INTERNATIONALE VEREINIGUNG FÜR THEORETISCHE UND ANGEWANDTE LIMNOLOGIE

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ASSOCIATION INTERNATIONALE DE LIMNOLOGIE THEORIQUE ET APPLIQUEE

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Volume 24 · Part 5

Edited for the Association by V. Sladeček and A. Sladečkova

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Contents of Part 5

XII. Ecology of Aquatic Organisms. 2. Algae and Macrophyta (continued)

| VAN DER DOES, J. & KLINK, F. J.: Excessive growth of Lemnaceae and <i>Azolla</i> in ditches observed by false colour teledetection | 2683 |
|---|------|
| KOK, C. J. & VAN DE LAAR, B. J.: Influence of pH and buffering capacity on the decomposition of <i>Nymphaea</i> alba L. detritus in laboratory experiments: A possible explanation for the inhibition of decomposi- tion at low alkalinity | 2689 |
| VAN DEN BRINK, F. W. B., MAENEN, M. M. J., VAN DER VELDE, G. & DE VAATE, A. B.: The (semi-) aquatic vege- tation of still waters within the floodplains of the rivers Rhine and Meuse in The Netherlands: Historical changes and the role of inundation | 2693 |
| VAN VIERSSEN, W. & HOOTSMANS, M. J. M.: On the origin of macrophyte population dynamics during lake recovery after eutrophication | 2700 |
| HOOTSMANS, M. J. M. & VAN VIERSSEN, W.: Computer simulations of macrophyte population dynamics during lake recovery after eutrophication | 2703 |
| COOPS, H. & SMIT, H.: Effects of various water depths on <i>Scirpus maritimus</i> L.: Field and experimental observations | 2706 |
| CLEVERING, O. A. & v. GULIK, W. J. M.: The establishment of <i>Scirpus lacustris</i> ssp. <i>lacustris</i> and <i>S. maritimus</i> in the northern Delta area, The Netherlands | 2711 |
| GACIA, E. & BALLESTEROS, E.: Two methods to estimate leaf production in <i>Isoetes lacustris</i> L.: A critical assessment | 2714 |
| VIAROLI, P. & FUMAGALLI, I.: Regeneration of dissolved reactive silica during decomposition of recalcitrant plant tissues in temporary shallow-water environments | 2717 |
| BREEN, C. M. & STORMANNS, CH.: Observations on the growth and production of <i>Cyperus papyrus</i> L. in a sub-tropical swamp | 2722 |

XII. Ecology of Aquatic Organisms. 3. Animals

| MEISTERFELD, R.: Vertical distribution of <i>Difflugia hydrostatica</i> (Protozoa, Rhizopoda) | 2726 |
|--|------|
| Ocaña, A. & PICAZO, J. S.: Study on nematode species encountered in the Monachil River (Granada, | |
| Spain): Response to organic pollution | 2729 |
| WARNER, B. G. & CHENGALATH, R.: Habrotrocha angusticollis (Bdelloidea, Rotifera): A new paleoecological | |
| indicator in Holocene peat deposits in Canada | 2738 |
| DE MANUEL, J.: Distribution of Brachionidae (Rotifera: Monogononta) in Spanish reservoirs | 2741 |
| ESPARCIA, A., ARMENGOL, J., VICENTE, E. & MIRACLE, M. R.: Vertical distribution of Anuraeopsis species as | |
| related to oxygen depletion in two stratified lakes | 2745 |
| WALZ, N. & ROTHBUCHER, F.: Effect of food concentration on body size, egg size, and population | |
| dynamics of <i>Brachionus angularis</i> (Rotatoria) | 2750 |
| CARMONA, M. J. & SERRA, M.: Comparative total protein and demographic patterns of mictic and amictic fe- | |
| male rotifers | 2754 |
| ROTHHAUPT, K. O.: The influence of toxic and filamentous blue-green algae on feeding and population growth of the rotifer <i>Brachionus rubens</i> (Abstract) | 2760 |
| MATVEEVA, L. K.: Can pelagic rotifers be used as indicators of lake trophic state? | 2761 |
| BONACINA, C., BONOMI, G., DI COLA, G. & MONTI, C.: An improved model for the study of population dynamics in <i>Tubifex tubifex</i> (Oligochaeta, Tubificidae) | 2764 |
| VIJVERBERG, J. & KOELEWIJN, H. P.: Size dependent mortality and production of Diaphanosoma brachyurum | |
| (LIEVEN) in an eutrophic lake | 2768 |
| HERZIG, A. & AUER, B.: The feeding behaviour of Leptodora kindti and its impact on the zooplank- | |
| ton community of Neusiedler See (Austria) (Abstract) | 2772 |
| SIEBECK, O. & BÖHM, U.: UV-B effects on aquatic animals | 2773 |
| DUNCAN, A. & DOS SANTOS, L. C.: Cohort analysis in three species of Daphnia in the London reser- | |
| voirs | 2778 |
| GERRITSEN, J. J.: The influence of phosphorus-limited grown algae on grazing of Daphnia magna | |
| (Abstract) | 2783 |
| GABRIEL, W. & TAYLOR, B. E.: Optimal resource allocation in cladocerans | 2784 |
| GIANI, A.: The nutritive value of different algae as food for two <i>Daphnia</i> species | 2788 |
| | |

XXXVI

| FUHLENDORF, D. C.: Measuring seasonal patterns of food limitation in <i>Daphnia</i> – an experimental study BERBEROVIĆ-JUNGE, R.: Starvation resistance of two coexisting <i>Daphnia</i> species under temperature con- | 2792 |
|--|------|
| ditions simulating vertical migration behaviour (Abstract) | 2794 |
| GLIWICZ, M. Z.: Food thresholds, resistance to starvation, and cladoceran body size | 2795 |
| WOLF, H. G. & WEIDER, L. J.: Do life-history parameters of Daphnia as determined in the laboratory cor- | 2700 |
| rectly predict species successions in the field? | 2799 |
| TOLLRIAN, R.: Some aspects in the costs of cyclomorphosis in Daphnia cucullata | 2802 |
| RINGELBERG, J.: The relation between ultimate and proximate aspects of diel vertical migration in <i>Daphnia</i> <i>hyalina</i> | 2804 |
| LEHTOVAARA, A. & SALONEN, K.: Diel vertical migration of Daphnia longispina in a humic lake with steep | |
| thermal and oxygen stratification (Abstract) | 2808 |
| GORBI, G., PARIS, G. M., MORONI, F. & BACHIORRI, A.: Differences in population dynamics of <i>Daphnia magna</i> clones | 2809 |
| BACHIORRI, A., ROSSI, V., BONACINA, C. & MENOZZI, P.: Enzymatic variability of a colonizing population of | 2007 |
| Daphnia obtusa Kurz (Crustacea, Cladocera) in Lake Orta (Italy) | 2813 |
| Rossi, V., Rozzi, M. C. & Menozzi, P.: Life strategy differences among electrophoretic clones of <i>Heterocypris</i> incongruens (Crustacea, Ostracoda) | 2816 |
| Снарман, М. А., Green, J. D. & Northcote, T. G.: The enigma of <i>Diaptomus connexus</i> (Copepoda) in Ma- | 2010 |
| | 2820 |
| honey Lake: One or two populations? (Abstract) | 2020 |
| HARTMANN, H. J.: In situ predation on planktonic ciliates by copepods, measured with diffusion exclosures (Abstract) | 2021 |
| | 2821 |
| FERRARI, I., FARABEGOLI, A., PUGNETTI, A. & STELLA, E.: The occurrence of a calanoid Australasian species, | 2022 |
| Boeckella triarticulata (Тномson), in fish ponds of Northern Italy | 2822 |
| MALY, E. J.: Dispersal ability and its relation to incidence and geographic distribution of Australian | 2020 |
| centropagid copepods | 2828 |
| BURNS, C. W. & XU, Z.: Utilization of cyanobacteria (blue-green algae) as food by freshwater calanoid co- | 2022 |
| pepods (Abstract) | 2833 |
| VILLALOBOS, L. & ZUNIGA, L.: Latitudinal gradient and morphological variability of copepods in Chile: | 2024 |
| Boeckella gracilipes DADAY | 2834 |
| WYNGAARD, G. A.: Evidence of food limitation in a subtropical copepod population | 2839 |
| ELGMORK, K.: Winter reproduction strategies in freshwater cyclopoids | 2844 |
| HALVORSEN, G.: The ecology of Cyclops abyssorum tatricus KOZMINSKI in Norway (Abstract) | 2847 |
| VAN DEN BOSCH, F. & GABRIEL, W.: The impact of cannibalism on the population dynamics of cyclopoid copepods | 2848 |
| | 2848 |
| SANTER, B.: The role of food limitation in summer diapause of cyclopoid copepods (Abstract) ADRIAN, R.: The feeding behaviour of <i>Cyclops kolensis</i> and <i>C. vicinus</i> (Crustacea, Copepoda) | 2851 |
| GROSSNICKLE, N. E.: Comparative feeding study of the opossum shrimp, Mysis relicta, in Trout Lake, | 2652 |
| Wisconsin, USA, Lake Pääjärvi, Finland, and Lake Jonsvatn, Norway | 2864 |
| | 2004 |
| YOUNG, L. B. & HARVEY, H. H.: The influence of lake pH and crayfish size on carapace elemental compo- sition in <i>Orconectes</i> spp. and <i>Cambarus</i> spp. | 2869 |
| CHAISEMARTIN, C.: Respiratory rates and adenylate energy charge in healthy and parasitized muscles of cray- | 2007 |
| fish (Austropotamobius pallipes) | 2873 |
| SCHMIDT-HALEWICZ, S. & BAUER, J.: Response of the macroinvertebrate community in NTA-, phosphate- | 2075 |
| and copper-charged freshwater ponds | 2877 |
| ALLAN, J. D., FLECKER, A. S. & KOHLER, S. L.: Diel changes in epibenthic activity and gut fullness of some | 20// |
| mayfly nymphs | 2881 |
| Zwick, P.: Growth and emergence of <i>Leuctra prima</i> (Plecoptera): Habitat – species interactions | 2886 |
| NEUMANN, P.: The egg development of <i>Brachyptera seticornis</i> (Insecta, Plec.) (Abstract) | 2891 |
| RUPPRECHT, R. & FRISCH, S.: The sensitivity of <i>Nemurella pictetii</i> (Insecta: Plecoptera) to acidity | 2892 |
| MALMQVIST, B.: Stonefly functional responses: Influence of substrate heterogeneity and predator interac- | 2072 |
| tion | 2895 |
| AURICH, M., WAGNER, R., REDER, E. & VEITH, R.: Defensive behaviour of the larva of Apatania fimbriata | 2075 |
| | 2901 |
| (Pictet)(Abstract) Миотка, Т.: Life history patterns of <i>Rhyacophila obliterata</i> in northern Finland (Abstract) | 2901 |
| JACKSON, J. K. & RESH, V. H.: Use of cellulose acetate electrophoresis to examine population gene- | 2702 |
| | 2903 |
| tics of the caddisfly <i>Helicopsyche borealis</i> ERLANDSSON, A.: Group dynamics in the water cricket <i>Velia caprai</i> (Hemiptera) | 2903 |
| GÍSLASON, G. M. & JÓHANNSSON, V.: Effects of food and temperature on the life cycle of Simulium | 2700 |
| vittatum ZETT. (Diptera: Simuliidae) in the River Laxá, N-Iceland | 2912 |
| \mathcal{O} | 6/12 |

XXXVII

| REIDELBACH, J.: Studies on population dynamics of blackflies (Diptera: Simuliidae) in a grassland stream (Abstract) | 2917 |
|--|------|
| SMIT, H., KLAREN, P. & SNOEK, W.: <i>Lipiniella arenicola</i> SHILOVA (Diptera: Chironomidae) on a sandy flat in the Rhine-Meuse estuary: Distribution, population structure, biomass and production of larvae in | |
| relation to periodical drainage | 2918 |
| HEINIS, F.: The relation between oxygen regimes and distribution patterns of the larvae of Chironomi- dae (Abstract) | 2924 |
| CURE, V.: Structure and ecological role of phytophilous chironomids from some Danubian ecosystems in | |
| Romania | 2925 |
| SAVAGE, H. M., REJMÁNKOVÁ, E., ARREDONDO-JIMENEZ, J. I., ROBERTS, D. R. & RODRIGUEZ, M. H.: Preliminary limnological and botanical characterization of larval habitats for two primary malarial vectors, <i>An</i> - | |
| opheles albimanus and An. pseudopunctipennis, in coastal areas of Chiapas State, Mexico (Abstract) | 2930 |
| WOLF, B. A. M.: Some aspects of the nutritional ecology of a detritus-feeding Diptera larva: Ptychoptera pa- | |
| ludosa (Abstract) | 2931 |
| YAMÉOGO, L., CALAMARI, D., GRUNEWALD, J. & FAIRHURST, C. P.: The aquatic monitoring and bioassay com- | |
| ponent of the WHO Onchocerciasis Control Programme in West Africa | 2932 |
| ALOI, J. E. & BRÖNMARK, C.: Effects of snail density on snail growth and periphyton | 2936 |
| JOKINEN, E. H .: The malacofauna of the acid and non-acid lakes and rivers of the Adirondack Moun- | |
| tains and surrounding lowlands, New York State, USA | 2940 |
| DORGELO, J.: Growth, food and respiration in the prosobranch snail Potamopyrgus jenkinsi (E. A. | |
| Sмітн) (Hydrobiidae, Mollusca) | 2947 |
| YIPP, M. W.: The relationship between hydrological factors and distribution of freshwater gastropods in | |
| HongKong | 2954 |
| RICCARDI, N., MANGONI, M. & PIVA, A.: The elemental (C, H, N, O, S) and biochemical composition of | |
| Unio mancus (PFEIFFER) and Anodonta cygnea L. | 2960 |
| TOKESHI, M.: Aggregation, habitat characteristics and species coexistence (Abstract) | 2964 |
| FRANCE, R. L. & WELBOURN, P. M.: Abundance of <i>Rana clamitans</i> tadpoles in Canadian Shield lakes | 2965 |
| (Hg) and pulsed (Chernobyl ¹³⁷ Cs) contaminants | 2970 |

XIII. Sediments

| CURTIS, P. J.: P and Fe release from anoxic Precambrian Shield lake sediments mediated by addition | |
|---|------|
| of Fe(II)-insoluble and Fe(II)-soluble bases | 2976 |
| ROWAN, D. J. & KALFF, J.: The limnological implications of catchment sediment load | 2980 |
| CARACO, N. F., COLE, J. J. & LIKENS, G. E.: Phosphorus release from anoxic sediments: Lakes that break | |
| the rules | 2985 |
| the rules | |
| spheric deposition | 2989 |
| EKHOLM, P., YLI-HALLA, M. & KYLMÄLÄ, P.: Availability of phosphorus in suspended sediments | |
| estimated by chemical extraction and bioassay | 2994 |
| HUPFER, M. & UHLMANN, D.: Microbially mediated phosphorus exchange across the mud-water interface | 2999 |
| KJENSMO, J.: Bio-geochemical composition of recent sediments from the mixo- and the monimolimnion of | |
| Lake Svinsjøen | 3004 |
| HORI, R., HJ. IKHSAN, S. BIN, WOOD, ABD. K. BIN & ABU BAKAR, MD. Y. BIN: Neutron activation analysis of | |
| the sediment of Kelang River, Malaysia | 3009 |
| SAGER, M.: Detection of environmental mobilities of nutrients and heavy metals in sediments | 3012 |
| OSBORNE, P. L. & TOTOME, R. G.: Sediment deposition in Lake Kutubu, Papua New Guinea | 3018 |
| TATUR, A., DEL VALLE, R. & PAZDUR, M.: Lake sediments in maritime Antarctic zone: A record of land- | |
| scape and biota evolution: preliminary report | 3022 |
| GOLTERMAN, H. L.: Influence of FeS on denitrification in shallow waters | 3025 |
| DE GROOT, CJ.: The influence of FeS on the inorganic phosphate system in sediments | 3029 |
| KOYAMA, T.: Biochemical reduction process in the lake sediment-water interface. On the basis of | |
| laboratory experiments | 3036 |
| MARXSEN, J. & FIEBIG, D.: Measurement of bacterial production in stream-bed sediments (Abstract) | 3044 |
| Томазzeк, J.: Oxygen consumption by bottom sediments | 3045 |
| WASMUND, N.: Microautoradiographic determination of the viability of algae in deep sediment layers (Ab- | |
| stract) | 3050 |
| ANDERSEN, F. Ø. & JENSEN, H. S.: The influence of chironomids on decomposition of organic matter and | |
| nutrient exchange in a lake sediment | 3051 |
| | |

XXXVIII

| IWAKUMA, T. & OTSUKI, A.: Role of chironomid larvae in reducing rate of nutrient release from lake | |
|--|------|
| sediment: Evaluation by a mathematical model | 3056 |
| SCHROEDER, F., KLAGES, D. & KNAUTH, HD.: Contributions of sediments to the nitrogen budget of the Elbe | |
| estuary | 3063 |
| KERNER, M.: The coupling of microbial respiration processes within the two-dimensional spatial structure | |
| of an intertidal mud flat sediment of the Elbe Estuary | 3067 |
| WILTSHIRE, K. H.: Experimental procedures for the fractionation of phosphorus in sediments with emphasis | |
| on anaerobic techniques | 3073 |
| WILTSHIRE, K. H.: Experimental procedures for the fractionation of phosphorus in sediments with emphasis | |

XIV. Received too late for classification

| HERRMANN, J.: Bioindication of nutrient and organic pollution by benthic stream invertebrates – pitfalls and problems (Abstract) | 3079 | | |
|---|-------------|--|--|
| MUNAWAR, M., LEPPARD, G. G. & MUNAWAR, I. F.: Ecotoxicology of stressed environments: Structural and functional strategy | 3080 | | |
| WARD, J. V. & STANFORD, J.: Benthic faunal patterns along the longitudinal gradient of a Rocky Mou river system | | | |
| Overbeck, J.: Plenary lecture: Initial, present and future aim of limnology | 3095 | | |
| Societas Internationalis Limnologiae: Twenty-Fourth Congress, Munich/Federal Republic of Germany, 1989 | 3102 | | |
| Officers and list of members Contents of volume 24 (completely) | 3137 (1) | | |

24

Optimal resource allocation in cladocerans

Wilfried Gabriel and Barbara E. Taylor

Introduction

The natural pattern for growth and reproduction of cladocerans results in continued growth during most or all of adult life. This reproductive strategy is not well understood because optimal control theory predicts simultaneous growth and reproduction only under very special conditions (SIBLY et al. 1985) which are unlikely to obtain for cladocerans. Theoretically preferred is the "bang-bang" strategy: no investment into reproduction until an optimal switching point is reached, then no further growth. TAYLOR & GABRIEL (1985) showed that indeterminate growth of Daphnia pulex and D. pulicaria is suboptimal under the assumption of constant mortality. To explain why Simocephalus vetulus (MÜLLER), another daphniid cladoceran, is not a "bang-bang strategist", PERRIN et al. (1987) proposed that structural constraints such as size of the brood chamber could require continued growth after first reproduction.

Because reproductive output is among the most important components of fitness, one can expect that the resource allocation pattern has been shaped by strong selection pressure during evolution. But there are many plausible excuses for disagreements between theory and nature. Genetic, developmental, physiological, or other factors that could constrain an organism from achieving optimal allocation are poorly known and thus difficult to include in a model. Before invoking such constraints to reconcile nature to theory in the case of resource allocation for Daphnia, we decided to analyse the problem further. From laboratory data for Daphnia pulex, we constructed a model in which adult growth and reproduction are functions of resource allocation. We numerically solved the model for optimal resource allocation patterns under various conditions. These optimal patterns are more similar to natural patterns than previous analyses led us to expect, and they indicate how selection may have shaped the life histories of cladocerans.

Methods and model

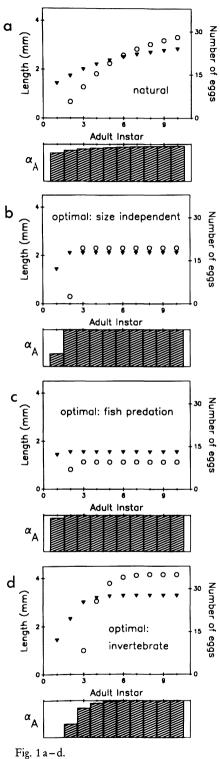
To describe growth and reproduction of cladocerans we used laboratory data for *Daphnia pulex* (TAYLOR 1985). From these measurements we estimated the various functions and parameters of the model, including net production as a function of body size and food concentration. Production is modelled as a continuous process during the intermolt; reproduction and change in body size are implemented as discrete events at instar transitions. For each adult instar A the allocation α_A of net production P_A to reproduction determines growth and reproduction: the number of eggs produced is proportional to $\alpha_A P_A$ and the weight increment is proportional to $(1-\alpha_A)P_A$. Measured values of α_A were used in this model to describe the natural allocation pattern. To find the optimal resource allocation patterns, we chose intrinsic growth rate r as our measure of fitness. For any specified size dependent mortality scheme, the life history parameters l_x (survival probability) and m_x (reproduction) are constants or functions of the α_A 's. Therefore, the discrete form of the renewal equation

$$1 = \sum l_x m_x \exp(-rx)$$

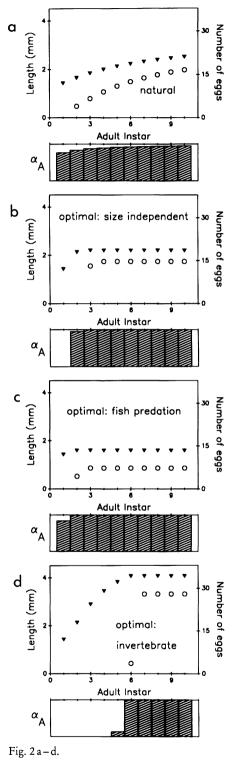
can be used to calculate numerically those α_A -values which maximize r. We assume three simple cases of mortality: i) size-independent, ii) survivorship linearly decreasing with body length to model a fish-like predation, and iii) survivorship linearly increasing with body length to represent invertebrate predation. For the results presented, the size-independent mortality is assumed to be 10% per adult instar and the size-dependent mortality is calculated as increasing or decreasing linearly with body length so that at 0.75 mm or 3.5 mm the mortality becomes 10% or 60%. A more detailed description of the model will be given elsewhere (TAYLOR & GABRIEL 1992).

Results and discussion

The natural pattern of growth and reproduction at abundant food is given in Fig. 1 a. The frequency histogram below the figure represents the part α_A of net production that is allocated to reproduction. We count the last juvenile instar where allocation to reproduction can start as A = 1. (The eggs resulting from this allocation are laid at the beginning of instar 2 and hatch at end of instar 2.) At this instar already 76% of net production is devoted to reproduction. This allocation increases to over 95% at adult instar 10, resulting in small but continuous growth after first egg production. This natural pattern is contrasted by the model results in Fig. 1 b-d. With size-independent mortality



(Legends of Figs. 1 + 2 see next page)



(Legends of Figs. 1 + 2 see next page)

Table 1. Intrinsic growth rates r for the best "bang-bang strategy" and comparison of r under natural resource allocation with the optimal values achievable for assumed size-independent mortality, fish-like and invertebrate-like predation risks under abundant and limited food conditions.

| food | predation | optimal | natural | difference | | bang-bang |
|------|--------------|---------|----------------------|----------------------|------|-----------|
| | | | r [d ⁻¹] | r [d ⁻¹] | abs. | rel. [%] |
| high | independent | 0.3412 | 0.3368 | 0.0044 | 1.3 | 0.3389 |
| | fish | 0.2710 | 0.2592 | 0.0118 | 4.3 | 0.2702 |
| | invertebrate | 0.1909 | 0.1460 | 0.0449 | 23.5 | 0.1897 |
| low | independent | 0.2314 | 0.2247 | 0.0067 | 2.9 | 0.2313 |
| | fish | 0.1665 | 0.1607 | 0.0058 | 3.5 | 0.1648 |
| | invertebrate | 0.0873 | 0.0183 | 0.0690 | 79.0 | 0.0864 |

(Fig. 1 b) the optimal strategy is to cease growing after one intermediate allocation to reproduction. Qualitatively the same is predicted if the mortality increases with body length (Fig. 1 c), but the first intermediate allocation to reproduction is higher and consequently the final body size is smaller than for size-independent mortality. Under invertebrate predation (Fig. 1 d) it is optimal to postpone the first reproduction by one instar and to have four intermediate allocations before investing all into reproduction. The largest final body size would be attained with this allocation pattern.

The natural allocation pattern seems to be quite independent of food level (TAYLOR 1985, LYNCH 1989), and it seems to be mainly a function of weight and/or age. At least for the Daphnia pulex clone used in the experiments by TAYLOR, the natural α_A values are a function only of the instar number. Therefore, limited food implies retarded growth and fewer eggs without any qualitative change in the natural allocation pattern (Fig. 2a). The optimal strategy under size-independent mortality delays reproduction by one instar (Fig. 2b), as compared to the high food situation. Food shortage does not change the optimal strategy under fish predation very much (Fig. 2 c), but the intermediate α_A is lower, i.e. allocation gives a higher proportion to growth, so that the final body size is similar. Under invertebrate predation

the optimal strategy strongly depends on the food level. Optimization with limited food postpones the first reproduction further, and there is only one intermediate allocation before reaching the final body size, which is larger than under abundant food.

Table 1 compares the intrinsic growth rates for natural and optimal allocations and the best "bang-bang" allocation for various predation schedules and food levels. The simple optimal control model obviously does not predict intermediate allocations and its "bang-bang strategy" can result in higher r values than natural allocation. The fitness under this strategy is very close but always below the optimum which our model reaches with intermediate allocations. The natural resource allocation seems to be suboptimal under all conditions tested. Invertebrate predation produces the largest deviations from the optimal values. In most cases, however, the realized fitness is very close to its maximum, so that indeterminate growth seems not to be very expensive. Similar results are obtained with more complicated predation schedules, such as arctangent or parabolic functions. A weak point of any such optimization is the underlying assumption of constant environmental conditions within and between generations.

But ponds and lakes are temporally variable, and thus cladocerans perceive a variety of environments even during one growing season. One can question whether the intrinsic growth rate is the appropriate fitness measure under variable environmental conditions. Optimizing the total reproductive output can lead to indeterminate growth as shown by GABRIEL (1982) in a different model approach. Other measures of fitness will be discussed elsewhere in detail; e.g. for non-overwintering cladocerans the number of adults able to produce resting eggs at the end of the season might be a better fitness measure.

If the environment changes from generation to generation one has to maximize the geometric mean fitness over successive generations. The re-

Fig. 1. Body size (= triangles) and fecundity (= circles) at abundant food resulting from allocation α_A of net production to reproduction (histogram below figure) for adult instars A starting with A = 1 as the last juvenile instar where first allocation to reproduction can occur. a) Natural allocation. b – d) Model results under the assumption of size-independent mortality (b), fish (c), and invertebrate predation (d).

Fig. 2. Same as Fig. 1 but for limited food (30 % below the incipient limiting level).

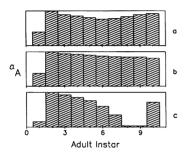


Fig. 3. Optimal resource allocation α_A of net production to reproduction if mortality varies between generations. a) Equal probability is assumed for fish and invertebrate predation at abundant food. b) As a) but with size-independent mortality as a third equal probable predation schedule. c) As b) but for limited food (30% below the incipient limiting level).

sulting optimal resource allocation is then not just a superposition of the results under constant conditions. This is demonstrated in Fig. 3 for the simple case that food is always constant but predation changes between generations. In reality we must of course consider that food conditions and kind and intensity of predation may change between generations and as well within generations. Depending on the frequency of the various environments this probably can result in almost any optimal resource allocation pattern.

More detailed measurements on resource allocations and its correlation with other life history parameters of different clones and species would be helpful to gain more insight into the selective forces shaping the observed growth and reproduction patterns. From our model we conclude: The natural resource allocation pattern with its consequences of indeterminate growth is suboptimal for any constant environment, but it can be understood as adaptive to variable environments which change between generations in food availability and predation risk.

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