

## Closed loop analysis of a triangular wave generator

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In this paper an analysis has been given of a closed loop system having an integrator, an On-Off element with hysteresis and a multiplier. It has been shown that the output of the integrator will be a train of triangular waves. Practical implementation of such a system using integrated circuits has been given.

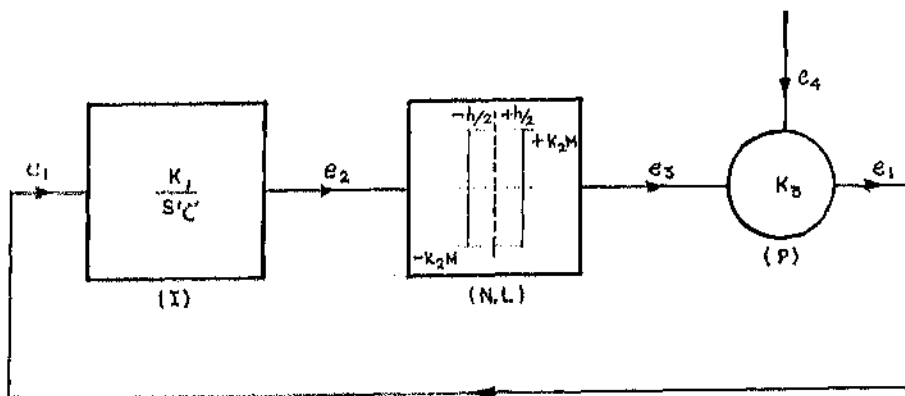
### 1. Introduction

Applications requiring a triangular wave generator that gives a symmetrical output, and the frequency of which can be varied over a wide range by an external input voltage, are many-fold. The theoretical basis for the design of such a system has been presented here, based on the closed loop analysis. A scheme for practical implementation that uses integrated circuit blocks, is also provided. The circuit described by Klein and Hagenbeuk (1907) for this purpose, however, uses only discrete components.

### 2. Analysis

In figure 1 is shown the schematic block diagram of the closed loop, that has an integrator (I), a non-linear element (N.L.), an On-Off element with

Fig. 1



Schematic of the closed loop.

hysteresis, and a multiplier (P). Much element has the respective transfer functions shown inside each box.  $e_1$ ,  $e_2$ ,  $e_3$  and  $e_4$  are as follows :

- $e_1$  = fed back voltage/output voltage of the multiplier,
- $e_2$  = output voltage of the integrator,
- $e_3$  = output voltage of the On-Off element,
- $e_4$  = external voltage input to the multiplier.

Now

$$e_1 = \pm K_2 M K_3 e_4, \quad (1)$$

$\pm$  sign indicates : for  $e_1 = \pm h/2$  switching takes place,

and

$$e_2 = \frac{K_1}{ST} e_1 \quad (2)$$

or

$$\frac{de_2}{dt} = \pm \frac{K_1 K_2 K_3 M e_4}{\tau}$$

or

$$e_2 = \pm \frac{K_1 K_2 K_3 M e_4}{\tau} t + C,$$

where  $C$  is a constant of integration.

At time

$$t = 0 ; e_2 = 0 ;$$

$$\therefore C = 0,$$

and calling

$$\frac{K_1 K_2 K_3 M e_4}{\tau} = \lambda ; \quad (3)$$

$$\therefore e_2 = \pm \lambda t. \quad (4)$$

### 3. Discussion

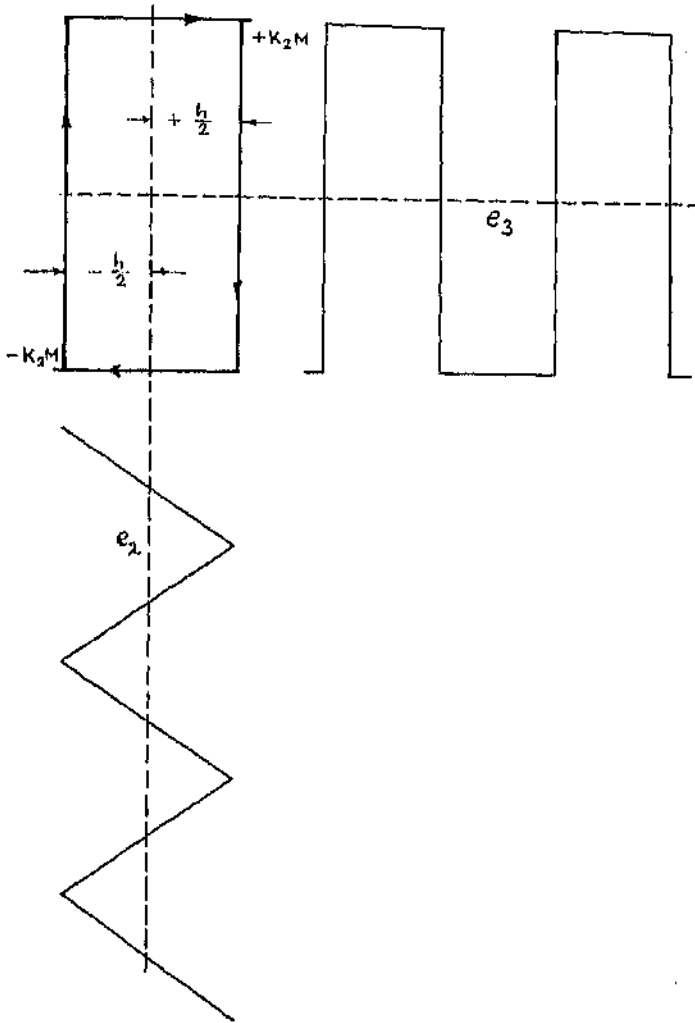
Figure 2 shows the process of switching. The output of the integrator is a ramp function. No switching takes place, until the value of  $e_2$  reaches  $+h/2$ . When  $e_2 > +h/2$ , switching takes place. When switching has occurred the slope of  $e_2$  changes from  $+\lambda$  to  $-\lambda$  and the next switching takes place only when  $e_2 = -h/2$ . The time  $T$  taken to complete one cycle is, therefore, the time taken for  $e_2$  to change from  $e_2 = +h/2$  to  $e_2 = -h/2$  and back to  $e_2 = +h/2$ , i.e. through  $h$ . Since  $\lambda$  is the slope,

$$T = \frac{2h}{\lambda}. \quad (5)$$

Thus the frequency of the generated triangular waves is

$$f = \frac{\lambda}{2h}. \quad (6)$$

Fig. 2

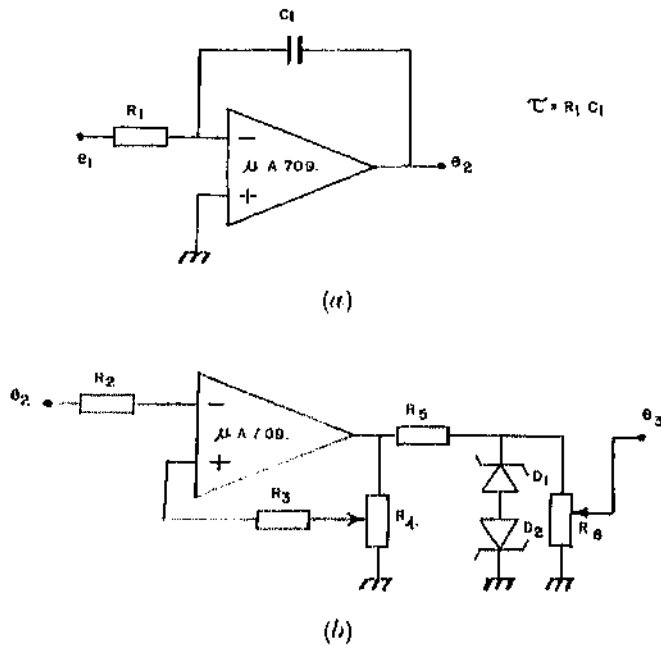


Hence, by varying  $A$  or  $h$ , it is possible to vary the frequency of the generated triangular waves. For a given value of  $T$ ,  $K_1$  and  $K_3e_4$ , either by setting the value of  $K_2M$  by the use of a potentiometer at the output of the On-Off element, or by setting the value of  $h$ , it is possible to make the system oscillate at the required frequency. And now, if  $e_4$  is varied,  $f$  changes linearly. Thus the system can be used as a linear voltage controlled oscillator. In addition to  $Mm$  triangular waves, the output of the On-Off element is a train of square waves. It is also possible to produce sine waves by properly shaping the triangular waves with diodes.

#### 4. Conclusions

It is not difficult to realize these elements electronically by using operational amplifiers. Figure 3 shows the operational integrator and the On-Off element.  $P$  can be an integrated chip multiplier.  $M$  is maintained constant by the

Fig. 3



(a) Integrator, (b) On-Off element.

two of zener diodes at the output of the On-Off element.  $K_2$  denotes the function of the potentiometer across these zener diodes.  $K_3$  is the constant of the multiplier.

In this paper only the basic theoretical aspects of a triangular wave generator based on the closed loop analysis has been given. However, practical implementation of this scheme using operational amplifiers as circuit blocks is not difficult.

#### ACKNOWLEDGMENT

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#### REFERENCE

- KLEIN, G., and HAGENBUCK, H., 1967, *Elect. Engng.*, **39**, 388.