = 0$". We have exercised the LLT on an index-set P using Fast Fermat-number-transform multiplication. Codes A and B ran on an ICL DAP, an SIMD parallel processor having 4096 elementary processing elements. Code C is under test.

P is a comprehensive set of primes for two reasons. First, the code for the relatively complex transform algorithm deserves the fullest testing. Secondly, the LLT is non-constructive and its history includes some incorrect residues which were temporarily thought to 'prove' their M_p composite. We believe an 'LLT proof' must include two independent residue computations. Thus, while we did not include almost all $p < 38220$ like Nelson, P otherwise contains all p for which we knew or presumed the LLT had been applied. P also contains all $p < 62982$ for which we knew of no M_p-factor.

Our codes checked the squaring mod-7 and were run twice over their respective ranges. Code A for $p < 31488$ tested M_{31487} in 142 seconds; Code B for $p < 62976$ tested M_{62929} in 562 seconds.

For some 2828 p less than the previous search-limit of 50024 we confirmed and filed a definitive set of residues. We thus validated the results, as sometimes corrected, of Hurwitz/Selfridge, Kravitz/Berg, Gillies, Tuckerman, Nickel/Noll and Nelson/Slowinski. For the range $50024 < p < 62982$, our 475 new residues are all non-zero and so reveal no new prime M_p: we invite their confirmation.

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