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### An Improved Method for Determining the DC Magnetization Curve Using a Ring Specimen

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Abstract -- When the dc magnetization curve (B-H) of non-oriented material is measured in a ring specimen, there is an intrinsic error due to the assumption that the mean magnetic path length is equal to the mean geometric path length.

In this paper, a new method for determining the B-H curve accurately is proposed. The validity of the method is verified by experiments.

#### I. INTRODUCTION

When the dc magnetization curve (B-H) is measured using a ring specimen, the mean geometric path length  $L_c$  is used instead of the mean magnetic path length  $L_a$ , because  $L_a$  is unknown. Therefore, the B-H curve obtained has an error, and it may be affected by the ratio  $\gamma$  of the outside radius to the inside radius and the shape of the B-H curve of the specimen. The IEC Standard specifies that  $\gamma$  should be less than or equal to 1.1 [1]. But it is difficult to make such a large specimen. If an unannealed specimen with a small width is used, the flux distribution may be affected by the stresses induced due to cutting [2]. Therefore, the specimen must be large and it becomes difficult to handle.

In this paper, the effects of  $\gamma$  and the shape of the B-H curve on the error are discussed, and a new method for determining the B-H curve accurately using a numerical calculation is explained in detail. The effectiveness of the proposed method is also verified by experiments.

#### II. ERROR OF CONVENTIONAL METHOD

If we want to determine the B-H curve using a ring specimen as shown in Fig.1, the flux density B(R) at a point P on the radius R and the corresponding magnetic field strength H(R) should be measured. Although H(R) can be calculated from Eq.(1),



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 $H(R) = NI / 2\pi R$  (1) where NI is the applied magnetomotive force (MMF), B(R) cannot be measured, but the average flux density B<sub>a</sub>, can be measured using a search coil, as defined by Eq.(2),

$$B_{a} = \frac{1}{R_{o} - R_{i}} \int_{R_{i}}^{R_{o}} B(R) dR$$
 (2)

where  $R_0$  and  $R_j$  are the outside and inside radii.

There are two kinds of approximation methods for B or H in the conventional method as follows:

1) Instead of the magnetic field strength  $H_a$  on the mean magnetic path corresponding to  $B_a$ , the magnetic field strength  $H_c$  on the center radius  $R_c(=(R_i+R_0)/2)$  is used as the approximate magnetic field strength corresponding to  $B_a$  as shown in Fig.2(a).

2) Instead of the flux density  $B_c$  on the center radius  $R_c$ , the flux density  $B_a$  is used as the approximate flux density corresponding to  $H_c$  as shown in Fig.2(b).



Fig.2 Approximation methods for B-H curve.

If the true B-H curve is known beforehand, the error  $\varepsilon_{\rm H}$  of the magnetic field strength corresponding to the case 1) mentioned above, and the error  $\varepsilon_{\rm B}$  of the flux density corresponding to the case 2) which are defined by Eqs.(3) and (4) are calculated as shown in Figs.3(a) and (b).

$$E_{\rm H} = ({\rm H_c} - {\rm H_a}) / {\rm H_a} \times 100 \ (\%) \tag{3}$$

$$\varepsilon_{\rm B} = (B_{\rm a} - B_{\rm c}) / B_{\rm c} \times 100 \,(\%) \tag{4}$$

Fig.3 is obtained for the steel (SS400). The errors  $\varepsilon_{\rm H}$  and  $\varepsilon_{\rm B}$  are affected by the ratio  $\gamma$  which is defined by Eq.(5) and the shape of the B-H curve.

$$= \mathbf{R}_{\mathbf{0}} / \mathbf{R}_{\mathbf{i}}$$
(5)

#### III. NEW METHOD FOR DETERMINING THE B-H CURVE

In the newly developed method proposed here,  $B_c$  in Fig.2(b) is obtained directly using Eq.(2) in order to eliminate the error of the conventional method. The applicability of the

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γ:

method for obtaining H<sub>a</sub> in Fig.2(a) is discussed later in this section. 250 r



For simplicity, it is assumed that the B-H curve can be approximated by linear interpolation. Fig.4 shows an example of the B-H curve which is measured by applying four kinds of MMF's. Fig.5 shows the part of B-H curve related to the 2nd MMF. H<sub>ik</sub>, H<sub>Ck</sub> and H<sub>ok</sub> are the magnetic field strengths for the k-th MMF on the radii R<sub>i</sub>, R<sub>c</sub> and R<sub>o</sub> respectively. B<sub>ik</sub>, B<sub>ck</sub> and B<sub>ok</sub> are the flux densities corresponding to H<sub>ik</sub>, H<sub>ck</sub> and H<sub>ok</sub>. B(R) is interpolated as follows:

$$B(R) = \frac{H(R) - H_L}{H_U - H_L} (B_U - B_L) + B_L$$
(6)

where  $H_L$  and  $H_U$  are the magnetic field strengths on the lower and upper boundaries for a piecewise linear interpolation.

The last m-th MMF should be chosen to be above the saturation magnetic field strength  $H_s$  as shown in Fig.4. This is due to the need to know the flux density  $B_{im}$  (This corresponds to  $B_{i4}$  in Fig.4) at the end point of the B-H curve in order to interpolate  $B_{i3}$  in Fig.4.  $B_{im}$  is calculated by the following equation:

 $B_{im} = \mu_0 H_{im} + M_s$  (7) where  $\mu_0$  is the permeability of free space.  $M_s$  is the saturation magnetization which is known.

For example, B(R) between  $B_{c1}$  and  $B_{c2}$  shown in Fig.5 is represented as follows:

$$\mathbf{B}(\mathbf{R}) = \frac{\mathbf{H}(\mathbf{R}) - \mathbf{H}_{c1}}{\mathbf{H}_{c2} - \mathbf{H}_{c1}} (\mathbf{B}_{c2} - \mathbf{B}_{c1}) + \mathbf{B}_{c1}$$
(8)

As B(R) between  $B_{02}$  and  $B_{12}$  are represented by three lines as shown in Fig.5, the integral in the right-hand side of Eq.(2) is separated into three parts as follows:

$$\int_{R_i}^{R_o} B(R) dR = S_{\alpha} + S_{\beta} + S_{\gamma}$$
(9)

where  $S_{\alpha}$ ,  $S_{\beta}$  and  $S_{\gamma}$  are the integrated results, which correspond to the hatched parts **1000**, **C** and **1000** shown in Fig.5 respectively. For example,  $S_{\beta}$  is calculated from Eqs.(1), (2), (8) and (9) as follows:

$$S_{\beta} = \frac{NI_{2}}{2\pi (H_{c2} - H_{c1})} \{ (-\ln \frac{H_{c2}}{H_{c1}} + \frac{H_{c2}}{H_{c1}} - 1)B_{c1} + (\ln \frac{H_{c2}}{H_{c1}} + \frac{H_{c1}}{H_{c2}} - 1)B_{c2} \}$$
(10)

When  $H_a$  is chosen as the unknown variable, the radius  $R_a$  of the mean magnetic path corresponding to  $H_a$  is also unknown. As a result, the equation of  $H_a$  like Eq.(10) cannot be obtained. Therefore,  $H_a$  is not chosen as the unknown variable.



By calculating Eq.(2) for all MMF's (four kinds of MMF's in this case) in the same way mentioned above, the following matrix equation, in which the number of equations is equal to 2458

the number of the applied MMF's, is finally obtained for the case of Fig.4:

$$\begin{bmatrix} A_{11} A_{12} & 0 & 0 \\ A_{21} A_{22} A_{23} & 0 \\ A_{31} A_{32} A_{33} A_{34} \\ 0 & A_{42} A_{43} A_{44} \end{bmatrix} \begin{bmatrix} B_{c1} \\ B_{c2} \\ B_{c3} \\ B_{c4} \end{bmatrix} = \begin{bmatrix} B_{a1} \\ B_{a2} \\ B_{a3} \\ B_{a4} \end{bmatrix}$$
(11)

where  $B_{ak}$  is the average flux density for the k-th MMF shown in Eq.(2), and this is the known value.  $A_{kj}$  is the coefficient of  $B_{cj}$  in Eq.(11) for the k-th MMF. When the matrix equation is solved, the unknown variables  $B_{ck}$  (k=1,---,m) are obtained simultaneously.

Fig.6 shows the errors related to the new method obtained for the steel(SS400). Even in the case of  $\gamma=3.00$ , it is found that the errors of the new method are very small compared with those of the conventional method.



(b) Errors in magnetic field strength Fig.6 Errors related to new method (steel(SS400)).

#### IV. EXPERIMENTAL VERIFICATION

#### A. Preparation of Specimens

In order to examine the effect of the ratio  $\gamma$  on the accuracy of the estimated B-H curve, three kinds of ring specimens shown in Table 1 are tested. The ratios  $\gamma$  are chosen as 1.10, 1.36 and 3.00 respectively. The specimens are made of carbon steel which has a weak anisotropy. In order to avoid an additional error due to the anisotropy, the specimens are cut from one lot as shown in Fig.7, so that the flux flows perpendicular to the rolling direction. A bar specimen shown in Fig.7(b) is prepared for the permeameter method for measuring the dc magnetic properties of solid steels (Type A in IEC Publication 404-4, N63) [1]. All specimens are annealed for 1.5 hours at about 650°C in nitrogen (N<sub>2</sub>). The accurate final reprocessing is done after annealing.

#### B. Results and Discussion

Fig.8 shows the B-H curves obtained by the proposed method, the conventional method and the permeameter method [1]. In the case of  $\gamma$ =3.00, the error EB related to the conventional method was about 40% at H=100(A/m). The value is smaller than that for the case of SS400 shown in Fig.3(a). If the squareness of the B-H curve is near 1.0, the error may be much larger.



#### V. CONCLUSIONS

The effects of the shape of the B-H curve and the ratio of the outside radius to the inside radius on the error of the measured B-H curve are discussed. A new method for determining a dc magnetization curve accurately is proposed. The validity of the proposed method is also verified by experiments.

Experimental investigation should be continued to clarify the error of the conventional method for various kinds of specimen with different curve squareness.

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