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## LIST OF SYMBOLS

$K$	-	shape parameter
$r$	-	correlation
$s_{xx}^2$	-	sample variance for observed flows
$s_{zz}^2$	-	sample variance for predicted flows
$s_{xz}^2$	-	sample covariance
$x_i$	-	observed flows
$z_i$	-	predicted flows
$\alpha$	-	scale parameter
$\mu$	-	mean of the $x$ series
$\sigma$	-	standard deviation of the $x$ series
$\xi$	-	location parameter
$\tau_3$	-	L-moment skewness
$\tau_4$	-	L-moment kurtosis
$\tau_3^1$	-	TL-moment skewness with $t = 1$
$\tau_4^1$	-	TL-moment kurtosis with $t = 1$
$\tau_3^2$	-	TL-moment skewness with $t = 2$
$\tau_4^2$	-	TL-moment kurtosis with $t = 2$
$\Phi$	-	standard normal distribution function
$\Phi^{-1}(F)$	-	the inverse of standard normal distribution function

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