



# EFFICIENT 3D TEMPERATURE PROPAGATION FOR LASER GLASS INTERACTION

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## ABSTRACT

A new algorithm in the class of the AGE method is for developed to solve the heat equation in 3 space dimensions laser glass model problem. AGE method is one of the iterative, convergent, stable and second order accurate with respect to space and time. All the parallel strategies were developed on a CPUs. The distributed parallel computer system were run on the homogeneous cluster of 20 Intel Pentium IV PCs, each with a storage of 20GB and speed of 1.6Mhz. where data decomposition is run asynchronously and concurrently at every time level. The performance evaluations of the algorithm are increasing in terms of speed-up, efficiency and effectiveness.

## INTRODUCTION

This research are to present the coordinate system cylinder parabolic equation with the laser glass interaction model problem and also to described its parallel implementation on the PVM platform is used.

## OBJECTIVES

- i. To derive the mathematical modelling of polar coordinate of parabolic equation.
- ii. To discretize of the laser glass using partial differential equation (PDE)
- ii. To compare the numerical performance of the Alternative Group Explicit method (AGE) with DOUGLAS, GSRB and BRIAN.

## METHODOLOGY

Using Alternative Group Explicit method (AGE), such as AGE-BRIAN, AGE-DR, and AGE-GSRB.

## NUMERICAL METHODS

The mathematical simulation of the problem statements lead to solving partial differential equation of the parabolic type. In the special case of temperature propagation in an isotropic and homogeneous medium in the 3-dimensional space of cylindrical coordinate of parabolic type and discretize by Taylor, this equation is (Smith, 1978):

$$\frac{1}{a} \frac{\partial U}{\partial t} = \frac{\partial^2 U}{\partial r^2} + \frac{1}{r} \frac{\partial^2 U}{\partial r} + \frac{1}{r^2} \frac{\partial^2 U}{\partial \theta^2} + \frac{\partial^2 U}{\partial z^2} + \frac{q}{k'}$$

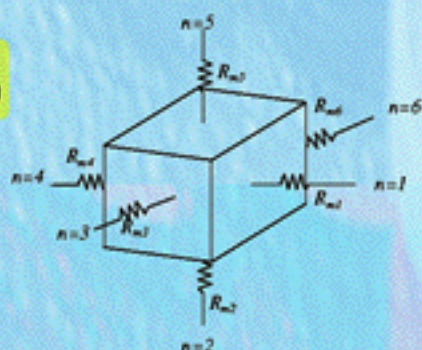
with the initial condition:

$$T(r, \theta, z, t) |_{t=0} = T_0$$

and boundary condition:

$$T(r, \theta, z, t) |_{s_1=0} = T_1$$

$$T(r, \theta, z, t) |_{s_2=0} = T_2$$



## CONCLUSION

The stable and highly accurate AGEB algorithm is found to be well suited for parallel implementation where the data decomposition runs asynchronously and concurrently at every time level.

AGE\_Brian scheme on system coordinate cylinder on laser glass interaction using heat equation proof that this scheme have a convergence value better than AGE\_Douglas and GSRB. Comparison the result shows that when the size of dimension is increase, speed-up and efficient of AGE will decrease. The factors are communication cost between processors increase, time idle increase and the level equilibrium of data storage decrease. AGE\_Brian proof as a theoretically and experimentally that is

## VISUALIZATION OF LASER GLASS

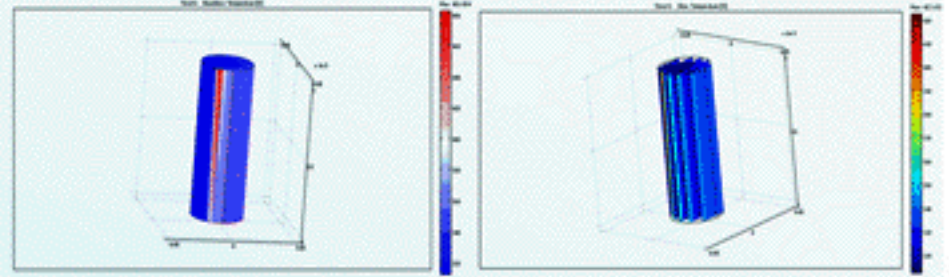


Figure 1: Temperature distribution after 1s of laser heating on the piece of glass



Example of Laser Glass Products

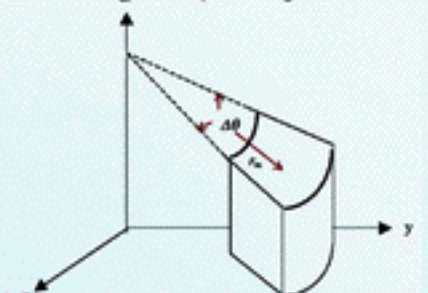


Figure 2: Cylinder with prescribed angle and radius

## EXPERIMENTAL RESULTS

No	70 X70X70				100X100X100			
	AGE	BRIAN	DOUGLAS	GSRB	AGE	BRIAN	DOUGLAS	GSRB
Time (sec)	10.000	41.467	48.718	110.440	122.000	200.000	200.000	200.000
Nodes	10	20	10	10	20	20	20	20
Nodes	710000	710000	710000	710000	710000	710000	710000	710000
P1	1.00000	1.00000	4.07000	1.70000	4.00000	4.00000	4.00000	4.00000
Max_Perror	1.00000	1.00000	1.00000	1.40000	1.40000	1.40000	1.40000	1.40000
1.00000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
1	1.00000	1.00000	1.00000	1.00000	1.00000	1.00000	1.00000	1.00000
2	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
3	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
4	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
5	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
6	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
7	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
8	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
9	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
10	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
11	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
12	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
13	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
14	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
15	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
16	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
17	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
18	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
19	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000
20	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000	1.40000

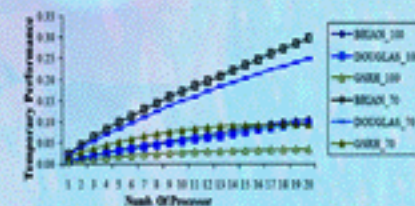
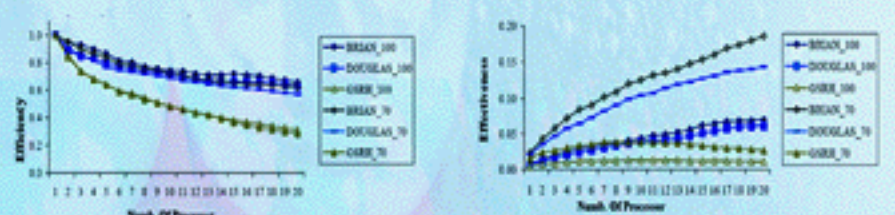
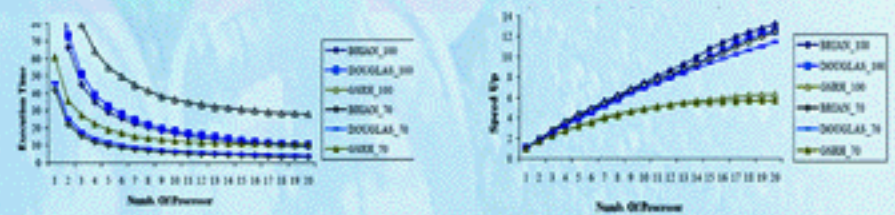
Table 1: Performance measurements of the sequential BRIAN and DOUGLAS schemes

in scheme	Substitutions	Addition
Coefficients	7	10
Level size	$30m^2 - 30m^2$	$15m^2 - 20m^2$
BRIAN	$5(m-1)^2 + 4m^2$	$13(m-1)^2 + 10m^2$
DOUGLAS	$12(m-1)^2 + 3m^2$	$13(m-1)^2 + 10m^2$
GSRB	$15(m-1)^2 + 14m^2$	$13(m-1)^2 + 12m^2$

Table 2: Computational cost for parallel strategies of BRIAN and DOUGLAS schemes

in scheme	Communication cost
coefficients	0
BRIAN	$12L((m-1)m) + 6L((m-1)m + 1)$
DOUGLAS	$12L((m-1)m) + 6L((m-1)m + 1)$
GSRB	$12L((m-1)m) + 6L((m-1)m + 1)$

L = number of interaction  
Table 3: Communication cost for parallel strategies of BRIAN and DOUGLAS schemes



Graphs of the execution time, speed up, efficiency, effectiveness and temporary performance vs. number of processor vs. number of processor using (70X70X70) and

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