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# Third Harmonic Generation in Organic Dye Solutions

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## 1 INTRODUCTION

Light at the third harmonic frequency,  $\nu_3=3\nu_L$ , may be generated by the direct third-order nonlinear interaction  $\nu_L+\nu_L+\nu_L+\nu_3$  due to the third-order nonlinear susceptibility  $\chi_{\text{THG}}^{(3)}$ , or it may be generated by cascading the second harmonic generation,  $\nu_L+\nu_L+\nu_2$ , and the frequency mixing,  $\nu_2+\nu_L+\nu_3$ . The cascading interaction is due to the second-order nonlinear optical susceptibilities  $\chi_{\text{SHG}}^{(2)}$  and  $\chi_{\text{FM}}^{(2)}$ . Phase-matching,  $\Delta k=0$ , is necessary for efficient light generation at the third harmonic frequency. Two nonlinear media in series are necessary for phase-matching both the second harmonic generation and the frequency mixing. The various generation schemes of phase-matched third harmonic light generation are summarized in Table 1.

In this paper the efficient phase-matched third harmonic generation in some organic dye solutions is studied. A picosecond Nd-phosphate glass laser is used as pump source. The third-order nonlinear susceptibilities and hyperpolarizabilities are determined. The limiting factors of the third-harmonic conversion efficiency at high pump pulse intensities are discussed. The third harmonic generation is resonantly enhanced by two-photon absorption (TPA,  $S_0$ - $S_1$  absorption peak between fundamental and third harmonic frequency). The phase-matching at a certain dye concentration is achieved by the anomalous dispersion of the refractive index of the dye above the  $S_1$ -absorption band.

**Table 1** Schemes of phase-matched light generation at third harmonic frequency. TPA = two-photon absorption. IC = inversion center.

Medium	Phase-matching	Process	Resonance	Reference
Metal vapors	puffer gas	direct	TPA	1-3
Inert gases	puffer gas	direct	-	4
Organic dye solutions	solvent	direct	TPA	5-11
vapors	puffer gas	direct	TPA	12
Birefringent crystals				
with IC	birefringence	direct	-	13-15
without IC	birefringence	direct and cascading	-	13,14 16,17
without IC	birefringence	cascading in two crystals	-	18,19
Liquid crystals and layered materials	reciprocal lattice vector	direct	-	20,21

## 2 RESULTS

### Determination of nonlinear susceptibilities

As long as other nonlinear optical processes and pump pulse depletion may be neglected the third harmonic energy conversion efficiency  $\eta_E = W_3/W_L$  is given by<sup>22</sup>

$$\eta_E = \frac{\kappa}{3^{3/2}} |x_{\text{THG}}^{(3)}|^2 I_{0L}^2 \quad (1)$$

with

$$\kappa = \frac{4\pi^2 v_3^2 \{ \exp(-3\alpha_L \ell) + \exp(-\alpha_3 \ell) - 2\exp[-(\alpha_3 + 3\alpha_L)\ell/2] \cos(\Delta k \ell) \}}{n_3 n_L^3 c_0^4 \epsilon_0^2 [(\alpha_3 - 3\alpha_L)^2/4 + \Delta k^2]} \quad (2)$$

$\alpha_L$  and  $\alpha_3$  are the linear absorption coefficients at  $\nu_L$  and  $\nu_3$ , respectively.  $n_L$  and  $n_3$  are the corresponding refractive indices.  $\ell$  is the sample length,  $c_0$  is the vacuum light velocity, and  $\epsilon_0$  is the permittivity. The

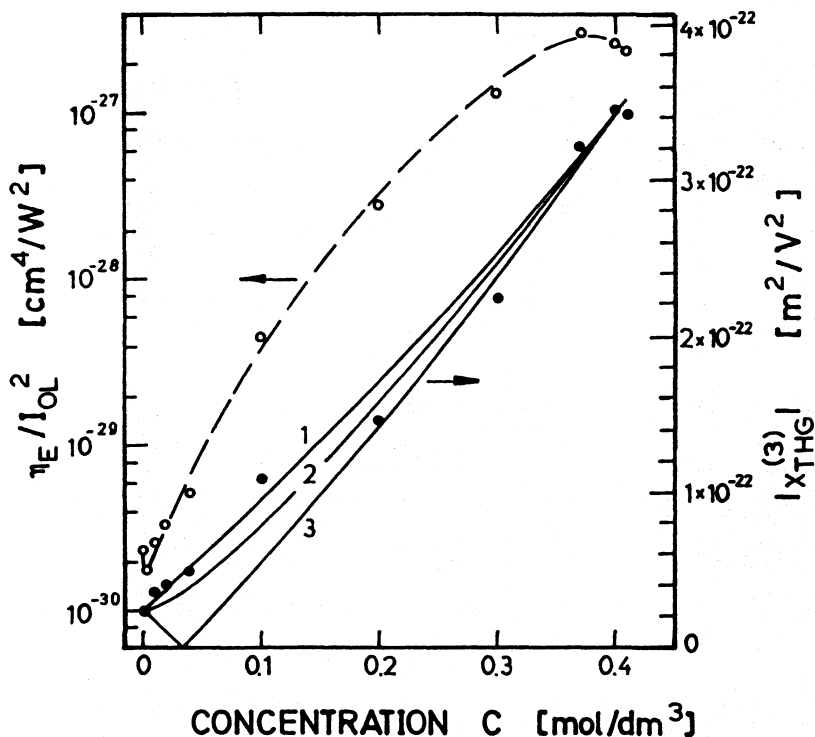


Figure 1 Third harmonic energy conversion efficiency and third-order nonlinear susceptibility for methylene blue in methanol. Solid curves are calculated for  $\chi_D^{(3)} > 0$  (1), imaginary (2), and  $< 0$  (3).

wave-vector mismatch is given by  $\Delta k = 6\pi\nu_L(n_3 - n_L)/c_0$ . A temporal and spatial Gaussian input pulse shape is assumed [intensity  $I_L = I_{OL} \exp(-t^2/t_0^2 - r^2/r_0^2)$ ]. An effective interaction length may be defined by

$$l_{\text{eff}} = \frac{\exp(-3\alpha_L l/2) + \exp(-\alpha_3 l)}{[(\alpha_3 - 3\alpha_L)^2/4 + \Delta k^2]^{1/2}} \quad (3)$$

The third order susceptibility  $\chi_{\text{THG}}^{(3)}$  comprises contributions from the solvent (S) and the solute (D), i.e.  $\chi_{\text{THG}}^{(3)} = \chi_S^{(3)} + \chi_D^{(3)}$ .  $\chi_S^{(3)}$  is real since the solvent is transparent, but  $\chi_D^{(3)} = \chi_{D'}^{(3)} - i\chi_{D''}^{(3)}$  is complex (resonance contributions). The nonlinear susceptibility  $\chi^{(3)}$  is related to the second hyperpolarizability by

$$\chi^{(3)} = NL^{(4)}\gamma^{(3)}/\epsilon_0 \quad (4)$$

$N$  is the number density of molecules and  $L^{(4)} = (n^2 + 2) \times (n^2 + 2)^3 / 81$  is the Lorentz-local field correction factor. The real and imaginary parts of  $\chi_D^{(3)}$  may be resolved by measuring the third harmonic energy conversion efficiency versus dye concentration.<sup>9</sup> For non-phased-matched third harmonic generation the cell windows and the surrounding air contribute essentially to the signal. A special experimental arrangement (sample in vacuum chamber and cell window thickness equal to an even multiple integer of the coherence length  $l_{\text{coh}} = \pi/\Delta k$ ) is necessary to avoid these contributions.<sup>22</sup> Fig.1 shows the third harmonic conversion efficiency and the resulting third-order nonlinear susceptibility versus concentration for the dye methylene blue in methanol.<sup>9</sup> The  $S_1$  absorption peak of methylene blue is at 650 nm and  $\chi_D^{(3)}$  is mainly real.

Table 2 contains experimental results of  $\chi^{(3)}$  and  $\gamma^{(3)}$ . The dye hyperpolarizabilities center around  $10^{-59} \text{ cm}^4 \text{ V}^{-3}$  ( $\approx 10^{-34}$  esu). The solvents are far out of resonance. Their hyperpolarizabilities are approximately a factor of 1000 smaller (for discussion see Ref.9).

### Efficient Phase-Matched Third Harmonic Generation

For some dyes phase-matched collinear third harmonic generation of Nd:glass laser pulses is possible at a fixed concentration  $C_{\text{PM}}$  due to the anomalous refractive index dispersion above the  $S_1$  absorption band. High conversion efficiencies require long effective interaction lengths (small linear absorptions  $\alpha_3$ , see Eq.3). The  $l_{\text{eff}}$  values at  $C_{\text{PM}}$  are given in Table 2. Fig.2 shows the absorption cross-section spectrum of the dye PYC in hexafluoroisopropanol. The absorption minimum of this dye is at 375 nm and does not coincide with  $\lambda_3 = 351.3$  nm. Nd-silicate glass lasers may be frequency tuned near to the absorption minimum.<sup>23</sup>

The third harmonic conversion efficiency  $\eta_E$  versus pump pulse peak intensity is plotted in Fig.3 for the

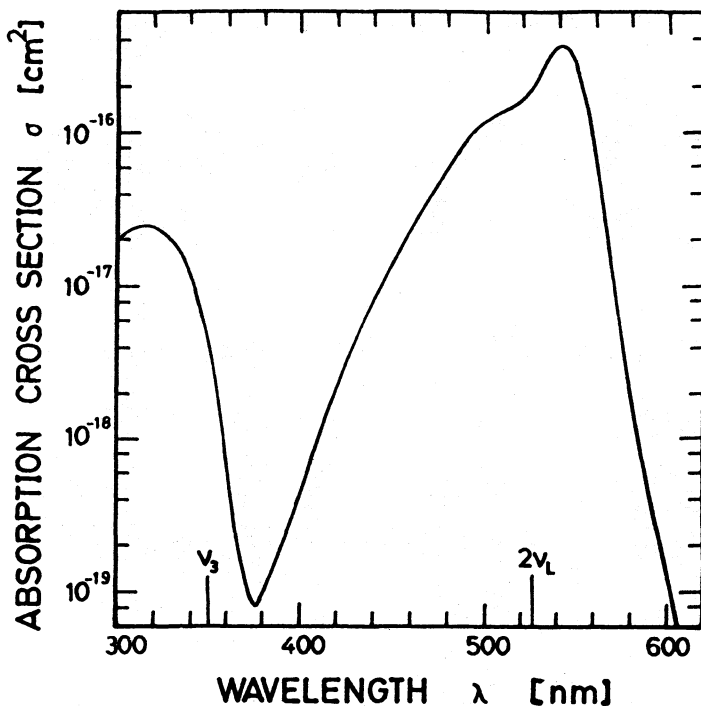


Figure 2 Absorption cross-section spectrum of 0.0825 molar PYC in HFIP.

dye PYC in hexafluoroisopropanol. At high pump pulse intensities the conversion efficiency saturates.  $\eta_E$ -values at  $I_{OL} = 2 \times 10^{11} \text{ W/cm}^2$  are listed in Table 2.

#### Limitation Of Conversion Efficiency

At high pump pulse intensities the two-photon absorption dynamics (two-photon absorption, excited-state absorption, amplified spontaneous emission, refractive index changes) and the self-phase modulation reduce the third harmonic conversion efficiency.<sup>11</sup> Some dependences of the conversion efficiency on material parameters are summarized in Table 3.<sup>1,2,11</sup>

Table 2 Dye and solvent parameters and THG results

Dye	Solvent	C [mol/dm <sup>3</sup> ]	$l_{\text{eff}}$ [ $\mu\text{m}$ ]	$ \chi_{\text{THG}}^{(3)} $ [m <sup>2</sup> V <sup>-2</sup> ]	$ \gamma_{\text{THG}}^{(3)} $ [cm <sup>4</sup> V <sup>-3</sup> ]	$\eta_E$ <sup>a)</sup>
Rhodamine 6G	ME	0.3 b)	2.8	$8 \times 10^{-22}$	$1.4 \times 10^{-59}$	
Fuchsin	ME	0.25 b)	7.9	$5.1 \times 10^{-22}$	$1.2 \times 10^{-59}$	
Methylene blue	ME	0.37 c)	13	$3.2 \times 10^{-22}$	$4 \times 10^{-60}$	
Safranin T	HFIP	0.33 c)	48	$1.7 \times 10^{-22}$	$3.3 \times 10^{-60}$	$1 \times 10^{-4}$
PYC	HFIP	0.0825 c)	113	$2 \times 10^{-22}$	$1.7 \times 10^{-59}$	$2 \times 10^{-4}$
HMICI	HFIP	0.08 c)	160	$2.48 \times 10^{-22}$	$2 \times 10^{-59}$	$4 \times 10^{-4}$
-	ME	24.73 b)	2.7	$2.4 \times 10^{-23}$	$6 \times 10^{-63}$	$1 \times 10^{-7}$
-	HFIP	9.46 b)	5.1	$1.4 \times 10^{-23}$	$1 \times 10^{-62}$	$1.3 \times 10^{-7}$

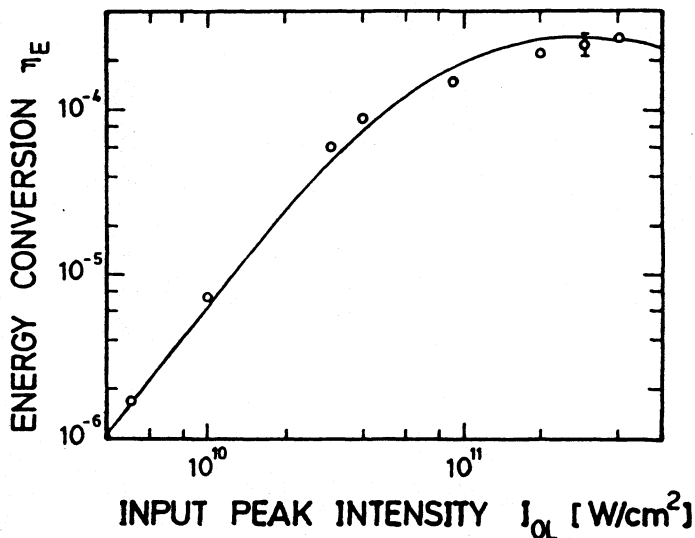
a:  $I_{\text{OL}} = 2 \times 10^{11}$  W/cm<sup>2</sup>. b: not phase-matchable. c: phase-matched concentration  $C_{\text{PM}}$ . ME = methanol. HFIP = hexafluoroisopropanol. PYC = 1,3,1',3'-tetramethyl-2,2'-dioxypyrimido-6,6'-carbocyanine hydrogen sulphate. HMICI = 1,3,3,1',3',3'-hexamethylindocarbocyanine iodide.  $\chi^{(3)}$  (esu) =  $(9 \times 10^8 / 4\pi) \chi^{(3)}$  (SI).  $\gamma^{(3)}$  (esu) =  $8.088 \times 10^{24} \gamma^{(3)}$  (SI).

### 3 CONCLUSIONS

The highest conversion efficiency obtained was  $4 \times 10^{-4}$ . Efficiencies  $\eta_E$  up to the percent region are expected for dyes with extremely low  $\alpha_3$  values and moderate excited state absorption cross-sections.

### REFERENCES

1. J.F. Reintges, 'Nonlinear Optical Parametric Processes in Liquids', Academic Press, Orlando, 1984.
2. J.F. Reintges, in 'Laser Handbook', edited by M. Bass and M.L. Stitch, North-Holland, Amsterdam, 1985, Vol.5, Chapter 1.
3. C.R. Vidal in 'Tunable Lasers', edited by F.L. Mollenauer and J.C. White, Springer, Berlin, 1987, p. 57.
4. A.H. Kung, J.F. Young and S.E. Harris, Appl. Phys. Lett., 1973, 22, 301.



**Figure 3** Third harmonic energy conversion efficiency of 0.0825 molar PYC in HFIP. Sample length 0.1 mm.

5. P.P. Bey, J.F. Guiliani and H. Rabin, IEEE J. Quant. Electron., 1971, QE-7, 86.
6. R.K. Chang and L.K. Galbraith, Phys. Rev., 1968, 171, 993.
7. J.C. Diels and F.P. Schäfer, Appl. Phys., 1974, 5, 197.
8. L.I. Al'Perovich, T.B. Baveav and V.V. Shabalov, Sov. J. Appl. Spectrosc., 1977, 26, 196.
9. W. Leupacher and A. Penzkofer, Appl. Phys., 1985, B36, 25.
10. W. Leupacher, A. Penzkofer, B. Runde and K.H. Drexhage, Appl. Phys., 1987, B44, 133.
11. A. Penzkofer and W. Leupacher, Opt. Quant. Electron., 1988, 20, 222.
12. V.F. Lukinykh, S.A. Myslivets, A.K. Popov, and V.V. Slabko, Appl. Phys., 1985, B38, 143.
13. P.D. Maker and R.W. Terhune, Phys. Rev., 1965, 137A, 801.
14. S.A. Akhmanov, L.B. Meisner, S.T. Parinov, S.M. Saltiel and V.G. Tunkin, Sov. Phys. JETP, 1977, 46, 898.
15. A. Penzkofer, F. Ossig and P. Qiu, Appl. Phys. B, to be published.
16. C.C. Wang and E.L. Baardsen, Appl. Phys. Lett., 1969, 15, 396.
17. P. Qiu and A. Penzkofer, Appl. Phys., 1988, B45, 225.



Table 3 Limitation dependences of third harmonic generation<sup>11</sup>

Linear absorption, $\alpha_L$	$\eta_E \propto  \chi_{\text{THG}}^{(3)} ^2 I_{\text{OL}}^2 \alpha_L^{-2}$
Linear absorption, $\alpha_3$	$\eta_E \propto  \chi_{\text{THG}}^{(3)} ^2 I_{\text{OL}}^2 \alpha_3^{-2}$
TPA of $2\nu_L$ , $\sigma_{\text{LL}}^{(2)}$	$\eta_E \propto  \chi_{\text{THG}}^{(3)} ^2 (\sigma_{\text{LL}}^{(2)})^{-2}$
Excited state absorption, $\sigma_{\text{ex}}$	
without ground state depletion	
( $\alpha_{\text{ex}} = N_{\text{ex}} \sigma_{\text{ex}} \alpha_{\text{ex}} \sigma_{\text{ex}}^{(2)} I_{\text{OL}}^2$ )	$\eta_E \propto  \chi_{\text{THG}}^{(3)} ^2 (\sigma_{\text{ex}} \sigma_{\text{LL}}^{(2)} I_{\text{OL}})^{-2}$
with ground state depletion	
( $\alpha_{\text{ex}} = N_D \sigma_{\text{ex}}$ )	$\eta_E \propto  \chi_{\text{THG}}^{(3)} ^2 I_{\text{OL}}^2 \sigma_{\text{ex}}^{-2}$
Refractive index dispersion	
( $D = \partial n_3 / \partial \nu - \partial n_L / \partial \nu$ )	$\eta_E \propto  \chi_{\text{THG}}^{(3)} ^2 I_{\text{OL}}^2 D^{-2}$
Refractive index change due to excited state population, $\Delta n$	Change of $C_{\text{PM}}$
Nonlinear refractive index, $n_2$	Change of $C_{\text{PM}}$

18. R. Piston, Laser Focus, 1978, 14/7, 66.
19. D. Eimerl, IEEE J. Quant. Electron., 1987, QE-23, 575.
20. J.W. Shelton and Y.R. Shen, Phys. Rev. Lett., 1971, 26, 538.
21. N. Bloembergen and A.J. Sievers, Appl. Phys. Lett., 1970, 17, 483.
22. M. Thalhammer and A. Penzkofer, Appl. Phys., 1983, B32, 137.
23. H. Schillinger and A. Penzkofer, Opt. Commun., to be publ.
24. R.W. Minck, R.W. Terhune and C.C. Wang, Appl. Opt., 1966, 5, 1595.