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# Experimental study of high pressure phase equilibrium of $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}\right)$ mixtures 

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#### Abstract

Experimental bubble pressure, as well as liquid density of $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}\right)$ mixtures are reported at temperatures ranging from ( 298 to 328.45 ) K. Experiments were carried out using a SITEC high-pressure variable volume cell. Transition pressures were obtained by the synthetic method and liquid density was deduced from measurement of the cell volume. Correlation of experimental results was carried out without considering chemical equilibrium of $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ system. (Liquid + vapour) equilibrium was found to be accurately modelled using the Peng-Robinson equation of state with classical quadratic mixing rules and with a binary interaction coefficient $k_{i j}$ equal to zero. Nevertheless, modelling of liquid density values was unsatisfactory with this approach.


## 1. Introduction

Supercritical carbon dioxide is now commonly recognized as a very promising compound to be used as a green solvent for chemical reactions as replacement for polluting organic solvents. This is due not only to the interesting physical properties of supercritical compounds, but also to the chemical inertness, low cost, non-toxicity of $\mathrm{CO}_{2}$ and the fact that this compound can be easily recycled. Although a weak solvent for polar interest molecules, $\mathrm{scCO}_{2}$ has been used as a solvent in a wide range of chemical reactions such as hydrogenations, hydroformylations, oxidations, or polymerizations. The use of $\mathrm{scCO}_{2}$ for chemical synthesis has been extensively reviewed by Beckman [1]. Because it is completely miscible with gases such as $\mathrm{O}_{2}$, CO , or $\mathrm{H}_{2}$, high pressure $\mathrm{CO}_{2}$ is very useful to enhance solubility of reactants into liquid phases or even to alleviate liquid-gas mass transfer limitations by solubilizing all the reactants to give a single-phase system. Moreover, carbon dioxide being the result of complete oxidation of organic compounds, it cannot be oxidized, and thus it is the ideal solvent for oxidation reactions. For this reason, $\mathrm{CO}_{2}$ has often been used as a solvent for oxidation reactions, employing mainly oxygen as the oxidant. Recently, another example of oxidation reaction in high pressure $\mathrm{CO}_{2}$, in which nitrogen dioxide is the oxidant, has been described [2] and the process of oxidation patented [3]. This involves oxidation of polysaccharides, and more

[^0]specifically cellulose, resulting in oxidized cellulose, a very attractive material for bio-medical applications. Indeed, when cellulose is partially oxidized it becomes degradable in the human body (a property termed "bioresorbability") and in addition possesses haemostatic properties (i.e. it halts bleeding), which can be advantageous in biomedical devices, like surgical compresses for instance. The suitable oxidant for preparing this material with both high carboxyl content and targeted physical properties is nitrogen dioxide $\left(\mathrm{NO}_{2}\right)$. This compound ensures selective oxidation of the primary hydroxyl groups of cellulose, leading to partially oxidized cellulose, with the already mentioned properties.

As an alternative to the present use of traditional halogenated solvents in the cellulose oxidation process [4-6], supercritical carbon dioxide $\left(\mathrm{scCO}_{2}\right)$ has been shown to be an attractive solvent to perform this oxidation [2]. Its major advantage in this case lies in its complete inertness regarding the oxidant, so, preventing a possible degradation of the solvent. Moreover, it ensures the biocompatibility of the processed material, because the latter is free from any solvent residue. Finally, because nitrogen dioxide is soluble in high pressure $\mathrm{CO}_{2}$, it allows operation with a significant concentration of this reactant in the solvent. In a previous paper [2], efficiency of the cellulose oxidation was shown to depend on operating parameters such as pressure, temperature, moisture content, and $\mathrm{CO}_{2}$ vs $\mathrm{NO}_{2}$ ratio. Moreover, in this process, the knowledge of the number of phases and their composition is also a key parameter to obtain an oxidized product with tightly specified properties and for the development of the process on an industrial scale.

In the oxidation process, the reacting mixture, composed of the oxidant $\mathrm{NO}_{2}$ and the solvent $\mathrm{CO}_{2}$, is characterized by the existence
of a chemical equilibrium between nitrogen dioxide and its dimer, nitrogen tetroxide ( $\mathrm{N}_{2} \mathrm{O}_{4}$ ), as follows:
$\mathrm{N}_{2} \mathrm{O}_{4} \leftrightarrows 2 \mathrm{NO}_{2}$.
Below $T=262.15 \mathrm{~K}$, the mixture is completely dimerised $\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$, and this dimer dissociates as temperature increases, the proportion of each compound depending on conditions of temperature and pressure, the equilibrium being governed by the mass action law, with an equilibrium constant $K$ depending only on the temperature. Under atmospheric pressure, the mixture boils at $T=294.25 \mathrm{~K}$, the liquid being yellowish brown and the vapour reddish brown. If moisture is present, the mixture decomposes readily into nitrous and nitric acid, and becomes very aggressive to numerous metals.

Physical properties of the $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ system, and values of the equilibrium constant, with respect to the temperature, have been the subject of several experimental and theoretical studies. For example, Reamer and Sage [7] have performed density measurements in the liquid-vapour coexistence region. Values of equilibrium constants in the vapour phase as a function of temperature can be found in works by Verhoek and Daniels [8] or Chao et al. [9]. These results describe a vapour phase containing mostly dissociated $\mathrm{NO}_{2}$ (around $90 \mathrm{~mol} \%$ of $\mathrm{NO}_{2}$ at $T=373.15 \mathrm{~K}$ and a complete dissociation at 413.15 K ). James and Marshall [10] have measured equilibrium constants in liquid phase and have shown that nitrogen dioxide is strongly associated in that physical state. Redmond and Wayland [11] have measured equilibrium constant data for nitrogen dioxide dissolved in some organic solvents.

Some authors studied the reaction of oxidation with $\mathrm{NO}_{2}$ of cellulose in different organic solvents [12] and showed that the degree of dissociation of $\mathrm{NO}_{2}$ increases in non-polar solvents, leading to an increase in the degree of oxidation of cellulose. So, although it is not yet clearly demonstrated, it is very probable that only the $\mathrm{NO}_{2}$ molecule, i.e., the monomer form, is the active oxidant molecule. Therefore, knowledge of the distribution between monomeric and dimeric species, especially when the oxidant $\mathrm{NO}_{2}$ is solubilized in a solvent, appears to be an important parameter of the reaction.

This work reports experimental data of high-pressure equilibrium between $\mathrm{CO}_{2}$ and $\mathrm{NO}_{2}$ in conditions close to operating conditions of the cellulose oxidation process, which have already been described in the literature [2]. As a result of a collaborative study, an attempt to model the thermodynamic behaviour of this mixture has been published by Belkadi et al. [13], who used the crossover soft-SAFT equation of state to predict (vapour + liquid) equilibrium of this mixture under pressure. The soft-SAFT equation of state is a modification of the original Statistical Associating Fluid Theory (SAFT) molecular-based equation of state, which is in nature able to describe the thermodynamic behaviour of associating compounds [14]. Belkadi et al. have shown that predictions matched correctly experimental data of the $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}\right)$ mixture provided that a binary interaction coefficient fits the experimental results. Although this kind of equation of state is a powerful tool to predict the thermodynamic behaviour of such a system, soft-SAFT equation is not implemented in most commercial thermodynamics software, and thus, from now, they cannot be easily used to compute fluid phase equilibrium of this mixture. Similarly, Bourasseau et al. [15] used the experimental results described in the present study, to show that (vapour + liquid) equilibria of the $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} /\right.$ $\mathrm{N}_{2} \mathrm{O}_{4}$ ) mixture could be predicted using a Monte-Carlo molecular simulation approach. Their interest in this mixture is justified by the necessity to predict atmospheric ( $\mathrm{CO}_{2}+$ contaminants ) mixtures. Interestingly, their simulations at $T=300 \mathrm{~K}$ predict a very low amount of non associated $\mathrm{NO}_{2}$ molecules in both phases, but they could not compare this result with experimental ones. However, Monte-Carlo simulation is not a common tool that can be routinely used to predict fluid phase equilibria.

In this paper, the experimental set-up and conditions in which (vapour + liquid) equilibria and volumetric properties of the $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}\right)$ mixture have been obtained will be described, and an attempt will be made to describe a way to predict the experimental data of this mixture using the well-known PengRobinson equation of state, in order to use this model in the specific context of the industrial application of cellulose oxidation.

## 2. Experimental

### 2.1. Materials

Liquid $\mathrm{NO}_{2}$ (water content max $0.5 \mathrm{wt} . \%$ ) and high purity $\mathrm{CO}_{2} \mathrm{TP}$ ( N 45 mass fraction purity 0.99999 ) were supplied by Air Liquide.

### 2.2. Specific hazards due to nitrogen dioxide handling

Nitrogen dioxide is a non-flammable and highly toxic gas (deadly poison). By consequence, a threshold limit value of $9 \cdot 10^{-6}$ by volume, i.e., $9 \mathrm{mg} \cdot \mathrm{m}^{-3}$, is recommended as the maximum concentration allowable in industrial premises [16]. For the purpose of this study, operators are protected thanks to a polypropylene transparent barrier guard placed around the experimental set-up, and an efficient ventilation of the whole set-up is ensured. Individual protection equipments are used too.

Before starting experiments, the entire installation must be carefully dried in order to remove moisture, as any trace of water would lead to $\mathrm{HNO}_{3}$ formation and therefore metal corrosion. Moreover, every gasket of the installation must be made of Teflon ${ }^{\circledR}$ because $\mathrm{NO}_{2}$ tends to soften most polymeric matter.

It should be pointed out here that in spite of corrosion protections, the experimental campaign has unfortunately been prematurely interrupted because of frequent $\mathrm{NO}_{2}$ leaks occurring in pump or tubing of the system. These technical problems explain the limited number of experimental points that have been obtained.

### 2.3. High-pressure equipment

The experimental set-up is a SITEC (SITEC-Sieber Engineering AG, Switzerland) high pressure phase equilibrium apparatus. The complete set-up is presented in figure 1 . This high-pressure unit allows detection and measurement of phase equilibrium and phase transitions by optical and analytical means. It is composed of a variable volume view cell (from $46.1 \mathrm{~cm}^{3}$ to $60.2 \mathrm{~cm}^{3}$ ) equipped with sapphire windows, a magnetic stirrer and a circulation pump for a better homogenization of the system. Sampling of gaseous and liquid phases can be taken from the top and the bottom of the cell, in which case the directly connected counterbalance piston operates to keep the pressure in the cell constant. The temperature of the cell is maintained by a thermostated bath. Measurement of temperature is taken by a thermocouple (J type, precision $\pm 0.1 \mathrm{~K}$ ) placed in the centre of the cell. Phase transitions can be directly observed through sapphire windows, or filmed and transmitted by a connected camera, and displayed on a video screen.

Pressure inside the cell is measured by a pressure sensor (Keller) with accuracy of $\pm 0.075 \mathrm{MPa}$.

Data of the process throughout (pressure, temperature, position of the piston) are recorded on a computer.

Both fluids $\left(\mathrm{CO}_{2}\right.$ and $\left.\mathrm{N}_{2} \mathrm{O}_{4} / \mathrm{NO}_{2}\right)$ are stored inside bottles at their (liquid + vapour) equilibrium at ambient temperature. So, the pressure of $\mathrm{CO}_{2}$ inside the bottle is around (5 to 6) MPa , while pressure inside the $\mathrm{NO}_{2}$ bottle is around 0.1 MPa . A correlation from DIPPR ${ }^{\circledR}$ database giving the $\mathrm{NO}_{2}$ vapour pressure is presented in figure 2.


FIGURE 1. High-pressure phase equilibrium equipment (CA: compressed air; CG: cooling group).


FIGURE 2. Vapour pressure of $\mathrm{NO}_{2}$ as a function of temperature $\left(\operatorname{Ln} P=42.779-4431.7 / T-2.997 \operatorname{Ln} T+9.7289 \mathrm{e}^{-6} \cdot T^{2}, T=[261.9-431.15] \mathrm{K}, P\right.$ in $\mathrm{MPa})$.

Carbon dioxide is introduced into the cell by action of a high pressure manual piston pump. This pump is cooled by a circulation of cold water in an external jacket, and pressure inside the pump is measured with a manometer. The amount of $\mathrm{CO}_{2}$ that is introduced into the equilibrium cell is calculated through measurement of the difference between the volume of liquid $\mathrm{CO}_{2}$ inside the manual pump, before and after its introduction.

Because of the very high toxicity of $\mathrm{NO}_{2}$, introduction of this compound into the equilibrium cell cannot be made as usually, i.e. by deposing the liquid or the solid in the open cell before closing and introducing of $\mathrm{CO}_{2}$. Rather, the procedure of introduction of this compound is similar to that of $\mathrm{CO}_{2}$, i.e. $\mathrm{NO}_{2}$ is injected into the $\mathrm{CO}_{2}$ pressurized cell, using a thermostated ISCO pump (Teledyne, model 260D).

### 2.4. Experimental procedure

Before starting an experiment, the whole system is flushed with gaseous $\mathrm{CO}_{2}$ in order to remove any trace of water in the system. Then, the desired amount of carbon dioxide is introduced into
the cell with the $\mathrm{CO}_{2}$ manual pump. The manual pump is first filled with liquid $\mathrm{CO}_{2}$ and the temperature and pressure of the system are allowed to establish themselves. Introduction of $\mathrm{CO}_{2}$ is made by opening valve V2. The volume of the manual pump is then adjusted in order to reach previous conditions of pressure and temperature of $\mathrm{CO}_{2}$ (i.e. initial conditions before introduction). The difference in volumes inside the manual pump allows calculation of the mass of $\mathrm{CO}_{2}$ introduced into the cell, with knowledge of the density of liquid $\mathrm{CO}_{2}$ at temperature and pressure of the manual pump.

The procedure of introducing the $\mathrm{NO}_{2}$ is similar to the $\mathrm{CO}_{2}$ one, i.e. amount of $\mathrm{NO}_{2}$ introduced into the cell is known by measurement of volume of $\mathrm{NO}_{2}$ introduced, directly given by ISCO pump. The corresponding mass of $\mathrm{NO}_{2}$ introduced into the cell is deduced through calculation (see section 3.1) of the density of $\mathrm{NO}_{2}$ at temperature and pressure of ISCO pump.

Amounts of $\mathrm{CO}_{2}$ and $\mathrm{NO}_{2}$ introduced into the equilibrium cell are estimated and then chosen in order that a phase transition can be observed, when moving the piston inside the cell before reaching its maximum range. After introduction, the cell is pressurized with the piston in such a way that the mixture becomes a single phase one. The system is maintained in that position for several hours, until no change in temperature or pressure is observed. After this equilibration time, the cell is very carefully depressurized by retracting the piston. Special care is necessary in order to maintain a constant temperature inside the cell during this depressurization step. This point is very delicate because depressurization of the mixture induces sharp changes in temperature of the system. So, the depressurization is slowly operated until phase transition is observed. Temperature, pressure and piston position are recorded by computer during the operation. Pressurizationdepressurization steps are repeated twice in order to check repeatability of the method.

When phase transition from a single phase to a two-phase system occurs, a sharp change in the moving speed of the piston is observed. Indeed, at equilibrium pressure, where a liquid and a vapour phases are present, the piston rises completely, changing vaporization ratio of the system without any pressure change. This


FIGURE 3. Example of pressure and piston position recording along an experiment.
appears very clearly when pressure and piston position are recorded as can be seen for example in figure 3. From this recording, the volume of the liquid phase at the pressure transition can be calculated and thus, knowing the amounts of introduced $\mathrm{CO}_{2}$ and $\mathrm{NO}_{2}$, density of the liquid phase can be calculated.

## 3. Results

### 3.1. Evaluation of measurement uncertainties

The experimental set-up previously described allows determination of transition pressure, i.e. bubble or dew pressure, for a fixed composition and temperature of the mixture. This is a very specific system and it has been found useful to assess the composition, pressure and temperature uncertainties associated with such experimental devices.

Measurements are taken after isothermal conditions have been reached, temperature being measured by a thermocouple whose accuracy is $\pm 0.1 \mathrm{~K}$.

In a first approach, evaluation of the uncertainty of the transition pressure measurements appears rather difficult because estimation of the phase transition point is partly subjective, its occurrence being visually decided by the operator. This drawback is nevertheless counterbalanced by the use of the recorded curves of the change in pressure, temperature, and position of the piston of the cell throughout the experiment. Indeed, phase transition corresponds to a sharp change in compressibility, and thus, around this boundary region the change in pressure presents a stiffness (figure 3). With this procedure, the phase transition pressure from a one-phase to a two phase mixture can objectively be determined and the pressure uncertainty can be directly related to the precision of the pressure sensor, i.e. $\pm 0.075 \mathrm{MPa}$ in the case of this study.

Uncertainty of the mixture mass fraction can be calculated from conventional error calculation, starting from the expression of the mass fraction of one of the two compounds:
$x_{1}=\frac{V_{1} \cdot \rho_{1}}{V_{1} \cdot \rho_{1}+V_{2} \cdot \rho_{2}}$,
$V_{i}$ and $\rho_{i}$ being respectively the volume and density of the compound $i$.

The absolute deviation of $x_{1}$ has been deduced by the differentiation of the expression (1).

The piston displacement of the manual syringe pump containing the liquid $\mathrm{CO}_{2}$ gives the liquid $\mathrm{CO}_{2}$ volume introduced into the measurement cell. The accuracy of this measurement is $\pm 1 \mathrm{~cm}^{3}$. Volume of $\mathrm{NO}_{2}$ introduced is directly obtained from the ISCO pump with a precision of $\pm 1 \cdot 10^{-3} \mathrm{~cm}^{3}$.

Liquid $\mathrm{CO}_{2}$ density is calculated using the Lee, Kesler and Plöcker (LKP) equation of state [17], giving a very satisfying correspondence with the experimental density values from Ely et al. [18] over a wide range of temperature and pressure, as shown in figure 4.

The LKP calculations are performed using Simulis ${ }^{\circledR}$ Thermodynamics, a commercial thermophysical properties server - PROSIM S.A. (France). It allows thermodynamic properties and equilibrium calculations for pure component and mixture fluid phase. Density estimation was obtained with mean error of $\pm 6.2 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$, when compared to the experimental results of Ely et al., who estimated the uncertainty of their measured densities to be equal to $0.02 \%$.

In a similar way, $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ liquid density uncertainty has been estimated by comparing calculations with experimental data from the literature [7]. These experimental results give the temperature dependence of the density of the saturated liquid of the $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ system. The Rackett's equation [19] has been used to estimate the liquid density of $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$, using Simulis ${ }^{\circledR}$ Thermodynamics. This model used with the DIPPR ${ }^{\circledR}$ data for $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ fits the experimental values, as shown in figure 5. Mean error of $\mathrm{NO}_{2}$ density prediction $\left(\Delta \rho_{\mathrm{NO}_{2}}\right)$ is equal to $\pm 8.5 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$.

In the same way, uncertainties of mixture liquid density measurements have been evaluated. Density of the liquid mixture is calculated by measuring position of the piston of the equilibrium cell when phase transition occurs (equation (2)). Thus, it is obtained by dividing total mass of the mixture ( $m_{m i x}$ ) introduced into the cell by the volume of the liquid phase $\left(V_{L}\right)$, this latter being calculated with the minimum volume of the cell (bottom position of


FIGURE 4. Comparison of experimental [16] and LKP calculated values of $\mathrm{CO}_{2}$ density (mean error $6.2 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$ ).


FIGURE 5. Temperature dependence of liquid density of $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ system at (vapour + liquid) equilibrium. Comparison of experimental [7] and calculated values with the Rackett's equation (mean error $8.5 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$ ).

TABLE 1
Evaluated uncertainties.

| Measured parameter | Evaluated uncertainty |
| :--- | :--- |
| $T / \mathrm{K}$ | 0.1 |
| $P / \mathrm{MPa}$ | 0.075 |
| $\Delta V_{\mathrm{CO}_{2}} / \mathrm{cm}^{3}$ | 1 |
| $\Delta V_{\mathrm{NO}_{2}} / \mathrm{cm}^{3}$ | $1 \cdot 10^{-3}$ |
| $\Delta \rho_{\mathrm{CO}_{2}} / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | 6.2 |
| $\Delta \rho_{\mathrm{NO}_{2}} / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | 8.5 |
| $\Delta V_{0} / \mathrm{cm}^{3}$ | 0.5 |
| $\Delta h_{\text {piston }} / \mathrm{mm}$ | 0.1 |

the piston) ( $V_{0}$ ) and with the measured position of the piston at phase transition ( $h_{\text {piston }}$ )
$\rho_{L}^{\text {mix }}=\frac{m^{\text {mix }}}{V_{L}}=\frac{m_{\mathrm{CO}_{2}}+m_{\mathrm{NO}_{2}}}{V_{0}+\pi \cdot \frac{d_{\text {piston }}^{2}}{4} \cdot h_{\text {piston }}}=\frac{V_{\mathrm{CO}_{2}} \cdot \rho_{\mathrm{CO}_{2}}+V_{\mathrm{NO}_{2}} \cdot \rho_{\mathrm{NO}_{2}}}{V_{0}+\pi \cdot \frac{d_{\text {piston }}^{2}}{4} \cdot h_{\text {piston }}}$.
The $V_{\mathrm{CO}_{2}}$ and $V_{\mathrm{NO}_{2}}$ are the volumes of liquid $\mathrm{CO}_{2}$ and $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ introduced into the cell and $\rho_{\mathrm{CO}_{2}}$ and $\rho_{\mathrm{NO}_{2}}$ are their densities calculated at the temperature and pressure of each pump.

Again, the absolute deviation in the liquid phase density has been deduced by the differentiation of the expression (2).

Measurements uncertainties $\Delta V_{\mathrm{CO}_{2}}, \Delta V_{\mathrm{NO}_{2}}, \Delta \rho_{\mathrm{CO}_{2}}$, and $\Delta \rho_{\mathrm{NO}_{2}}$ have been evaluated as described above. Volume of the cell $V_{0}$ has been measured to an accuracy of $\pm 0.5 \mathrm{~cm}^{3}$ and the piston position is measured to an accuracy of $\pm 0.1 \mathrm{~mm}$.

Finally, measurements uncertainties are presented in table 1.

### 3.2. Experimental $\mathrm{P}-x$ data and liquid densities of $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}\right)$ mixture at high pressure

The experimental set-up described in the previous section does not allow measuring the degree of dissociation of $\mathrm{N}_{2} \mathrm{O}_{4}$ inside the equilibrium cell, only the overall mass of $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ mixture introduced into the cell is measured. So, it has been decided initially to appoint the $\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}$ mixture as an apparent pure $\mathrm{NO}_{2}$ compound (termed "appNO ${ }_{2}$ " in this work). The ternary $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2}+\mathrm{N}_{2} \mathrm{O}_{4}\right)$ system is thus fictively considered as a binary $\left(\mathrm{CO}_{2}+\mathrm{appNO}_{2}\right)$ system.

Although the equilibrium cell is supposed to allow dew-points measurements (transitions from one vapour phase to a two phase system), this type of experiment is actually very tricky because the
formation of the first liquid droplet is really difficult to observe in the cell. As a consequence, in this work, experimental data mainly concern bubble pressures.

Experimental results and their related measurement uncertainties are presented in table 2.

As explained earlier, for safety reasons, the number of experiments has been quite low. However, the findings are sufficient to yield a good estimation of behaviour of the mixture, at temperature corresponding to operating conditions of cellulose oxidation conditions.

## 4. Modelling and discussion

The $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ form a reacting binary system with only one degree of freedom at (liquid + vapour) equilibrium. That is why in the ( $P, T, x$ ) coordinates, the two-phase region of this reacting system is a curve which ends at the critical point of these molecules. Thus, the critical coordinates $T_{c}, P_{c}$ and the acentric factor $\omega$ are the same for $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$. The fugacities calculated with a cubic equation of state are the same for $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ too. To calculate the equilibrium of such a ternary system, the only equation where $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ are distinguishable is the chemical equilibrium between $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$, where the standard Gibbs free energies and enthalpies of formation get involved. In a first approach, the case of the hypothetical binary $\left.\left(\mathrm{CO}_{2}+\mathrm{appNO}\right)_{2}\right)$ mixture without considering $\mathrm{NO}_{2}-\mathrm{N}_{2} \mathrm{O}_{4}$ chemical equilibrium was considered. Calculations of fluid-phase equilibrium of this pseudo-binary mixture, obtained from a conventional equation of state have been compared to experimental results. Calculations have been performed with Simulis ${ }^{\circledR}$ Thermodynamics. Because $\left(\mathrm{CO}_{2}+\mathrm{appNO}_{2}\right)$ mixture involves apolar compounds, the well-known Peng-Robinson (PR) cubic equation of state [20] was chosen to describe the thermodynamic behaviour of the mixture.

In the case of a mixture, parameters $a, \alpha$ and $b$ of PR equation of state are calculated using a mixing rule, involving the attraction term $a_{i}$, the co-volume $b_{i}$, and $\alpha_{i}$ parameters of pure components. Standard van der Waals mixing rules involving mixture composition $z_{i}$, with one binary interaction coefficient for parameter $a$, have been chosen here in this work. Critical parameters and acentric factor of pure compounds necessary for calculations are gathered in table 3.

Conventional mixing rules bring into play one binary interaction parameter $k_{i j}$, to take account of the specific interactions exist-

TABLE 2
Transition pressures $(P)$ and liquid density measurements of different $\left(\mathrm{CO}_{2}+\mathrm{appNO} \mathrm{O}_{2}\right)$ mixtures at different temperatures. Compositions are expressed in mass fractions.

| T/K | $\chi_{\mathrm{CO}_{2}}$ | $\chi_{\text {appNO }_{2}}$ | P/MPa | $\Delta x_{\mathrm{CO}_{2}}$ | Type | $\rho_{L} / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\Delta \rho L / \rho_{L} \cdot 100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 298.15 | 0.072 | 0.928 | 1.000 | 0.014 | Bubble | n.m ${ }^{a}$ |  |
| 313.65 | 0.281 | 0.719 | 3.300 | 0.013 | Bubble | 1338.3 | 3.20 |
| 312.95 | 0.323 | 0.678 | 3.800 | 0.012 | Bubble | 1255.9 | 2.99 |
| 313.05 | 0.355 | 0.645 | 4.200 | 0.011 | Bubble | 1195.4 | 2.83 |
| 313.05 | 0.937 | 0.063 | 8.000 | 0.003 | Bubble | 551.1 | 5.44 |
| 313.35 | 0.778 | 0.222 | 6.620 | 0.006 | Bubble | 1152.9 | 3.47 |
| 313.35 | 0.784 | 0.216 | 6.690 | 0.006 | Bubble | 1229.9 | 3.47 |
| 313.55 | 0.788 | 0.212 | 6.770 | 0.006 | Bubble | 1171.1 | 3.37 |
| 313.35 | 0.546 | 0.455 | 5.550 | 0.011 | Bubble | 1172.6 | 3.58 |
| 313.35 | 0.571 | 0.430 | 5.500 | 0.010 | Bubble | 1196.8 | 3.45 |
| 313.35 | 0.586 | 0.414 | 5.520 | 0.010 | Bubble | 1158.0 | 3.32 |
| 313.25 | 0.606 | 0.394 | 5.600 | 0.009 | Bubble | 1144.0 | 3.17 |
| 313.15 | 0.136 | 0.864 | 2.100 | 0.014 | Bubble | 1384.4 | 3.13 |
| 313.65 | 0.160 | 0.840 | 2.560 | 0.013 | Bubble | 1329.2 | 3.02 |
| 312.35 | 0.884 | 0.116 | 5.500 | 0.010 | Dew | n.m. |  |
| 328.45 | 0.839 | 0.161 | 8.970 | 0.007 | Bubble | 950.7 | 3.29 |
| 328.45 | 0.847 | 0.153 | 8.950 | 0.007 | Bubble | 873.8 | 3.10 |
| 328.45 | 0.707 | 0.293 | 7.810 | 0.010 | Bubble | n.m. |  |

[^1]TABLE 3
Parameters of pure compounds (from DiPPr database).

|  | $T_{c} / \mathrm{K}$ | $P_{c} / \mathrm{MPa}$ | $\omega$ |
| :--- | :--- | ---: | :--- |
| $\mathrm{CO}_{2}$ | 304.15 | 7.37600 | 0.231 |
| $\mathrm{NO}_{2}$ | 431.15 | 10.13252 | 0.851088 |
| $\mathrm{~N}_{2} \mathrm{O}_{4}$ | 431.15 | 10.13252 | 0.851088 |

ing between components in the mixture. This parameter is usually obtained by matching experimental data with the equation of state.

In the case of $\left.\left(\mathrm{CO}_{2}+\mathrm{appNO}\right)_{2}\right)$ mixture, it can be seen from figure 6 that PR EoS predict reliable values of bubble pressure even using $k_{i j}=0$. Experimental results are plotted with experimental errors given in table 1 . These values of $k_{i j}=0$ mean that no specific interactions between $\mathrm{CO}_{2}$ and $\mathrm{appNO}_{2}$ exist in fluid phases.

In the same way, volumetric behaviour of the saturated liquid phase (at bubble point) of the $\left(\mathrm{CO}_{2}+\mathrm{appNO} \mathrm{O}_{2}\right)$ mixture has been evaluated using the PR EoS. Although it is well known that cubic equations of state derived from van der Waals theory are not very suitable to calculate liquid molar volumes, PR EoS is considered to give a better restitution of this property. Liquid density has been also evaluated with the LKP equation of state. For both calculations,


FIGURE 6. Comparison of experimental and calculated $(P, x, y)$ data for the $\left.\left(\mathrm{CO}_{2}+\mathrm{appNO}\right)_{2}\right)$ system.


FIGURE 7. Experimental $\left({ }^{\circ}\right)$ and calculated with PR EoS $(\times)$ and LKP EoS saturated liquid density for the $\left(\mathrm{CO}_{2}+\mathrm{appNO}_{2}\right)$ system at temperatures between 312.95 K and 313.65 K .
liquid density is calculated at experimental temperature, bubble pressure and mass composition of the $\left(\mathrm{CO}_{2}+\mathrm{appNO}_{2}\right)$ mixtures.

Experimental and calculated results are given in table 4. For a clearer visualization of the results, experimental and calculated densities at temperature around 313.15 K are presented in figure 7.

From figure 7, a sharp discrepancy between experimental and calculated results for mixtures such that $x_{\mathrm{CO}_{2}}$ is around 0.8 is observed, whatever the model. From table 4, this can also be observed for high temperature measurements. Results for $x_{\mathrm{CO}_{2}} \approx 0.8$ are quite surprising when compared to others, so an experimental artefact may be suspected for these results. Overall, our experimental results are roughly predicted by these EOS, PR EOS giving slightly better results but the precision remains poor.

However, it is not surprising that the volumetric behaviour of the liquid phase cannot be well predicted without taking into account the equilibrium between $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ inside the mixture. Indeed, density of the mixture is highly dependent on the real composition of the mixture, i.e. proportion of $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ in the presence of $\mathrm{CO}_{2}$. Moreover, our results do not enable us to deduce proportion of each compound by fitting experimental results with PR EoS since the parameters of pure compounds involved in the EoS are the same for $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}\left(T_{c}, P_{c}\right.$, and $\left.\omega\right)$.

TABLE 4
Experimental and calculated liquid density of different $\left(\mathrm{CO}_{2}+a p p \mathrm{NO}_{2}\right)$ mixtures at different temperatures. Compositions are expressed in mass fractions.

| Experimental results |  |  |  |  | PR calculations |  | LKP calculations |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| T/K | $x_{\mathrm{CO}_{2}}$ | $\chi_{\text {appNO }}^{2}$ | $P_{b} / \mathrm{MPa}$ | $\rho_{L} /\left(\mathrm{kg} \cdot \mathrm{m}^{-3}\right)$ | $\rho_{L} /\left(\mathrm{kg} \cdot \mathrm{m}^{-3}\right)$ | Relative deviation/\% | $\rho_{L} /\left(\mathrm{kg} \cdot \mathrm{m}^{-3}\right)$ | Relative deviation/\% |
| 298.15 | 0.072 | 0.928 | 1.000 | n.m. | 1350.99 | n.c. ${ }^{\text {a }}$ | 1636.07 | n.c. |
| 313.65 | 0.281 | 0.719 | 3.300 | 1338.3 | 1239.65 | 7.96 | 1371.56 | 2.43 |
| 312.95 | 0.323 | 0.678 | 3.800 | 1255.9 | 1217.67 | 3.14 | 1318.42 | 4.74 |
| 313.05 | 0.355 | 0.645 | 4.200 | 1195.4 | 1202.88 | 0.63 | 1287.44 | 7.15 |
| 313.05 | 0.937 | 0.063 | 8.000 | 551.1 | 616.21 | 10.56 | 616.21 | 10.56 |
| 313.35 | 0.778 | 0.222 | 6.620 | 1152.9 | 893.95 | 28.97 | 890.88 | 29.41 |
| 313.35 | 0.784 | 0.216 | 6.690 | 1229.9 | 886.93 | 38.66 | 884.27 | 39.08 |
| 313.55 | 0.788 | 0.212 | 6.770 | 1171.1 | 880.79 | 32.96 | 878.42 | 33.32 |
| 313.35 | 0.546 | 0.455 | 5.550 | 1172.6 | 1098.06 | 6.79 | 1115.04 | 5.16 |
| 313.35 | 0.571 | 0.430 | 5.500 | 1196.8 | 1080.42 | 10.77 | 1092.06 | 9.59 |
| 313.35 | 0.586 | 0.414 | 5.520 | 1158.0 | 1068.99 | 8.33 | 1077.60 | 7.46 |
| 313.25 | 0.606 | 0.394 | 5.600 | 1144.0 | 1055.39 | 8.40 | 1060.62 | 7.86 |
| 313.15 | 0.136 | 0.864 | 2.100 | 1384.4 | 1288.75 | 7.42 | 1504.47 | 7.98 |
| 313.65 | 0.160 | 0.840 | 2.560 | 1329.2 | 1279.25 | 3.90 | 1477.01 | 10.01 |
| 328.45 | 0.884 | 0.116 | 8.970 | 950.7 | 651.77 | 45.87 | 651.77 | 45.87 |
| 328.45 | 0.839 | 0.161 | 8.950 | 873.8 | 648.69 | 34.70 | 458.18 | 90.71 |
| 328.45 | 0.847 | 0.153 | 7.810 | n.m. | 875.15 | n.c. | 867.50 | n.c. |

[^2]
## 5. Conclusions

This work has provided experimental data about the high pressure $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}\right)$ phase equilibria. Although this first approach for modelling the liquid-vapour experimental study did not allow a complete description of the actual behaviour of the system, i.e., the dissociation degree of $\mathrm{N}_{2} \mathrm{O}_{4}$ was not measured and modelled, the modelling, using a simple Peng-Robinson equation of state with $k_{i j}=0$ was shown, nevertheless, to be very suitable for predicting the physical state of the $\left(\mathrm{CO}_{2}+\mathrm{NO}_{2} / \mathrm{N}_{2} \mathrm{O}_{4}\right)$ mixture, within the given range of pressure and temperature which is of interest for the targeted process of oxidation of cellulose. Therefore, it achieves one of its objectives, i.e., providing a simple tool to predict the phase diagram in the reactor and to determine the maximum amount of $\mathrm{NO}_{2}$ which can be dissolved in $\mathrm{CO}_{2}$ as the solvent to a maintain a single-phase oxidant fluid medium in the so-lid-fluid reactor. Having this knowledge is essential for the future development of the new process of oxidation of cellulose.
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[^1]:    ${ }^{a}$ Not measured.

[^2]:    ${ }^{a}$ Not calculated.

