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## All-Electrical Detection of the Relative Strength of Rashba and Dresselhaus Spin-Orbit Interaction in Quantum Wires

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We propose a method to determine the relative strength of Rashba and Dresselhaus spin-orbit interaction from transport measurements without the need of fitting parameters. To this end, we make use of the conductance anisotropy in narrow quantum wires with respect to the directions of an in-plane magnetic field, the quantum wire, and the crystal orientation. We support our proposal by numerical calculations of the conductance of quantum wires based on the Landauer formalism which show the applicability of the method to a wide range of parameters.

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With conventional electronics expected to reach critical boundaries for its performance soon, a new field of research utilizing the spin of the electron has evolved in recent years. Within this field called spintronics, much attention has been focused on spin-orbit interaction (SOI) because it provides a way of controlling the spin degree of freedom electrically in (nonmagnetic) semiconductorbased systems without the need of external magnetic fields. However, SOI in two-dimensional electron gases (2DEG) is a double-edged sword, since spin relaxation in disordered 2DEGs, which is typically dominated by the D'yakonov-Perel' (DP) mechanism [1], is enhanced for strong SOI. Since many promising semiconductor spintronics device proposals, e.g., the Datta-Das spin field effect transistor [2], rely on coherent spin transport, it is desirable to efficiently suppress the spin relaxation. In 2DEGs formed in III-V semiconductor heterostructures, there are typically two main SOI contributions, namely, Rashba SOI due to structural inversion asymmetry [3] and Dresselhaus SOI due to bulk inversion asymmetry of the semiconductor crystal [4]. An interesting situation occurs when the k-linear Rashba and Dresselhaus terms are of equal strength, i.e.,  $\alpha = \beta$ . Then spin is a good quantum number and DP spin relaxation is absent [5]. Lately, there has been much effort into this direction both theoretically with new device proposals [5,6] and experimentally with the aim to achieve  $\alpha = \beta$  [7]. Naturally, a precise control of the ratio  $\alpha/\beta$  is essential for spin manipulation and the operability of many spintronics devices. Since the strength  $\beta$  of the Dresselhaus SOI is fixed in a given quantum well, the most promising tool to modify  $\alpha/\beta$  is the control of the Rashba SOI strength  $\alpha$  via gate voltages [8].

To operate spintronics setups relying on the value of  $\alpha/\beta$  requires the ability to measure this ratio with high accuracy. Although it is possible to determine  $\alpha/\beta$  by using optical techniques [7,9,10], this is not always an option. If, e.g., the semiconductor heterostructure is covered by a top gate used to tune the Rashba SOI strength, it

is very difficult to carry out optical measurements; therefore, methods are highly desirable that allow one to determine the ratio  $\alpha/\beta$  from transport measurements. In principle, this can be achieved by fitting weak antilocalization (WAL) data from magnetoconductance (MC) measurements to analytical predictions [11,12]. However, the results usually bear a certain ambiguity, since one has to fit the data with several parameters and the possible error margins are thus quite large.

Hence, in this Letter, we propose an alternative, allelectrical method to determine the relative strength  $\alpha/\beta$ of Rashba and Dresselhaus SOI from measuring the conductance of narrow quantum wires defined in a 2DEG subject to an in-plane magnetic field. The method is based on the fact that only for a field parallel to the effective magnetic field due to SOI the weak localization (WL) correction to the conductance survives, while it is suppressed for all other directions. No fit parameters are required, and  $\alpha/\beta$  is straightforwardly related to this specific field direction, where the conductance is minimal.

We numerically calculate the conductance G of a disordered quantum wire realized in a 2DEG with SOI linear in momentum. The single-particle Hamiltonian of the quantum wire in the x direction reads [13]

$$\mathcal{H} = \frac{\pi_x^2 + \pi_y^2}{2m^*} + U(x, y) + \frac{\mu_B g^*}{2} [\vec{B}_{||} + \vec{B}_{so}(\vec{\pi})] \cdot \vec{\sigma},$$
(1)

with the effective spin-orbit field

$$\vec{B}_{so}(\vec{\pi}) = \frac{2}{\mu_B g^* \hbar} \{ \hat{e}_x [\alpha \pi_y + \beta (\pi_x \cos 2\phi - \pi_y \sin 2\phi)] + \hat{e}_y [-\alpha \pi_x - \beta (\pi_x \sin 2\phi + \pi_y \cos 2\phi)] \}$$
(2)

and the external in-plane magnetic field

$$\vec{B}_{\parallel} = B_{\parallel} [\cos(\theta - \phi)\hat{e}_x + \sin(\theta - \phi)\hat{e}_y]. \tag{3}$$

The vector potential components  $A_i$  in  $\pi_i = (p_i + eA_i)$ arise due to the perpendicular magnetic field  $B_z$  whose contribution to the Zeeman effect we neglect. In Eq. (2),  $\alpha$  and  $\beta$  are the Rashba and Dresselhaus SOI strengths, respectively, and  $\phi/\theta$  is the angle between the quantum wire or in-plane magnetic field and the [100] direction of the crystal for a zinc-blende heterostructure grown in the [001] direction. The electrostatic potential U(x, y) includes the confining potential for the quantum wire and the disorder potential from static nonmagnetic impurities in a region of length L. For the calculations we use a discretized version of the Hamiltonian (1) that allows us to evaluate the transport properties of the wire by computing lattice Green functions. For details see, e.g., Ref. [14]. The dimensionless numerical parameters used in this Letter (denoted by a bar) are related to real physical quantities as follows (for square lattice spacing a): energy  $\bar{E} =$  $(2m^*a^2/\hbar^2)E$  and SOI strengths  $\bar{\alpha} = (m^*a/\hbar^2)\alpha$  and  $\bar{\beta} =$  $(m^*a/\hbar^2)\beta$ . As a typical length scale for the simulations, we introduce  $W_0 = 20a$ . In the calculations, the disorder potential is modeled by Anderson disorder with strength  $\bar{U}_0$ . The mean free path is given by  $l = 2.4W_0\sqrt{E_F/U_0^2}$ , where  $\bar{E}_{\rm F}$  is the scaled Fermi energy. The conductance of the wire is obtained by averaging over  $N_d$  disorder configurations, and unless stated otherwise the following parameters are fixed:  $\bar{E}_{\rm F} = 0.5$  (corresponding to 4 propagating modes for a wire of width  $W_0$ ), L = $7.5W_0$ ,  $\bar{U}_0 = 1.4$  (i.e.,  $l \approx 0.87W_0$ ), and  $N_d = 10000$ .

To understand the mechanism for the detection of  $\alpha/\beta$ , which requires finite  $\vec{B}_{||}$ , we first study the conductance of quantum wires at  $B_{||}=0$ . Specifically, we present the MC for two cases, where WAL is suppressed: (a) Rashba and Dresselhaus spin precession lengths larger than the width of the wire W, i.e.,  $L_{\rm SO}^{\alpha}=(\pi\hbar^2/m^*\alpha)\gg W$  and  $L_{\rm SO}^{\beta}=(\pi\hbar^2/m^*\beta)\gg W$ , and (b)  $\alpha=\beta$ . In Fig. 1(a), we plot  $G(\Phi_s)-G(0)$  for wires with fixed  $\alpha\neq 0$ ,  $\beta=0$  and different widths W, showing that for smaller W WAL is suppressed, which is in line with earlier experimental

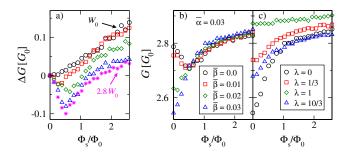


FIG. 1 (color online). Magnetoconductance of a quantum wire plotted against the magnetic flux  $\Phi_s = W_0^2 B_z$  in units of  $\Phi_0 = h/e$ . (a)  $\Delta G = G(\Phi_s) - G(0)$  for  $\bar{\alpha} = 0.03$  (i.e.,  $L_{SO}^{\alpha} \approx 5.2 W_0$ ),  $\bar{\beta} = 0.0$ , and widths  $W = W_0$ ,  $1.3 W_0$ ,  $1.8 W_0$ ,  $2.3 W_0$ , and  $2.8 W_0$  from top to bottom. (b)  $\bar{\alpha} = 0.03$ ,  $W = 2.3 W_0$ , and  $\phi = \pi/2$  for several values of  $\bar{\beta}$ . (c)  $\bar{\alpha} = \bar{\beta} = 0.03$ ,  $W = 2.3 W_0$ ,  $\phi = \pi/2$ , and  $\theta = \pi$  for several values of  $\lambda$ .

results [15] and confirms analytical [16] and numerical treatments [15]. Since spin relaxation is essential for WAL, the mechanism for the suppression of WAL can be attributed to an enhancement of the spin-scattering length in narrow wires [17,18] and, more generally, in confined geometries [19,20]. In case (b),  $\alpha = \beta$ ,  $\vec{B}_{so}$  points uniformly into the  $[\bar{1}10]$  direction for all k vectors, and a socalled persistent spin helix forms [21]. There the spin state of an electron is determined only by its initial and final position independent of the exact path in between. Therefore, charge carriers do not acquire an additional phase due to SOI upon return to their initial positions, resulting in constructive interference of the wave functions connected by time reversal and hence WL [22]. This behavior is shown for fixed W and  $\alpha$  but variable  $\beta$  in Fig. 1(b), where we observe that WAL is suppressed for  $\alpha = \beta$ . In both cases shown in Figs. 1(a) and 1(b), the absence of WAL is caused by the suppression of spin relaxation with the spin relaxation length exceeding the length of the wire L, where L in the numerical simulation takes the role of the phase coherence length in the

We now investigate the influence of an additional inplane magnetic field on the conductance of a quantum wire where WAL is suppressed. For convenience, we introduce the ratio  $\lambda = B_{\parallel}/|\vec{B}_{so}(k_x)|$ , which is the relative strength of the in-plane magnetic field and the effective magnetic field due to SOI for a k vector along the quantum wire; see Eqs. (2) and (3). In Fig. 1(c), we show the MC for the case  $\alpha =$  $\beta$  for several values of  $\lambda$ : The conductance at  $\Phi_s = 0$  is enhanced by a finite  $B_{||}$ . The form of the MC curves in Fig. 1(c) can be understood from the expression for the WL/WAL conductance correction from diagrammatic perturbation theory [23]. It is of the form  $\Delta G \propto (C_{00} \sum_{m=-1}^{1} C_{1m}$ ), where the first (singlet) term  $C_{00}$  contributes positively to the conductance and is responsible for the typical WAL peak in systems with SOI. It is unaffected by DP spin relaxation but suppressed by an in-plane magnetic field [24]. The second (triplet) term gives a negative conductance contribution and is suppressed for short spin relaxation times [23]. For the parameters used in Fig. 1(c),  $C_{00}$  is suppressed for  $\lambda \ge 0.15$ ; thus, in the respective curves shown in Fig. 1(c) only the triplet term is present in  $\Delta G$  resulting in positive MC  $(\partial G/\partial \Phi_s) > 0$ . While for  $\lambda = 0$  we observe WL due to  $\alpha = \beta$ , increasing  $\lambda$  gives rise to a transition to  $\partial G/\partial \Phi_s \approx 0$  at  $\lambda \approx 1$  and back to WL for  $\lambda \gg 1$ . This can be understood by the change of the spin relaxation in the system: For finite  $B_{\parallel}$  in a direction different from [ $\bar{1}10$ ] ( $\theta = 3\pi/4$ ), the resulting magnetic field  $\vec{B}_{\rm tot}(\vec{\pi}) = \vec{B}_{||} + \vec{B}_{\rm so}(\vec{\pi})$  will not be uniformly in the [110] direction anymore but cause spin relaxation, which is strongest for comparable strengths of  $B_{||}$  and  $\vec{B}_{so}$  and yields a reduction of the triplet term [green diamonds in Fig. 1(c)]. For in-plane magnetic fields which distinctly exceed the effective magnetic field ( $\lambda \gg 1$ ), on the other hand, WL is restored to some degree [blue triangles in Fig. 1(c)] since the resulting  $\vec{B}_{\rm tot}(\vec{\pi})$  is strongly aligned in the direction of  $\vec{B}_{||}$  and spin relaxation is reduced again. The enhancement of  $G(\Phi_s=0)$  in an in-plane magnetic field is anisotropic with respect to the direction of  $\vec{B}_{||}$ . For  $\theta=(3/4)\pi$ , spin remains a good quantum number due to  $\vec{B}_{||} \parallel \vec{B}_{\rm so}$ . Thus DP spin relaxation is absent, resulting in WL. This behavior can be observed in Fig. 2(a) , where  $G(\theta)$  at  $\Phi_s=0$  is shown for a slightly different geometry. Contrary to the case considered here, in systems showing WAL for  $B_{||}=0$ , the transition from WAL to WL is observed with increasing  $B_{||}$  [25,26] due to the reduction of the singlet term caused by  $\vec{B}_{||}$ .

We now investigate the conductance subject to an inplane magnetic field in quantum wires where WAL is suppressed due to a much smaller width with respect to the spin precession lengths. In Fig. 2, we plot the dependence of the conductance on the angle  $\theta$  for three different ratios  $\alpha/\beta$ . In order to understand the increase of G at  $\lambda >$ 0 for all but one angle  $\theta$ , we consider the case of a strictly one-dimensional quantum wire (1DQW) with SOI. We follow this approach, since for the system investigated in Fig. 2 the width of the wire is much smaller than the phase coherence length, a situation where it is sufficient to take into account only the transversal zero mode for the calculation of the quantum correction to the conductance [16]. A disordered 1DOW exhibits WL even if SOI of the Rashba and/or Dresselhaus type is present, since the spin is a conserved quantity in this limit. The effective magnetic field experienced by the electrons is exactly opposite for electrons traveling in the  $+\hat{x}$  or  $-\hat{x}$  direction, and thus no additional phase in the wave function is acquired by electrons returning to their original position. However, a finite in-plane magnetic field can suppress the WL and induce an increase in the conductance. If  $\vec{B}_{\parallel} \not\parallel \vec{B}_{so}(k_x)$ , the direction of the total magnetic field  $\dot{B}_{||} + \dot{B}_{so}(k_x)$  is different for electrons traveling in the  $+\hat{x}$  or  $-\hat{x}$  direction, resulting in spin relaxation and an increase of G (reduction of WL). A minimum in  $G(\theta)$  exists for  $\vec{B}_{\parallel} \parallel \vec{B}_{so}(k_x)$ , where no DP

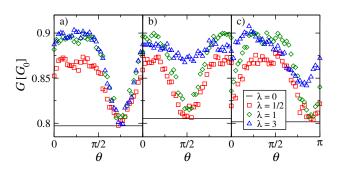


FIG. 2 (color online). Conductance of a wire of width  $W_0$  at  $\Phi_s=0, \quad \phi=\pi/2$ , and fixed  $(\mu_B g^* m^* a^2/\hbar^2) |\vec{B}_{\rm so}(k_x)| = \sqrt{2(\bar{\alpha}^2+\bar{\beta}^2)}=0.02$  with respect to  $\theta$  for different values of  $\lambda$ . (a)  $\bar{\alpha}=\bar{\beta}$ ; (b)  $\bar{\alpha}=0$ ; (c)  $\bar{\alpha}=3\bar{\beta}$ .

spin relaxation takes place since spin is still a good quantum number. In Fig. 2, we observe that the minimum of G appears at the angle which corresponds to the respective effective magnetic field direction for a k vector along the wire direction.

In view of the results of Fig. 2, we conjecture that also for a quasi-one-dimensional quantum wire with  $W \ll L_{\rm SO}^{\alpha/\beta}$  the angle at which the minimum in the conductance appears is given by the direction of the effective magnetic field  $\vec{B}_{\rm SO}(k_{\rm x})$  for a k vector along the wire direction  $\hat{x}$ :

$$\theta_{\min} = \arctan\left(-\frac{\alpha\cos\phi + \beta\sin\phi}{\beta\cos\phi + \alpha\sin\phi}\right). \tag{4}$$

In Fig. 3, we plot Eq. (4) for three different wire orientations  $\phi$  (solid lines), whose validity is nicely confirmed by extracting  $\theta_{\min}$  from the numerical  $G(\theta)$  dependence (such as Fig. 2) for different ratios of  $\alpha/\beta$  (symbols) with fixed  $\alpha + \beta$ . In order to use this feature for the determination of the ratio  $\alpha/\beta$ , we suggest to measure  $G(\theta)$  for quantum wires oriented either along the [100] or the [010] direction. Then the angle of the minimum conductance directly provides the unambiguous value for the relative strength and signs of  $\alpha$  and  $\beta$ . Choosing, e.g.,  $\phi = \pi/2$ , this ratio is given by  $\alpha/\beta = -\cot(\theta_{\min})$ , which is representative for the whole sample, since the influence of the lateral confinement on the strength of the SOI is negligible [27]. Considering quantum wires realized in InAlAs/InGaAs heterostructure (typical values  $m^* =$  $0.05m_0$  and  $g^* = 3$ ) and fixing the width  $W_0 = 350$  nm, we see that the parameters used in Fig. 3 ( $l \approx 412$  nm,  $B_{||} \approx 0.17$  T, and  $\alpha + \beta \approx 3.5 \times 10^{-12}$  eV m) are well in reach of present day experiments [25,28].

We have neglected effects due to the cubic Dresselhaus SOI term, which becomes increasingly important for wide quantum wells. In general, it induces additional randomization of the spin state, which for the case of a very strong cubic Dresselhaus contribution can result in the absence of the suppression of WAL [22]. Nevertheless, since cubic Dresselhaus coupling is smallest for k vectors along the [100] or [010] directions, we have neglected it for the determination of  $\alpha/\beta$ , since in our proposal the quantum

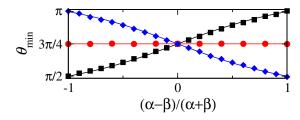


FIG. 3 (color online).  $\theta_{\rm min}$  determined numerically for a system with  $W_0$ ,  $\bar{\alpha}+\bar{\beta}=0.04$ ,  $\bar{U}_0=1.2$ ,  $(\mu_B g^* m^* a^2/\hbar^2)B_{||}=0.01$ , and  $N_d=20\,000$ . Black squares:  $\phi=\pi/2$ ; red circles:  $\phi=\pi/4$ ; blue diamonds:  $\phi=0$ . The solid lines represent Eq. (4) for the respective angles  $\phi$ .

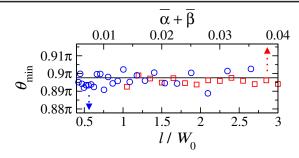


FIG. 4 (color online). Numerically determined  $\theta_{\min}$  for  $W_0$ ,  $\phi = \pi/2$ ,  $(\mu_B g^* m^* a^2/\hbar^2) B_{||} = 0.01$ ,  $N_d = 8000$ , and  $\alpha/\beta = 3$ . Either the mean free path l for fixed  $\bar{\alpha} + \bar{\beta} = 0.02$  (blue circles) or  $\bar{\alpha} + \bar{\beta}$  for fixed  $l \approx 0.87 W_0$  (red squares) was varied. The black line shows the expected value of  $\theta_{\min}$  from Eq. (4).

wire is assumed to be oriented in one of those directions. However, in contrast to a 1DQW, it might have an effect on  $\theta_{\min}$ , if it is comparable in strength to the linear term.

In order to assess possible limitations of this method, we performed calculations varying several parameters, while keeping the ratio  $\alpha/\beta=3$  constant. In Fig. 4, we show that Eq. (4),  $\theta_{\rm min}=\arctan(-1/3)\approx 0.9\pi$ , is fulfilled for a wide range of both SOI strengths (squares) and mean free paths (circles). Further numerical calculations, upon increasing the number of transverse orbital modes in the wire up to 13, showed that Eq. (4) still holds true (not presented here).

In conclusion, we have shown that Eq. (4), derived for a 1DQW, provides a valuable tool to determine the ratio  $\alpha/\beta$  also for a quantum wire with several transversal modes, only requiring  $W \ll L_{\rm SO}^{\alpha/\beta}$ , i.e., a suppression of WAL due to the confinement [15]. For increasing width,  $G(\theta)$  evolves into a behavior typical of a 2DEG [24,29], where  $G(\theta)$  is only anisotropic if both  $\alpha$ ,  $\beta \neq 0$ . Opposed to the narrow quantum wires considered where  $\theta_{\rm min}$  [Eq. (4)] is a function of  $\phi$ ,  $\alpha$ , and  $\beta$ , in a 2DEG the minimum of the conductivity appears at either  $\theta = \pi/4$  or  $3\pi/4$ , depending on the sign of the product  $\alpha\beta$  but independent of the ratio  $\alpha/\beta$ .

Apart from the condition  $W \ll L_{\rm SO}^{\alpha/\beta}$ , the method should be applied at sufficiently small  $B_{||}$  ( $\lambda \ll 1$ ). As can be seen from Figs. 2(b) and 2(c) when  $\lambda \gtrsim 1$ , G is increased for any  $\theta$ , potentially changing the position of  $\theta_{\rm min}$  [see, e.g., blue triangles in Fig. 2(c)]. Only for the case of  $\alpha = \beta$  shown in Fig. 2(a) does  $G(\theta_{\rm min})$ not increase, since  $\vec{B}_{\rm so}(\vec{k}) \parallel \vec{B}_{||}$  for any k vector. In this special case, the validity of Eq. (4) is not limited to narrow wires and small magnetic fields.

In summary, in narrow quantum wires which exhibit weak localization even in the presence of spin-orbit coupling, an in-plane magnetic field can suppress the weak localization effect. We employed the unique angular dependence of this effect to suggest a method for the direct

and experimental determination of the ratio between Rashba and Dresselhaus spin-orbit strengths from transport measurements. Its straightforward applicability may help to facilitate the design of semiconductor-based building blocks for spintronics.

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