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Simulation of low rigidity part machining applied to thin-walled structures

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Abstract The aim of this study is to evaluate the modelling of machining vibrations of thin-walled aluminium workpieces at high productivity rate. The use of numerical simulation is generally aimed at giving optimal cutting conditions for the precision and the surface finish needed. The proposed modelling includes all the ingredients needed for real productive machining of thin-walled parts. It has been tested with a specially designed machining test with high cutting engagement and taking into account all the phenomena involved in the dynamics of cutting. The system has been modelled using several simulation techniques. On the one hand, the milling process was modelled

using a dynamic mechanistic model, with time domain simulation. On the other hand, the dynamic parameters of the system were obtained step by step by finite element analysis; thus the variation due to metal removal and the cutting edge position has been accurately taken into account. The results of the simulations were compared to those of the experiments; the discussion is based on the analysis of the cutting forces, the amplitude and the frequency of the vibrations evaluating the presence of chatter. The specific difficulties to perfect simulation of thin-walled workpiece chatter have been finely analysed.

Keywords High-speed machining · Milling · Thin wall · Chatter · Time domain simulation

Sadly, Grégoire Peigné died during the preparation of the article.

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1 Introduction

Nowadays metal machining is one of the most important manufacturing processes, and the technology of this process has been widely developed in recent years, with advances covering the process itself, machines, materials, simulation, sensors, etc. However, productivity is often limited by strong vibrations; this regenerative vibration creates chatter. Chatter causes poor surface roughness, increases the rate of tool wear and reduces the spindle life span. The scope of simulation has increased dramatically over the past decade, and it is merely the beginning for machining processes. The real aim of simulation in machining is to represent behaviour during the process and to give accurate predictions for use in designing the product or the machining process. The trial-and-error method—which is time consuming and expensive—is still widely used to optimise the machining process. The initial steps may be simulated very early, before actual machining.

However, the study of stability lobes diagram for machining started many long years ago with the first work by Tobias et al. [1] and Tlustý et al. [2]. This theory was extended to the milling process [3, 4]. More recently, modelling was improved by more detailed analysis of the governing delay differential equation; see, for example [5–7]. These new analytical methods allow a new type of instability called period doubling or flip bifurcation [8–10]. In the special case of thin-wall milling, stability lobes cannot be applied directly because of dynamic change during machining, in particular the tool position and the material removed. In order to stage this defect, Lapujoulade et al. [11] studied the part per small zones. In these zones, the part was able to be modelled with constant dynamic properties and with rigid body motion [12]. The stability lobe change during machining that lead to a third dimension on the stability lobe [13, 14]. This approach was also extended by taking into account machine and tool flexibility [15]. All these analytical methods give direct explanations of the stability in machining [16]; however, many effects are very difficult to model by using these analytical approaches due to the complexity of the peripheral milling of thin-walled parts.

In the field of the dynamic study of milling, time domain simulation has also been used for many years. This modelling technique is useful in the detailed examination of effects which are too difficult to model by analytical means. Kline et al. [17] developed a refined model to predict static cutting forces with a tool decomposition into infinitesimal disc elements in order to improve the cutting force determination for helical cutters. Later, this approach was extended to all general milling cutters with various geometries [18]. Time domain simulation was also extensively used for dynamic milling modelling. The complexity of surface modelling prompted the first studies to focus only on modelling the regenerative phenomenon to analyse the stability of milling (see, for example, [19–21]). However, these first time simplified models simply can predict the stability lobes, as analytical methods. Few studies have aimed to predict the surface finish of the part. Montgomery and Altintas [22] provided a time domain milling model in which the surface profile, during simulation, is generated by linear interpolation. This approach was improved by quadratic interpolation [23] in order to reduce error. It is important to note that these works consider a flexible element, which can be the tool, the part or both of them, having a rigid body motion [24]. The time domain simulation of flexible parts like thin-walled structures has also been studied. Altintas et al. [25] developed a dynamic model using finite element modelling, in order to obtain the dynamic parameters of the part. This approach was later improved by considering the dynamic variation along the cutting depth of cut for both the cutter and workpiece [10, 26]. The generalisation of 3D surface profile modelling, for

complex thin-wall parts, requires a particularly improved geometrical model using Z-Buffer or Dixel [27]. For thin-wall milling, the non-linear impact of the ploughing effect or edge force was also taken into account more recently [28].

Many studies have described the stability and the simulation of the milling process in which the tool and the workpiece are considered a rigid body with one or more degrees of freedom. However, few works consider the real dynamic evolution for thin-wall milling.

The aim of this work is to simulate the machining process of low rigidity parts with significant cutting engagement in order to increase the metal removal rate with the problems related to dynamic displacement. Our study uses a specially designed thin-walled workpiece and is aimed at obtaining variations of its dynamic properties during the process. The model considers the variations of the dynamics along the cutting depth of cut for the workpiece, the removal material and the tool path evolution throughout machining. The results of the model, i.e. displacement amplitude and spectrum, will be compared to the real machined part.

2 Model: milling process and dynamic properties of the workpiece

In this section, the test part is defined and then the various steps of the time domain simulation are presented.

2.1 Design of the test part and cutting conditions

In order to study a real machining case, a special part was designed. The machining process is shown in Fig. 1. The test consists of the progressive increase of axial depth of cut, with a strong effect on the dynamic parameters of material removal and tool position. The evolution of the parameters—axial depth of cut, material removal, dynamic stiffness along the tool path—is significant. The calculation is simplified by the continuity of parameter variation, the

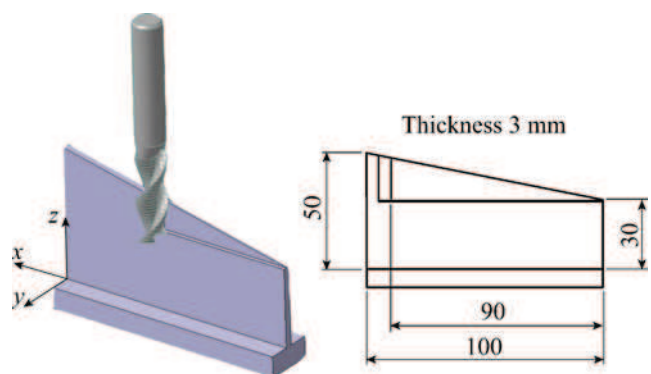


Fig. 1 Test workpiece

tool being much stiffer than the workpiece and the direction of the deformation being mainly along the y axis.

The down-milling operation consists of an axial depth of cut increasing from 0 to 19 mm. The radial depth of cut is 2 mm.

2.2 Milling modelling

As shown in Fig. 2, the dynamics of the workpiece are represented following a finite element analysis and the cutting force law is represented by a linear model. The finite element model is updated as the workpiece is machined. These two models are then used in the dynamic model of milling to represent the interaction between the instantaneous cutting force and dynamic displacement. This simulation predicts the stability and surface finish of the machined surface.

The basis of the dynamic milling model is given in [23, 29]. This model was developed to generate precisely the real chip thickness for a flexible workpiece. In this paper, the adaptation of this model is considered to take into account the evolution of the dynamic properties of thin wall during machining. The simulation uses an implicit scheme of time domain integration. In order to simplify the model, the following assumptions have been made:

- Vibrating occurs only along the y axis.
- The cutting zone corresponding to the tip of the tool is neglected.

2.3 Finite element analysis

In order to follow the variation of the workpiece during machining, several finite element modal analyses were carried out every 18 mm. The results are presented in Fig. 3

and Table 1. The evolution is smooth enough here to allow an interpolation between six calculations with less than 10% error. Following the previous assumptions (see section 2.2), in this case of modelling, the following considerations apply:

- Only the displacement along the y axis is significant.
- The dynamic properties of the workpiece change slowly compared to the variation time of the cutting forces.
- The displacement of the workpiece in the cutting zone depends only on time and z value, and it is related to the stiffness, mass, damping, frequency and shape of each mode.
- The first three modes represent the dynamic behaviour of the workpiece.

2.4 Mechanistic model of the cutting law

The mechanistic model gives the cutting force during milling; in this study, the model proposed by Altintas [4] is used. Figure 4 illustrates this model, which is in three steps:

- Calculation of the position of each discretized cutting edge.
- Corresponding depth of cut associated.
- Total of all the elementary forces.

At each discretized cutting edge, the following cutting law has been applied for tangential, radial and axial force:

$$\begin{cases} dF_t = K_{te}dS + K_{tc}hdz \\ dF_r = K_{re}dS + K_{rc}hdz \\ dF_a = K_{ae}dS + K_{ac}hdz \end{cases} \quad (1)$$

Fig. 2 Principles of modelling

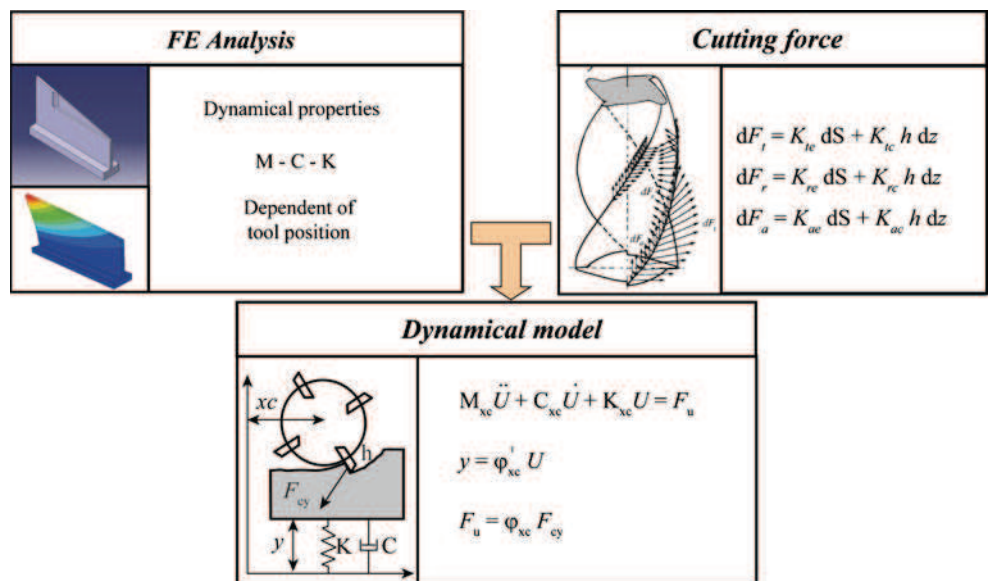
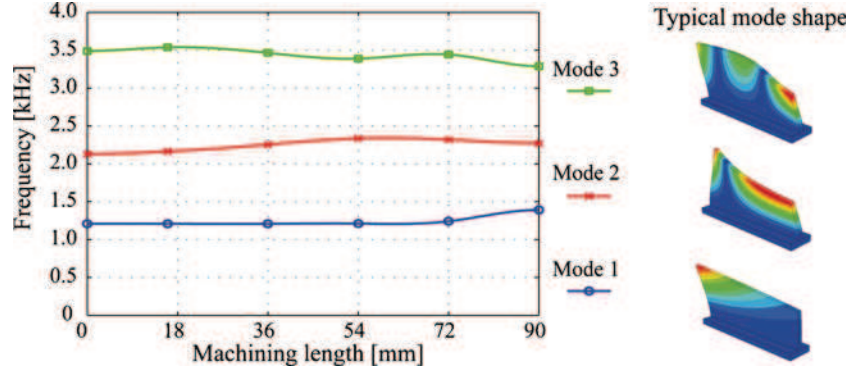


Fig. 3 Evolution of natural frequencies during machining



with dS the elementary length of the cutting edge, h the width of chip just before cutting and dz is the height of the elementary cutting edge considered. The model requires six coefficients K_{tc} , K_{rc} , K_{ac} , K_{te} , K_{re} and K_{ae} , which are experimentally determined (see section 3). They are mainly associated with the tool, the workpiece material and the presence of cooling fluid. The method used to determine these coefficients is the one proposed by Altintas [4].

2.5 Modelling of the flexible workpiece and of the milling process

The time domain simulation is resource consuming, and so it is necessary to choose the simplest model at each step of modelling. Due to the high stiffness level of the workpiece in x and z axis, it is possible to consider only the displacements

along the y axis. Because of the milling direction, it is possible to decompose the tool and the workpiece geometry using the steps along z as shown in Fig. 5. Thus, the surface is whole, consisting of profiles combined with an elementary height. Lastly, on each plane, the part has only a translating motion following the y direction and the value of the translation is the displacement of the surface point in front of the tool axis.

A modal basis is used to represent workpiece vibrating:

$$M_u \ddot{U} + C_u \dot{U} + K_u U = F_u \quad (2)$$

where $U = \{u_i\}_{i=1..n}$ is the modal time function vector associated with the n modes, F_u is the projected force vector and M , C and K are the modal matrices associated with mass, damping and stiffness. These matrixes are not constant during machining because of the material removed. They have been calculated by finite element analysis at several points along x during machining; between these points, cubic spline is used for interpolation. According to the previous assumptions, the displacement of the workpiece will be considered as a function of z and x along the machining surface. Displacement of the workpiece is calculated using the modal displacement functions u_i and shape functions ϕ (obtained by interpolation), as follows:

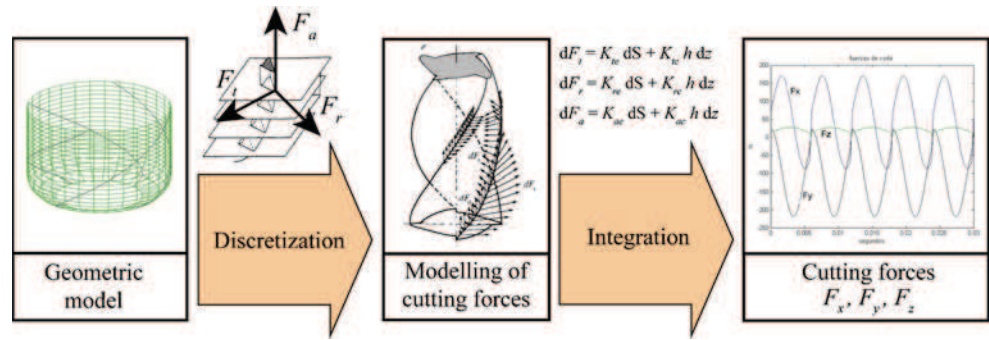
$$y(z) = \sum_{i=1}^3 u_i \phi_i(x, z) \quad (3)$$

The occurrence of ploughing is detected by monitoring the instantaneous clearance angle based on the current value of the velocity vector. The ploughing process proposed model is an elementary model increasing a viscous force when negative clearance angle was detected. This added damping produces a reduction of the vibrations in the unstable zone and the clearance angle condition is respected, that reduction means a damping rate over 1,000%. The value of this viscous force—linked to the ploughing effect—was determined by simulation. The influence of the damping rate on the simulation result is more detailed on the discussion section (see section 4.4).

Table 1 Evolution of the dynamic properties of the workpiece

Mode	Machined length [mm]	Frequency [Hz]	Damping [%]
1	0	1,209	0.6
	18	1,209	0.6
	36	1,208	0.6
	54	1,211	0.6
	72	1,241	0.6
	90	1,392	0.6
2	0	2,130	0.5
	18	2,164	0.5
	36	2,254	0.5
	54	2,335	0.5
	72	2,319	0.5
	90	2,271	0.5
3	0	3,489	0.3
	18	3,538	0.3
	36	3,464	0.3
	54	3,388	0.3
	72	3,443	0.3
	90	3,288	0.3

Fig. 4 Illustration of the mechanistic modelling of the cutting law



Finally, the global cutting force is obtained from the sum of the z -discretized forces, considering only the y axis. The modal project forces are expressed as follows:

$$F_{u,i} = \sum_z \varphi_i(x,z) \sum_n (dF_{l,z,n} \cos(\theta_{z,n}) + dF_{r,z,n} \sin(\theta_{z,n})) \quad (4)$$

3 Experimental setup and preliminary tests

The experimental tests were carried out on a Deckel-Maho DMU60L high-speed milling machine, from 10,000 to 18,000 rpm. The material is aeronautic aluminium Al-6082 T6. The tool is a monolithic carbide end mill, two teeth, 16-mm diameter, helix angle 45° , mounted on a HSK63A holder. The run-out was measured and used in the cutting force simulation to correlate with measurements.

Firstly, in order to obtain the specific coefficients of the tool-material combination, slot-milling experiments were conducted at different feed rates. The cutting conditions are defined in Table 2, and the experimental setup is shown in Fig. 6. The cutting force measurement was done using a three component Kistler 9257BA dynamometer. The obtained cutting coefficients are given in Table 3.

Secondly, the force modelling was validated with flank milling tests as seen in Fig. 7. Figure 8 shows the comparison between the simulated and the experimental

cutting force for this operation. There is a good correlation. The differences between modelling and experiments can be explained by the following arguments:

- When the chip thickness is close to zero, the force is minimal, but the friction contact generates a residual constant force. The modelling gives a near zero force because friction was not taken into account.
- When the chip is maximal, experiments give a higher force than simulation, probably because static and dynamic deflections were not taken into account in this modelling.

4 Thin-wall milling test and simulations

In this section, the results of the previous section are used for thin-wall milling. First, many tests were done in order to evaluate the stability of the machining. Then various comparisons between modelling and experiment were made.

4.1 Stability analysis

A set of nineteen experimental tests were carried out to evaluate the behaviour of the workpiece during machining

Fig. 5 z -Discretization of the surface

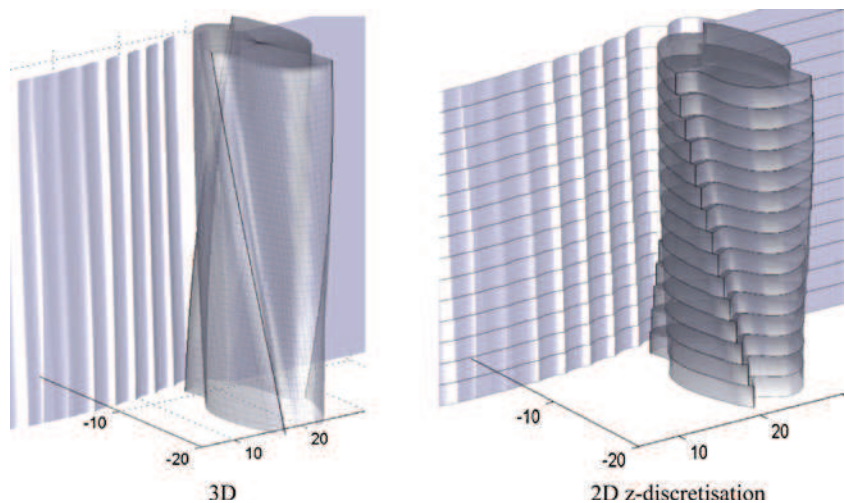


Table 2 Cutting condition used for the specific coefficients identification

Cutting conditions	Values
Cutting speed	502 m/min (10,000 rpm)
Feed rate	0.03; 0.05; 0.07; 0.12 mm/tooth
Axial depth of cut (A_p)	4 mm
Radial depth of cut (A_e)	16 mm (slotting)

and to validate the proposed milling model. The thin walls were down-milled, with axial depth of cut variable along the tool path from 0 to 19 mm, a radial depth of cut of 2 mm and a feed rate of 0.1 mm/tooth. The experimental setup is shown in Fig. 9. The displacement of the cutting zone of the workpiece—during milling—was measured with an eddy current sensor. The acoustic signal of a microphone was also recorded to detect vibration frequencies and chatter. The presence of unstable machining, i.e. chatter, is shown in Table 4.

Most of the tests show instability much before machining is completed mainly because there is an increasing axial depth of cut during the operation and different vibrating modes are involved in vibrations of this test part. The proposed milling test is a very unstable machining operation with only two rotating speeds avoiding chatter vibrations in the workpiece, 12,000 and 15,330 rpm.

We have often noted that machinists in industrial context do not hesitate to use the full machine capacities, as much as acceptable surface qualities make it possible. Here, we consider strong tool engagement for thin wall machining in order to test the simulation in a realistic context, as illustrated Table 4.

4.2 Frequency vibration

In order to validate the simulation, the results obtained from experimental tests were compared to the simulated data; the dynamic behaviour of the test piece during the machining operation is well described by the milling model according to the vibration frequency spectrum. Figure 10 shows a stable machining operation. The main peaks of the vibration spectrum are related to tooth passing frequency and its harmonics, which are forced vibrations. The strong influence of the harmonics can be explained by the interrupted nature of the cutting process with a radial immersion ratio of $A_e/D=0.125$.

Figure 11 shows the results for a spindle speed of 17,660 rpm. In this case, a chatter problem occurs in the zone between 10 and 20 mm. A peak can be seen in the frequency spectrum at 2,267 Hz, near the natural frequency of mode 2. Other harmonics of the forced vibrations are present, but in this case, the chatter frequency is clearly linked to the second mode of the part.

Figure 12 shows the results for a chatter problem in the zone between 0 and 10 mm; in this case, a peak at 3,627 Hz can be identified near the natural frequency of mode 3; it is also chatter frequency.

The experimental displacement and sound measurements show that the chatter is related to the three vibration modes considered. Moreover, the influence of each mode in the chatter vibrations is related to the x position, and this is clearly influenced by the mode shapes showed in Fig. 3, therefore:

- Mode 3 is the most important factor between 0 and 15 mm.
- Mode 2 is the most important factor between 15 and 25 mm.
- Mixed effects of Mode 2 and Mode 3 can be observed between 25 and 55 mm.
- Mode 1 is the most important factor in the final stage of machining.

The qualitative results obtained proved to have a useful model due to the fact that the simulations can predict the chatter problems at different zones of the workpiece. The correlation between the spectrum predicted by simulation and the experiment measurement also correspond.

4.3 Displacement vibration

To verify the predictive capabilities of the model, the simulation results were compared to the displacement directly measured during the thin-wall machining.

Figure 13 shows the behaviour of an unstable case for a spindle speed of 12,660 rpm. The experimental displacement measured during the test and the simulation results can be seen. Both displacements are also sampled at the tooth passing frequency. On the panel (a) (c), chatter cannot be seen clearly because amplitude would be affected by the run-out of the tool. However, on the panel (b) (d)—signal sampled at the tooth passing frequency—different vibrating behaviour is observed.

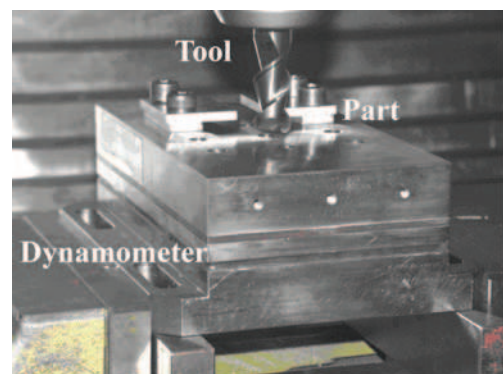
**Fig. 6** Preliminary experimental setup, for slotting test

Table 3 Specific cutting coefficient identified for Al-6082 T6

K_{tc} [MPa]	K_{rc} [MPa]	K_{ac} [MPa]	K_{te} [MPa]	K_{re} [MPa]	K_{ae} [MPa]
631	99	273	13	10	2.8

Between $x=0$ and 25 mm, both experimental and simulated results present an amplitude of about 0.4 mm. For these stable conditions (forced vibration), the curve of the panel (b) (d) is very smooth.

In contrast, between $x=25$ and 45 mm, there is a difference between the predicted amplitude and the measured amplitude. However, from a qualitative point of view, the phenomenon is detected by simulation. On the displacement sampled at the tooth passing frequency—panel (b) (d)—the curve shows more peaks and large variations over short periods of time, characteristic of unstable cutting condition with chatter. The surface finish and the marks present on the piece can confirm the machining area in which there has been instability during the process detected in this case between 25 and 45 mm on the machined length.

Between $x=45$ and 75 mm, both the simulation and the experiment are coherent. Stable cutting conditions are again present in this area, with smooth evolution of the sampled displacement.

Finally, between $x=75$ and 80 mm, different result appears between experiment and simulation. The large shift in the experimental data is linked to the stoppage of the tool speed; this stoppage implies a static movement of the part of about 1.5 mm. This phenomenon is not taken into account in modelling.

In conclusion, the trends discussed above can be observed both in the experimental signals and in the simulations, although the frequency spectrums of the peak values are comparable. Moreover, the experimental amplitude and the simulated amplitude are significantly different in unstable areas, while for stable cutting condition the vibration amplitudes are comparable, as shown in Fig. 13.

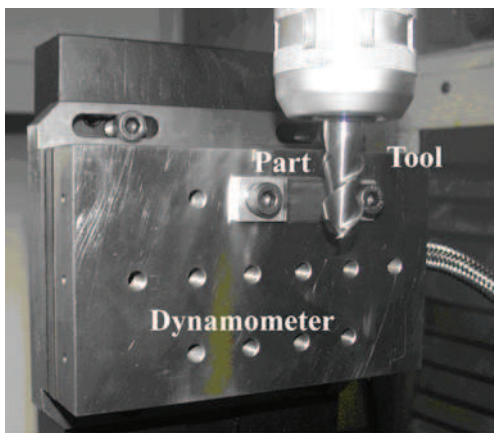


Fig. 7 Experimental setup for testing the cutting law, in flank milling

4.4 Discussion

A chatter model, developed and verified for several years [10, 21], was used in this study. Here, this model was applied on the milling of a flexible thin-wall workpiece with a large cutting tool engagement where chatter is a major problem that is very difficult to avoid.

The simulation results were compared with experimental tests. The dynamic behaviour of the workpiece during machining is very well described by the simulation according to the vibration frequency spectrum. For this qualitative aspect, the simulations match the experiments well. Regarding vibratory displacement, the experimental and simulated results are significantly different for the unstable cases, while for stable areas the amplitudes are comparable, as shown in Fig. 13. The discrepancies between simulated and experimental displacement can be observed for strong chatter cutting conditions. The correlations, although satisfactory, are actually not as good as those usually shown for single degree of freedom massive workpiece. The reproducibility of the machining test, the validity of the discretization parameters (spatially and temporally) and the robustness of the modal shape used have been confirmed. At present, it is not clear what causes these discrepancies. Possible reasons could be: the linear cutting law and the effect of the process damping.

For low chip thickness, it is difficult to consider direct proportionality between the chips and cutting forces—linear cutting law. A non-linear cutting law would be more efficient, but it would be necessary to develop a new method for the reliable identification of the cutting coefficients [30].

Process damping is often caused by the contact on the clearance face due to the vibration of the workpiece [22].

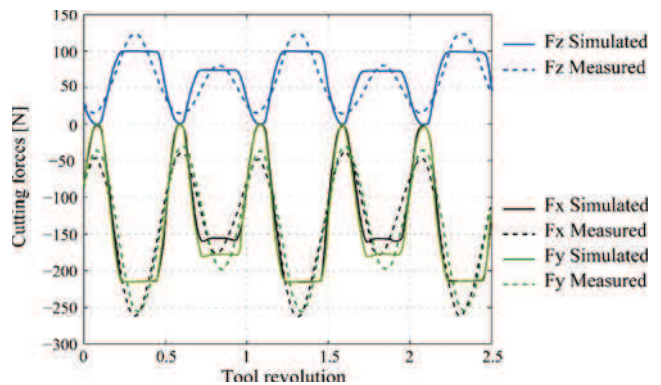


Fig. 8 Simulated and measured forces: side milling, $A_p=17.5$ mm, $A_e=2$ mm, $f_z=0.12$ mm/tooth, $N=5,000$ rpm

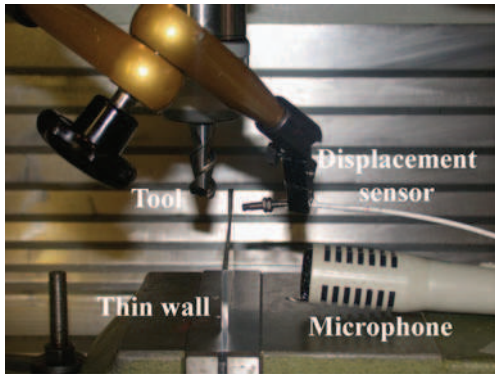


Fig. 9 Experimental setup for thin-wall milling

This ploughing effect increases the damping of the process, and the machining becomes more stable than the simulation [31]. In this way, other complementary simulations were made with different ploughing force models. The ploughing process model was an elementary model increasing the damping of the system when negative clearance angle was detected. The fact that the ploughing effect occurs in only during very short periods (1% to 10% of the time of passage of tools) led us to concentrate on its modelling study. Indeed, it shows both by simulation and experiment that thin walls are very sensitive to the cutting and ploughing forces that can virtually immobilize the thin-walled or restart by one single tooth contact, unlike what happens on parts with higher inertia. The ploughing force is modelled by a viscous force, which allows an important

Table 4 Stability of the cutting tests

Spindle speed [rpm]	Stability
12,000	No chatter
12,330	Chatter
12,660	Chatter
13,000	Chatter
13,330	Chatter
13,660	Chatter
14,000	Chatter
14,330	Chatter
14,660	Chatter
15,000	Chatter
15,330	No chatter
15,660	Chatter
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16,330	Chatter
16,660	Chatter
17,000	Chatter
17,330	Chatter
17,660	Chatter
18,000	Chatter

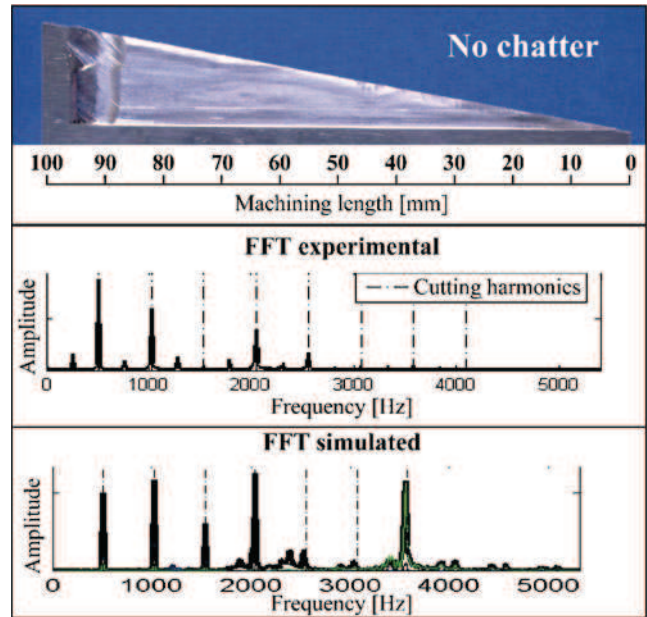


Fig. 10 Results comparison for chatter free machining at 15,330 rpm. Spectrum between 28.7 and 32.7 mm

robustness during the numerical integration. In addition, it should be noted that if one considers a quasi-zero damping, the system is always very unstable. On the other hand, with a very high damping, although there would be more energy dissipation, the ploughing model becomes a simple contact, and again the system is always very unstable. The modelling takes into account the spatial extent on the tool

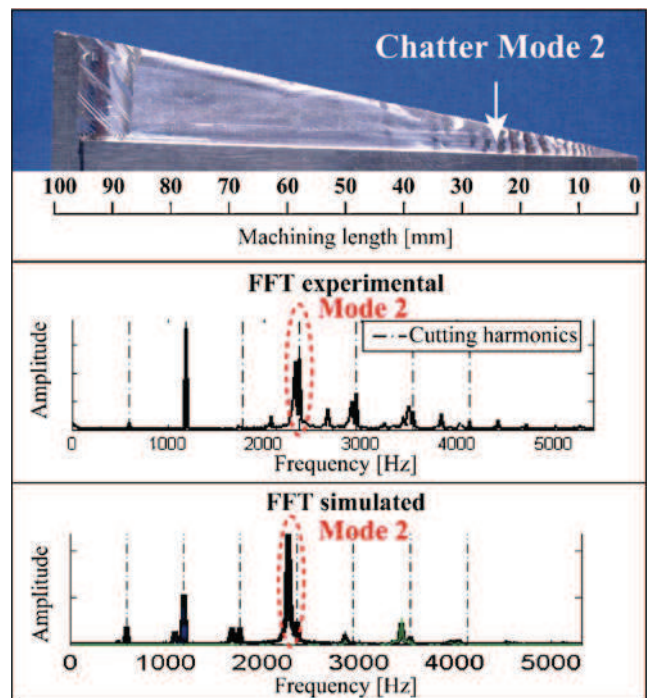


Fig. 11 Results comparison for chatter machining at 17,660 rpm. Spectrum between 9.6 and 13.6 mm

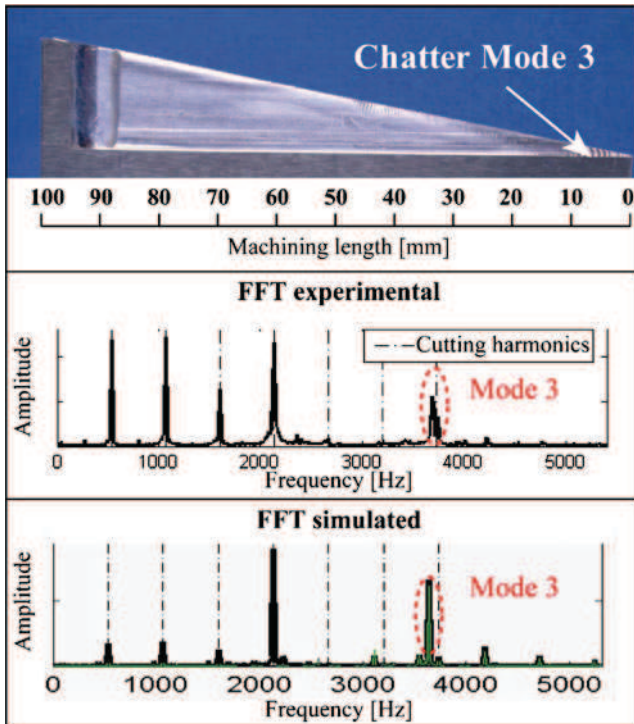


Fig. 12 Results comparison for chatter machining at 16,000 rpm. Spectrum between 9.6 and 13.6 mm

and the local intensity at each point, making a fairly complex analysis to be undertaken. To check the consistency of the model, we have tested several simplifications in order to avoid the actual extent or intensity of the damping, but with standard values (either average or maximum). We have checked the effect of many changes on the ploughing model, we cannot detail here all. We will simply give the main results of these investigations. By simplifying more or less the ploughing model, we have obtained similar results with the nominal case presented in this article. It should be noted that the use of a higher damping need a smaller discretization time step because of the interaction time of the contacts, getting closer and closer to solid contact model. Practically, it is difficult to determine the ploughing modelling that would provide the desired damping.

5 Conclusions

This paper presents a study of stability of the cutting process for the machining of thin-walled parts. A specific model of flexible workpiece was developed to simulate the machining of such pieces. The instantaneous clearance angle is taken into account all along the cutting edges in order to accurately model the ploughing effect. The variations of the dynamical parameters are computed by finite element analysis in order to take into account the removal material and the cutting edge position. This modelling allows to predict the part

dynamical properties without having excessive computing times. With this data, the dynamic modelling of milling is made by time domain simulation, using modal decomposition. This approach is novel for thin-wall machining because previous simulations were made without real machining to compare with.

The comparison between experiment and simulation show very good correlation for the cutting force prediction both on shape than on the value. The results show that simulation was able to predict realistic chatter frequency, which was very helpful for the improvement of the thin-wall milling. The milling model shows good agreement with experimental data when the vibration amplitude is low and the machining operation is chatter free. On the contrary, it is highlighted that the prediction of amplitudes in case of unstable milling is very complex. The simulation results provide only qualitative information about the modal vibrations for operations with high vibration amplitudes. This could be explained by the influence of ploughing effect. Such phenomenon is well-known to act like damping and the use of a quasi-steady-state force model to simulate machining with high vibration levels seems to be

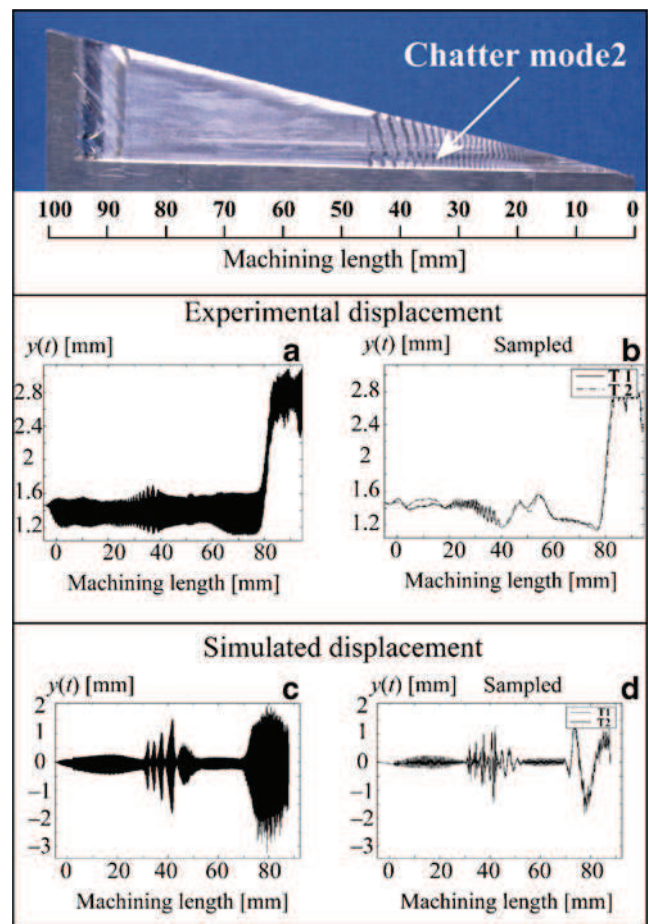


Fig. 13 Displacement comparison for chatter machining at 12,666 rpm

inadequate, whatever be tested to improve the simulation parameters considered here.

The modelling widely robust for vibration tools or more massive pieces seems to have reached its limits on this case. Therefore, the improvement in the simulation of thin-walled components machining needs development of cutting force models including contact modelization and ploughing due to the variation of the clearance angle during machining.

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