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Population dynamics of a non-cultivated biennial plant *Tragopogon pratensis* L. infected by the autoecious demicyclic rust fungus *Puccinia hysterium* (Str.) Röhl.

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1 **ABSTRACT**

2 Population dynamics of the biennial plant *Tragopogon pratensis* have been monitored
3 in the Park Grass Experiment at Rothamsted Research, Harpenden, UK, over many
4 years. Observations of diseased *T. pratensis*, systemically infected by the autoecious
5 demicyclic rust *Puccinia hysterium*, were made over the period 1995-2008, and
6 confirmed an outbreak pattern of dynamics, characterised by an increase to a
7 relatively high incidence to low almost indiscernible levels. An epidemiological
8 model was developed taking into account the biennial habit of the host plant, and the
9 systemic nature of infection during the winter period, and the partial sterilisation of
10 infected second year plants. Seedling emergence rate and natural mortality between
11 season and within season were key parameters affecting host performance. The
12 transmission rate between infected second year plants and susceptible first year
13 seedlings, and the probability that the fungus would survive the winter systemically as
14 mycelium producing aecia and telia on emerging second year plants, were key
15 parameters associated with pathogenicity. Furthermore the possibility of pathogen-
16 induced additional mortality was modelled. The model predicted that outbreak
17 dynamics of *T. pratensis* would occur with high pathogenicity and medium or high
18 host performance. In the former case the population dynamics would be cyclical, with
19 in some cases infected plants going to extinction. In the latter case both host and
20 pathogen would go to extinction. The model predicted that the two pathogenicity
21 parameters were critical in determining whether the pathogen would invade a healthy
22 population; whereas pathogen induced mortality had little influence, a result also
23 obtained in some limited potted plant experiments. Fitting the model to the field data
24 indicated that there was little or no density-dependence in seedling emergence rate,
25 and again that pathogen-induced mortality played little role in the observed population
26 dynamics.

27

28 **INTRODUCTION**

29 Pathogens can play a key ecological role in natural plant communities impacting on
30 species performance, affecting viability and fecundity of individual plants, reducing
31 population size, generating selective forces for genetic change, and altering
32 community structure (Burdon 1982; Burdon *et al.* 1989; Dinoor & Eshed 1990; Thrall

33 & Burdon 1997; Frantzen & Muller-Scharer 2002; Burdon *et al.* 2006). However,
34 there have been few attempts to model epidemics in natural plant populations in non-
35 cultivated systems, with many studies mostly limited to empirical descriptions that
36 ignore theoretical implications or applications (Dobson & Grenfell 1995). Models
37 have been developed describing the population dynamics of annual plant hosts and
38 soil-borne pathogens (Thrall *et al.*, 1997); dispersal characteristics and disease
39 dynamics in populations (Thrall & Burdon, 1999; Frantzen & van den Bosch, 2000);
40 and especially in recent years, combining spatial statistics with spatially explicit
41 models to estimate rates of spread and effects of regional heterogeneity on co-
42 evolutionary processes (Ovaskainen & Laine 2006; Brooks *et al.* 2008; Soubeyrand
43 *et al.* 2009; Smith *et al.* 2011).

44

45 The Park Grass Experiment (PGE) at Rothamsted Research, Harpenden, UK, is the
46 oldest continuous ecological experiment in the UK, with work conducted on long-
47 term plant population dynamics over many years (Silvertown *et al.* 2002). Plant
48 species within the PGE have shown a range of dynamics including: increases (e.g.
49 *Trifolium pratense*), decreases (e.g. *Veronica chamaedrys*), and fluctuations (e.g.
50 *Conopodium majus*) in population size. Other species (e.g. *Tragopogon pratensis*)
51 followed an outbreak dynamic in which the population increased and then declined
52 (Dodd *et al.* 1995). Many of these patterns have been interpreted as consequences of
53 the long-term fertiliser regimes altering the soil nutrient content and pH. However it
54 has been speculated that the outbreak pattern of dynamics of the biennial species *T.*
55 *pratensis* has been due to an autoecious, demicyclic rust, *Puccinia hystereum*
56 (Silvertown *et al.* 2006). It is also possible that edaphic factors may affect the plant-
57 pathogen interaction directly, as found in other systems studied (Springer, 2009).
58 Unfortunately the long term PGE data set does not include the recorded incidence of
59 rust infection.

60

61 Importantly, the rust is systemic during the wintering of the biennial host. This
62 systemic nature is relatively unusual as systemic rusts are more prevalent in arctic and
63 montane ecosystems (Wennström 1999). The example most cited of a systemic rust is
64 *P. punctiformis* on *Cirsium arvense* and other thistle species (Frantzen 1994; Cripps *et*

65 *al.* 2009), with other examples noted including *P. pulsatillae*, *P. pratensis*, *P.*
66 *monoica* and *P. thlaspeos* (Jarosz & Davelos 1995). Similarly to *P. hystereum*, *P.*
67 *thlaspeos* is a systemic rust but does not vertically transmit through seeds (Kropp *et*
68 *al.* 2002), therefore transmission is solely through spore dispersal. *P. hystereum*
69 suppressed reproduction of *T. pratensis* (Salama *et al.* 2010), whilst in a similar non-
70 cultivated host-pathogen system, the rust *P. lagenophorae* significantly altered plant
71 fitness by reducing seed production of *Senecio vulgaris* (Paul & Ayres 1986a; 1986b).
72 Both *P. lagenophorae* and *P. hystereum* are demicyclic and lack an asexual repeating
73 urediospore phase (Wilson & Henderson 1966).

74

75 The scientific literature on *P. hystereum* is sparse. The life history involves teliospores
76 from diseased second year plants infecting first year plants from June to the end of the
77 growing season (Parmelee & Malloch 1972). Symptoms are not normally seen on first
78 year plants. The dispersal period is often interrupted in traditional hay meadows (such
79 as the PGE) by a “hay cut” at the end of June which limits the infective period.
80 Basidia develop from germinated teliospores on first year plants and produce
81 basidiospores which can also be transported to new hosts. The basidiospores
82 germinate to produce systemic mycelia, which enable the pathogen to survive the die-
83 back period during the host’s below-ground overwintering phase. Pycnia develop and
84 undertake a sexual stage as pycniospores. The following season, surviving plants re-
85 emerge exhibiting aecia formed mostly on the stem, giving the typical “cluster cup”
86 appearance, which produce aeciospores. Aeciospores germinate on the host tissue and
87 germ tubes either directly penetrate tissue or grow through natural openings such as
88 stomata. Telia, bearing teliospores on localised mycelium are then produced (Wilson
89 & Henderson, 1966) completing the cycle.

90

91 This paper investigates the hypothesis presented by Silvertown *et al.* (2006) that *P.*
92 *hystereum* has a regulatory influence on its host population dynamics and that this
93 relationship is density dependent (Silvertown *et al.*, 2002). This assessment is
94 undertaken by presenting data relating to the long term population dynamics of the
95 system in the PGE and attempting to obtain information on pathogen induced
96 mortality through the use of inoculation experiments. Biological characteristics of a

97 biennial host – systemic pathogen system are then incorporated into an
98 epidemiological model which is used to determine conditions under which population
99 dynamics similar to those observed for *T. pratensis* infected by *P. hystrium* in the
100 PGE are simulated. Specifically the epidemiological model takes into account the
101 biennial nature of the host plant *T. pratensis* and the systemic characteristics of the
102 rust, *P. hystrium*. The model is of *SIR* form, in which host categories are defined as
103 Susceptible, Infectious and Removed (Anderson & May 1979), and models non-
104 continuous host generations using discrete time. Such compartmentalised models of
105 disease dynamics have been used previously to represent plant – fungal pathogen
106 dynamics in continuous time (Gilligan, 2002). The model developed here is an
107 example where a discrete-time approach (Allen 1994; Switkes, 2003) provides a more
108 appropriate representation of the host–pathogen system, given the biennial host
109 characteristics, the unusual yet key systemic nature of the rust pathogen, and the
110 infection process linking second and first year plants. Expanded forms of the discrete
111 *SIR* model have been used to describe gene frequency and disease spread in plant
112 populations (Kesinger *et al.*, 2001).

113

114 The model was developed to be sufficiently flexible to include the impact of
115 pathogen-induced mortality on the ability of first year plants to overwinter and to re-
116 emerge and grow in the second growing season. Pathogen-induced mortality - often
117 termed *virulence* in human and animal epidemiology, see Antonovics (2005) - has
118 been reported for a wide range of plant foliar diseases (e.g. *Mycosphaerella laricina*
119 on Pinaceae), systemic diseases (e.g. *Urocystis trientalis* on *Trientalis europaea*), as
120 well as a range of cankers, wilts and butt rots (Gilbert 2002). Thus we incorporated
121 within, as well as between, growing season pathogen-induced mortality. Specifically
122 this type of pathogen-induced mortality has been reported with late infections of
123 *Puccinia*, e.g. *S. vulgaris* infection by *P. lagenophorae*; at the beginning of a growing
124 season, infected host plants have a lower probability of survival, but also increase
125 their chances of mortality in the overwintering phase (Frantzen & Müller-Schärer
126 1999). Within our model, pathogen-induced mortality of individual plants has an
127 effect on the population dynamics of the host, not simply by altering the number of
128 seedlings through partial sterilisation of infectious individuals, but also by reducing
129 the numbers of infected first year plant individuals which potentially become

130 infectious when there is additional mortality between seasons. Additionally, within
131 season pathogen-induced mortality reduces the number of second year infectious
132 individuals that can infect first year susceptible plants in the same season. Within the
133 modelling framework we consider both constant and variable pathogen-induced
134 mortality.

135

136 **METHODS**

137 **Field observations**

138 Vegetative and flowering *T. pratensis* individuals and signs of rust infection were
139 recorded in each of the subplots prior to the annual hay cut at the PGE in late-June
140 from the years 1995 – 1998 and 2000 – 2004 using one 10 x 2 m quadrat placed in the
141 centre of each of the 97 subplot from the 24 plots. Each of the plots varied in size and
142 had a range of fertilizer and pH treatments applied (Silvertown *et al.* 2006). These
143 counts may be an underestimation due to the difficulty of identifying first year
144 individuals. During the years 2005 – 2008 the methods of data collection were
145 modified due to plot access restrictions that were imposed at the PGE. This modified
146 method involved using five 1m x 1m quadrats placed at random near the edges of
147 each sub plot. These quadrats are likely to adequately represent the situation in the
148 rest of a subplot because plants are distributed relatively homogeneously throughout a
149 plot and there are sharp boundary characteristics due to minimal lateral nutrient
150 movement between plots (Crawley *et al.* 2005). Within each transect or quadrat, the
151 numbers of flowering and vegetative individuals were recorded and rust incidence
152 assessed using a three point score (uninfected, low infection, high infection); however
153 this scoring was subsequently simplified to rust presence or absence.

154

155 **Estimations of *P. hystrium* infection, overwintering survival and induced plant** 156 **mortality**

157 In order to ascertain mortality rates, 100 *T. pratensis* seeds collected from the Royal
158 Horticultural Society (RHS) gardens, Wisley, in 2005 were germinated and grown in
159 pots (diameter 130mm, height 121mm). Half of the cultivated first year individuals

160 were artificially inoculated with *P. hysterium* using a method of brushing infected
161 plant material, bearing both aecia and telia and also collected from the RHS gardens
162 with a camel hair brush over talc, and then applying the talc/inoculum powder over
163 susceptible individuals at dusk, so optimising stomatal opening, and the other half
164 sprayed with water as a control. The plants were kept in high humidity for four days
165 using dew chambers. Plants were then kept outside under natural conditions, allowed
166 to die back over the winter, and monitored for re-emergence as second year plants in
167 the spring and for the incidence of rust infection. The effects of inoculation on
168 survivorship were quantified (Salama 2009). A second cohort of individuals was
169 grown and inoculated using the same method the following season. For both cohorts
170 the second year plants were kept in pots for a second winter to check on whether they
171 re-emerged for a third year.

172

173 **Model description**

174 The epidemiological model was developed in discrete time for a closed biennial host –
175 pathogen system (Fig 1) with characteristics similar to the *P. hysterium*/*T. pratensis*
176 system. We assume the biennial host has a vegetative, non-seeding first year when
177 individuals are healthy and susceptible (*S*) to infection. First year plants are exposed
178 to inoculum from infectious second year plants (*I*). The average number of spores
179 deposited on a plant is proportional to the density of infectious second year plants.
180 The probability that no spores are deposited on a healthy plant is given by the first
181 term of the Poisson distribution, $e^{-(cI)}$, which gives the infection frequency as $1 - e^{-(cI)}$
182 (Madden *et al.*, 2008) where c is the effective transmission rate between infectious
183 and susceptible individuals. Individual plants are exposed (*E*) and latently infected at
184 the end of their first growing season, or non-exposed, then die back and overwinter
185 below ground. The plants re-emerge the following year and reproduce (i.e. are
186 monocarpic). A proportion (p) of exposed individuals become infectious (*I*) second
187 year plants, a proportion $(1-p)$ of the exposed individuals emerge as healthy (*R*)
188 second year plants, as do the non-exposed individuals. Re-emerging healthy second
189 year plants are effectively removed from the epidemic dynamics as they do not
190 contribute to subsequent infection of first year plants, nor do they become infected by
191 *I* plants. Individual plants have mortality rates b within season and d between seasons,
192 and have a pathogen-induced mortality rate (β) which is assumed to be related to the

193 numbers of infectious individuals according to the flexible term $\beta e^{-\sigma I}$, which can
 194 represent different forms of pathogen-induced mortality. For $\sigma = 0$, pathogen induced
 195 mortality is constant ($= \beta$); when σ approaches ∞ , there is effectively no pathogen
 196 induced mortality; and when $0 < \sigma \leq f$, where f is a finite upper bound for σ , there is a
 197 variable form of pathogen induced mortality that decreases with the size of the
 198 infected population. The latter possibility may be associated with selection for
 199 decreased virulence in the pathogen (or alternatively for increased resistance or
 200 tolerance in the host) as the pathogen population increases. R individuals set seed with
 201 a seedling emergence rate a . We assume that I individuals are sterilized and do not
 202 contribute seed to the following generation, but note that this is an oversimplification
 203 as sterilization is incomplete (Salama *et al.*, 2010). The seedling emergence rate is
 204 also density-dependent, using the λ parameter as proposed by de Wit (1960)
 205 specifically for plant populations. The higher is the value of this parameter, the greater
 206 the level of density dependence. Although there may be additional intra-specific (from
 207 non-seed producing I plants) and inter-specific competition from the plant meadow
 208 community, these additional complications to the model are not investigated. As noted
 209 above there is a natural mortality within (b) and between (d) seasons.

210

211 With these assumptions the host categories are linked in the following system of
 212 equations:

$$213 \quad S_{t+1} = \frac{a(1-b)R_t}{1 + (1-b)\lambda R_t} \quad (1)$$

$$214 \quad I_{t+1} = (1-d)(1-b)(1 - \beta e^{-\sigma I_t}) p S_t \left(1 - e^{-c(1-b)(1-\beta e^{-\sigma I_t}) I_t} \right) \quad (2)$$

$$215 \quad R_{t+1} = (1-b)(1-d) S_t \left[1 - p \left(1 - e^{-c(1-b)(1-\beta e^{-\sigma I_t}) I_t} \right) \right] \quad (3)$$

216 A full derivation of this *SIR* model from the *SEIR* formulation described above is
 217 given in Appendix 1. These equations can also be adapted to cases where there are
 218 differential within and between season mortality rates and/or mixed constant and
 219 variable mortality rates, but these elaborations are not considered in this paper.

220

221 Numerical and analytical techniques were used to determine the quantitative and
222 qualitative properties of the three models representing the three forms of pathogen
223 induced mortality (Equations 1-3 with σ set accordingly). Implicit solutions for the
224 steady-state density of infected individuals I^* , i.e. when there was no change in the
225 size of host categories between time-steps t and $t+1$, were obtained (Appendix 2).
226 Time plots of the model were obtained numerically using R 2.7.2 (R development
227 core team) for varying parameter values. In addition, an invasion criterion
228 determining whether the pathogen could establish following introduction was derived.
229 Finally a second-order recurrence equation was derived from the models describing
230 the relationships between population sizes at discrete time intervals (Appendix 3).

231

232 **Obtaining parameter values**

233 Numerical data for approximating parameter values were obtained from field
234 observations and greenhouse trials (Salama 2009; Salama *et al.* 2010), unpublished
235 survey data by two of the authors (G. Edwards and M. Heard) collected from the
236 PGE, and published material relevant to *T. pratensis*, *P. hystericum* and similar host –
237 pathogen systems (Table 1). The population dynamics of *T. pratensis* in the entire
238 PGE were plotted against year with polynomial models of the n^{th} order (with $2 \leq n <$
239 6) used to interpolate missing data using Microsoft Excel (Microsoft Corp. 2003).

240

241 **RESULTS**

242 **Survey data**

243 *T. pratensis* was found in all but one of the plots and 15 subplots between 1995 –
244 2008, across a range of fertiliser and pH treatments. The survey data demonstrates the
245 outbreak nature of infected second year plants (Fig. 2a) in plots under differing
246 treatment types and of healthy second year plants across all plots in the PGE (Fig. 2b),
247 in both cases followed by a low but stable population size. Although no data were
248 collected in 1999, 2000 and 2005 these data were interpolated using polynomial
249 regression. The intention here was simply to obtain missing values for use in
250 subsequent model investigations, not to model the epidemic. A range of polynomial

251 orders was used in the regressions, the predicted values were compared with observed
252 values, and goodness of fit tested adjusting for the degrees of freedom in the
253 regressions. Polynomials which predicted negative values were rejected irrespective
254 of the fit obtained. On this basis a 6th order polynomial provided the most consistent
255 estimates for the missing values [adjusted $R^2 = 0.881$; F-value = 13.34 (6,4 d.f.); $p =$
256 0.013]. When comparing the observed versus predicted values a good linear fit was
257 obtained for the 6th order polynomial, having a slope not differently different from 1
258 and a positive intercept close to 0. The missing values obtained in this way for healthy
259 second year plants are shown in Fig. 2(b). A similar procedure was used to estimate
260 missing values for the infected plants and again a 6th order polynomial was chosen as
261 most suitable for the purpose intended - to obtain missing values used in subsequent
262 model investigations. The initial numbers of hosts used in the simulations (Table 1)
263 were set as the lowest non-zero recordings in the PGE.

264

265 **Inoculation experiments**

266 Because of the difficulty in observing spore dispersal (transmission), disease
267 expression (probability of an exposed first year plant becoming an infected second
268 year plant), and the influence of infection on host survivability in the field, plant
269 inoculations were conducted with potted plants under greenhouse conditions. In 2005
270 seeds collected from RHS Wisley were germinated, but due to facility restrictions,
271 only 100 of the germinated seeds were grown to form the first cohort of susceptible
272 first year plants; of these, 50 were artificial inoculated and 50 treated as controls. The
273 method of inoculation does not necessarily mean that plants had been exposed to a
274 sufficient infective dose; without detailed histological work (beyond the scope and
275 scale of this study), there was no way of ascertaining until re-growth the following
276 season whether plants had been infected. This made it difficult to estimate the value of
277 p in these inoculation experiments. Furthermore expression of disease in second year
278 plants in the field is a composite of p and c and it is difficult to distinguish the relative
279 contribution of either factor.

280

281 In 2006, 15 of the control plants did not re-emerge, whereas all the inoculated plants
282 survived the over-wintering phase and three of these plants produced aecia,
283 suggesting a p value of 0.06. All re-emerged plants were monitored until July to
284 assess within season mortality. Of the 82 healthy plants ($50-15 = 35$ from the re-
285 emerged control group, $50-3 = 47$ from the re-emerged inoculated group) four
286 suffered mortality whilst all three of the diseased plants survived. These results show
287 no evidence for pathogen-induced mortality. Seeds were collected from healthy and
288 infected plants; additionally these second year plants remained in pots until the
289 following season. In 2007, none of the three diseased plants re-emerged, whereas 16
290 of the 78 healthy plants re-emerged again as healthy second year type individuals,
291 surviving the 2007 season but did not re-emerge in 2008. This demonstrates that pot
292 grown plants have differing characteristics to their biennial nature in the field, most
293 likely due to the managed interventions and conditions which also make the
294 estimation of rates of natural within and between season mortality difficult.

295

296 Of the 100 seeds collected for the second cohort of plants in 2006, 50 were inoculated
297 and nine emerged in 2007 all with aecia, suggesting a p value of 0.18. There was also
298 high mortality for the 50 control plants with only five re-emerging as healthy second
299 year plants, suggesting a high natural between-season mortality rate of 0.90; one of
300 the five died in the 2007 season. Again these results show no evidence for pathogen-
301 induced mortality. The remaining plants were left to overwinter again resulting in no
302 re-emergence of the nine infected plants, and re-emergence of three second year type
303 plants from the four remaining healthy plants, of which one died during the 2008
304 season.

305

306 These findings illustrate the difficulties inherent in estimating life-history parameters
307 including natural mortality under pot conditions for a non-cultivated host-pathogen
308 system. The values in Table 1 are thus best estimates based on the sources identified
309 above. The between season mortality rates in these pot-grown plants varied
310 considerably between the two cohorts, and for within-season mortality are likely to be
311 an underestimate due to the managed growing conditions; however within season
312 mortality was in the order of 15-30 %, whilst overwintering mortality was in the order

313 of at least 30% There was no evidence for pathogen-induced mortality in these results.
314 However, the similar cultivation of *S. vulgaris* (Frantzen 2007) demonstrates that such
315 evidence can be found for a different system. Because of these uncertainties we
316 produce simulations under a range of values for β , c and p .

317

318 **Modelling investigation**

319 *Steady states in the absence of the pathogen*

320 In the absence of the pathogen the equations for healthy first and second year
321 individuals are:

$$322 \quad S_{t+1} = \frac{a(1-b)R_t}{1+(1-b)\lambda R_t}$$

$$323 \quad R_{t+1} = (1-b)(1-d)S_t$$

324 Giving steady-state expressions in the absence of the pathogen as:

$$325 \quad \hat{R} = \frac{a(1-b)^2(1-d)-1}{\lambda(1-b)} \quad (4)$$

$$326 \quad \hat{S} = \frac{a(1-b)^2(1-d)-1}{(1-b)^2(1-d)\lambda} \quad (5)$$

327 Provided that the condition $a(1-b)^2(1-d) > 1$ is met, the plant population will
328 approach a steady-state population size determined by the seedling emergence
329 density-dependence parameter, λ , and plant mortality rates, b and d . This expression is
330 intuitive as it is the product of the seedling rate, mortality within the two growing
331 seasons (thus the squared term), and mortality during the one winter period.

332

333 *Derivation of the invasion criteria*

334 The conditions for pathogen invasion within the host population were derived for the
335 three forms of pathogen-induced mortality. For the pathogen to persist within the
336 system the basic reproductive number (R_0) must be greater than one (Anderson &
337 May, 1979).

338 For the case with no disease-induced mortality (equations 1 – 3, $\beta = 0$), the criterion
 339 for the pathogen to invade was obtained as:

$$340 \quad \frac{I_{t+1}}{I_t} = (1-b)^2(1-d)pc\hat{S} = \frac{pc[a(1-b)^2(1-d)-1]}{\lambda} > 1 \quad (6)$$

341 Where for infinitesimally small values of I , $1 - e^{-c(1-b)I_t}$ was approximated by
 342 $c(1-b)I_t$

343 or equivalently:

$$344 \quad \hat{S}(1-b)^2(1-d)pc > 1 \quad (7)$$

345 The expression on the left hand side has a direct interpretation as the basic
 346 reproductive number of the disease. If one infected second year plant is introduced
 347 into a susceptible first year population then the number of second year infected plants
 348 that will result in the following year is determined by the product pc (the number of
 349 successful infections that emerge) corrected for by the survival terms over the two
 350 growing seasons and the one between seasons.

351

352 Thus, if a pathogen is introduced into a previously healthy plant population then the
 353 transmission rate c and the probability of overwintering survival p must be
 354 sufficiently high for this criterion to be met and for the pathogen to establish.

355

356 Similarly for models with constant pathogen-induced mortality, for infinitesimally
 357 small values of I , the term $1 - e^{-c(1-b)(1-\beta)I_t}$ can be approximated by $c(1-b)(1-\beta)I_t$.

358 The criterion for pathogen invasion is then:

$$359 \quad \hat{S}(1-\beta)^2(1-b)^2(1-d)pc > 1 \quad (8)$$

360

361 In the case of variable disease-induced mortality, when I is infinitesimally small, the
 362 criterion derived is the same as equation 8.

363

364 In all three cases the pathogen invasion criteria depends on the transmission rate, the
365 probability that an exposed individual will become infectious in the second year,
366 pathogen induced mortality (where non-zero), as well as the background host
367 mortality between and within season and the susceptible host population size.

368

369 *Model Simulations*

370 Parameter values (Table 2) were used to generate a range of outputs representing
371 high, medium and low host performance (a, b, d, λ) and similarly high, medium and
372 low pathogenicity (p, c, β). Performance here is used to define the level of host
373 mortality, recruitment and density-dependent seedling emergence; whilst
374 pathogenicity describes the rates of pathogen-induced mortality, and disease
375 expression (following overwintering survival). The ranges in parameter values were
376 considered for the three model formulations presented above. We also applied a
377 transmission-virulence trade-off in the pathogenicity parameters but this aspect is not
378 developed further in this paper due to the absence of genetic information for this host-
379 pathogen system.

380

381 In general the models produced similar outcomes, although varying in transient
382 dynamics. The model simulation outputs with medium pathogenicity and medium
383 host performance produced steady-state populations for both healthy and infected
384 plants (Fig. 3a) within the population. Under conditions where low pathogenicity was
385 combined with a low host performance (Fig 3b) infected plants became extinct. Both
386 healthy and infected plant populations became extinct when high pathogenicity and
387 high host performance were combined (Fig 3c).

388

389 Cyclical dynamics occur when high pathogenicity is combined with medium host
390 performance; however the trajectory of the population cycles differ dependent on the
391 model used. Where there is no pathogen-induced mortality (Fig. 4a) or there is
392 variable pathogen-induced mortality (Fig. 4c) the host population cycles, but then
393 tends to a steady-state population size where infected plants are absent from the

394 population. Continual, repeating population cycles are obtained when constant
395 pathogen-induced mortality is maintained (Fig 4b). Other combinations of host
396 performance and pathogenicity levels tended to stable steady values without cycles.

397

398 *Parameter influence on the disease invasion criterion*

399 Using the derived invasion criterion for the constant pathogen-induced mortality form
400 of the model (Equation 8) it is possible to obtain the parameter space where the
401 criterion conditions are met by altering pathogen parameters and host population size.
402 For the case of constant pathogen-induced mortality, with for simplicity the mortality
403 rates set to $b = d = 0.3$, Fig 5 demonstrates the range of parameter values that satisfy
404 the invasion criterion.

405

406 *Derivation of recurrence relationships*

407 Second-order (two time-step) recurrence equations were derived (Appendix 3) to
408 represent the relationship between population sizes at different discrete time intervals.

409

410 For the model without pathogen induced mortality the following relationship was
411 derived:

$$412 \quad \frac{1}{I_{t+2} + R_{t+2}} = \frac{1}{a(1-b)^2(1-d)R_t} + \frac{\lambda}{a(1-b)^2(1-d)} \quad (9)$$

413 This indicates that infected second year plants are simply replacing healthy second
414 year plants in the overall relationship (the recurrence relationship derived in the
415 absence of disease is identical to equation 9 with $I_{t+2} = 0$). There are no pathogenicity
416 parameters contained on the right hand side of the recurrence relationship.

417

418 However, when pathogen-induced mortality is included in the model, a recurrence
419 relationship is derived in which:

$$420 \quad \frac{(1-\beta)}{I_{t+2} + (1-\beta)R_{t+2}} = \frac{\lambda}{a(1-b)^2(1-d)} + \frac{1}{a(1-b)^2(1-d)R_t} \quad (10)$$

421 This indicates that disease-induced mortality would directly affect the population
 422 dynamics as the β parameter appears on the left hand side of the equation.

423

424 *Infected plant steady-states*

425 A necessary condition for an endemic steady-state of diseased plants is that the
 426 invasion criterion is met, depending on the form assumed for pathogen-induced
 427 mortality (Equations 6-8). As shown in Fig. 4 the transient approach to steady states
 428 can show many complexities in the cycling behaviour. Simulations across some 1000
 429 combinations of values of β , p and c , with other parameters held at default values
 430 (outlined in Table 1), were made and less than half of these showed single stable
 431 steady states corresponding to equation A9 in Appendix 2. The parameter space in
 432 which stable endemic steady states occurred are shown in Fig.6. In Fig. 6a-c is shown
 433 the values of I^* corresponding to values of p , c and β respectively across the range of
 434 the values in the other two parameters. The scatter represents the sensitivity to the
 435 tested parameter. Clearly, across the combination of the other parameter default
 436 values, there is a clear dependence of I^* on p , the probability that an exposed first
 437 year plant becomes an infected second year plant. The scatter only becomes apparent
 438 at high values of p . For β and c there is scatter across the range tested and the
 439 dependence is conditional on values of the other two parameters.

440

441 In the expression for the invasion criterion (Equation 8) the product pc appears, so in
 442 Fig. 6d is shown a colour contour plot of I^* against β and pc . The boundary of the
 443 steady state region is irregular because of the numerical procedures used in the
 444 calculation, but gives a good approximation to the actual parameter space enclosed.
 445 As would be expected from the invasion criterion, low values of pc and high values of
 446 β do not result in an endemic steady state for disease. The colours for values of I^*
 447 indicate a complex response surface but with a reasonably consistent pattern. In
 448 general there is an increase in value of I^* above a pc threshold of around 0.4, whereas
 449 there appears to be a slight decrease in I^* with increasing values of β .

450

451 *Relating the models to T. pratensis – P. hystereum in the PGE*

452 Applying equation 9 to the field data and interpolated points, there was a linear
453 relationship between the numbers of healthy flowering plants and the numbers of
454 flowering plants (infected and healthy) two years later (Fig 7). The residuals between
455 the observed data and predicted values based on the recurrence relationship are
456 normally distributed (mean residual is 0.0037 with standard deviations of 0.0019) and
457 do not significantly differ from each other. The regression line describes over half the
458 residual variation in the adult plant population. We recognise that this relationship
459 depends strongly on using interpolated values in the fitting of equation 9; and thus the
460 following interpretation, although informative in terms of estimation, does not refer to
461 statistical significance and should be treated with caution.

462

463 In the basic model without pathogen-induced mortality the fitted coefficients (S.E.)

464 gave an intercept $\frac{\lambda}{a(1-b)(1-d)} = 0.002$ (0.002) and gradient $\frac{1}{a(1-b)^2(1-d)} = 0.860$

465 (0.262). This gradient is less than 1 which means that the host population persists
466 ($a(1-b)^2(1-d) > 1$). Under these conditions, the net reproductive number for the

467 host plant *T. pratensis* is: $R_0 = \frac{1}{0.86} = 1.16$. Fitting the model with pathogen-induced

468 mortality (Equation 10), the greater the value of β the better the fit to observed data
469 although the estimates of the slope barely differ across this range (Table 3). As β

470 approaches 1, the number of diseased plants I approaches 0 and equation 10 reduces
471 to the recurrence relationship obtained in the absence of disease. While

472 acknowledging the caution noted above, the value of $\lambda(1-b)$ can be approximated from
473 the fitted intercepts and gradients. Assuming a default within-season mortality rate

474 ($b=0.3$) gives a very low λ value of about 0.03 suggesting little influence of seedling
475 emergence density-dependence on the host population dynamics.

476

477

478

479 **INTERPRETATION AND DISCUSSION**

480 The aim of this paper was to examine the hypothesis that *Tragopogon pratensis*,
481 described as an outbreak species in the Park Grass Experiment, is regulated by the
482 autoecious, demicyclic rust pathogen *P. hystereum* (Dodd *et al.* 1995). This was done
483 by reference to field observations for *T. pratensis* and *P. hystereum*, developing a
484 generic epidemiological framework appropriate for the life history characteristics
485 associated with this host and pathogen system, and obtaining parameter values from
486 small scale pot experiments to use in model investigations.

487

488 Although several forms of the model are presented, the model without pathogen-
489 induced mortality corresponds to Wennström's (1999) claim that in several annual
490 host-systemic pathogen systems there is little additional mortality associated with
491 disease as this would not be to the pathogen's advantage; this may also be the case for
492 a biennial or perennial host. However, systemic vascular wilt pathogens cause
493 mortality in annual hosts whereby the pathogen is able to produce either long-lived
494 spores in the dead plants or produce spores that can be aerially dispersed. In relating
495 the model outputs to the long-term data describing the outbreak dynamics of *T.*
496 *pratensis* in the PGE (Dodd *et al.* 1995), there are suggestions of outbreaks or longer
497 term cycles occurring. If this version of pathogen-induced mortality is appropriate for
498 the *T. pratensis* - *P. hystereum* system, it could be inferred that the PGE consists of a
499 medium performing host exposed to highly contagious pathogen but which has a low
500 probability of surviving the overwintering period. The rate of field mortality in *T.*
501 *pratensis* is reported as 0.5 within season and 0.88 between seasons (Mahesh,
502 Upudhyaya & Turkington 1996), which are within the range that will lead to cycling
503 in the plant population. The host population in the PGE increases and decreases over a
504 60 year period (Silvertown *et al.* 2002) which is longer than predicted in the basic
505 model; but as with the detailed observations between 1995 – 2008 of *T. pratensis*
506 there is a two year delay in the relationship between the incidence of susceptible
507 plants and the resulting incidence of infectious individuals within the longer cycles.
508 The survey data demonstrates the outbreak nature of both healthy and infected *T.*
509 *pratensis* and thus indicates that neither population reaches a high endemic steady-
510 state.

511

512 When the pathogen invasion criterion is not met there will be no endemic steady state
513 for diseased plants and the pathogen will be eliminated from the system; healthy
514 plants would then increase towards steady-state values. Additionally the model
515 replicates the expectation that a biennial host will have a two year lag relationship in
516 counts of second year plants. The derived recurrence relationship (equation 9) is of
517 the same form in the presence or absence of infected second year plants. Where
518 infected plants are present they simply substitute for healthy plants in the recurrence
519 relationship. Therefore it can be inferred that a biennial host population would not be
520 regulated by a systemic pathogen if it does not cause additional mortality of infected
521 hosts. Pathogen regulation of host dynamics may have a limited impact as
522 demonstrated by the absence of pathogen related parameters in the recurrence
523 relationship. This supports the statements of Harper (1990) and Frantzen (2007) that
524 at the population level, pathogen influence on populations may be minimal.

525

526 When considering constant pathogen induced mortality in the model ($\sigma = 0$), under
527 the majority of conditions the host population tended rapidly towards a stable
528 population (as in Fig.3a) or the infected or total host population crashed (Fig. 3b,c).
529 The exception was for the combination of medium host performance and high
530 pathogenicity, which leads to initial population cycles (Fig. 4a) which could under
531 certain time-frames be interpreted as repeated outbreaks, rather than the single
532 outbreak pattern seen in the PGE for *T. pratensis* (Fig 2a). Where there is both high
533 host performance and a highly pathogenic strain, the host will become extinct
534 (Fig.3c). However, it is unknown whether our 1995 – 2008 observations in the PGE
535 are leading to a host crash, a trough in continual repeating cycles, or a trough in a
536 population which eventually tends to a stable population. If this form of the model is
537 reflective of *T. pratensis* in the PGE, then the PGE contains a high performance host
538 population that has been exposed to a highly pathogenic strain. However, high
539 pathogenicity would not be of advantage if it leads to extinction of the host plant.

540

541 Although constant pathogen induced mortality was assumed within and between
542 seasons, other forms may be more appropriate to describe a natural host-pathogen
543 system depending on when the host population is exposed to inoculum. For example,
544 Paul & Ayres (1987) reported no additional mortality of *Senecio vulgaris* seedlings
545 infected by *P. lagenophorae*, whilst mature individuals showed increased mortality
546 and decreased growth. This suggests an additional mortality term acting on mature
547 infected individuals within a growing season and not on latently infected first year
548 individuals. Our model outputs predict that it would be advantageous for the host
549 population not to be high performing, as an introduction of a highly pathogenic strain
550 would lead to a population crash. Similarly, the most beneficial strategy for the
551 pathogen would not to be highly pathogenic, as in a low performing host population
552 the pathogen invasion criterion would not be met; and similarly, in a high
553 performance host population the host would go extinct along with the pathogen. This
554 strategy for the pathogen is also supported by the outputs where pathogen induced
555 mortality is applied within or between seasons, as highly pathogenic strains do not
556 tend to a stable population independently of host population size.

557

558 The third form of the model is for variable pathogen induced mortality. Examples of
559 where there is a reduction in pathogen-induced mortality are given by Strong (1992)
560 and Alexander (1992). *Silene alba* infected by the castrating smut *Ustilago violacea*
561 (also known as *Microbotryum violaceum*) provides evidence that smaller populations
562 have higher relative levels of infection and in turn, host pathogen-induced mortality,
563 whereas larger host populations show less signs of infection. Additionally, Alexander
564 & Antonovics (1988) and Alexander (1990) found that in the same host-pathogen
565 system, smaller populations were less likely to become infected than larger
566 populations. From these observations it could be inferred that increased host density
567 has an effect in lowering the pathogen-induced mortality rate, whilst potentially
568 enabling highly transmissible strains to develop.

569

570 Here we apply a reducing factor of the form $e^{-\sigma N}$, where N is a measure of
571 population size (MacFadyen 1963). In our case we take N to be the size of the infected

572 population I and for simplicity $\sigma = 1$ It could be the case that σ takes other non-zero
573 values; however we have no information on which to apply a different conditional
574 response and this would lead to further model elaboration. Under most parameter
575 combinations the population tends towards a stable population except where there is a
576 strain with high pathogenicity in a high performing host population, in which case the
577 population crashes. The outcome in models with variable disease-induced mortality
578 could be representative of the PGE observations of *T. pratensis* as there are dynamics
579 reminiscent of the recorded observations in all simulations with highly pathogenic
580 strains in medium or high performance host populations; these demonstrate the
581 increase and then decrease in host population numbers as described by Dodd *et al.*
582 (1995). However this prediction is made for all forms of pathogen-induced mortality
583 where there is both high host performance and high pathogenicity.

584

585 In order to assess the model, data collected from the PGE relating to healthy and rust-
586 infected *T. pratensis* were fitted to the derived recurrence relationships.
587 Acknowledging the caution we have already expressed due to the interpolated data
588 points, we note that as the value of β increases towards 1, the better fit to the data.
589 However, although increasing β in the recurrence relationship does improve the fit it
590 only marginally changes the fitted coefficients, suggesting a lack of biological
591 relevance for β as a single parameter, confirming the results of the steady state
592 analysis of the model. The results of the pot-grown *T. pratensis* experiments also
593 provided no evidence for pathogen-induced mortality under those conditions; however
594 the variable results obtained on the other parameters and the managed growing
595 environment mean that direct comparisons with field data should be made with
596 caution.

597

598 Using the estimated coefficients for the recurrence relationships and the approximate
599 parameter values in the model, it was possible to estimate $\lambda(1-b)$. Given there is a low
600 natural death rate of plants within-season (b), and also with those used in the
601 simulations, by inserting the estimates into equation 1, it shows that the seedling
602 emergence rate is not under density dependent regulation. Therefore the seedling

603 emergence density dependent term can be deleted to give $S_{t+1} = a(1-b)R_t$. Where a
604 host population is exposed to a pathogen which is highly transmissible, the outbreak
605 increase and then decrease in host population (Fig 8) similar to that seen for *T.*
606 *pratensis* in the PGE (Fig 2) can be obtained, although the numbers of plants and
607 time-scales are different. Ideally, the model would be validated with alternative
608 datasets; however there are no such long-term dataset of a biennial host plant and an
609 associated systemic, partially sterilising rust pathogen. Although the PGE (and other
610 experiments) provides long-term records for host population dynamics, there is
611 limited or no recording of infection by pathogens which prevents such analysis.
612 However, this simplified density-independent model provides some insight into the
613 dynamics of *T. pratensis* within the PGE. The outbreak (Dodd *et al.* 1995) can be
614 interpreted as being partially effected through the reduction of reproductive capacity
615 by association with the partially sterilising rust pathogen, *P. hystereum*; however it
616 cannot be concluded that pathogen regulation is the driver of such dynamics without
617 direct evidence for pathogen-induced mortality.

618

619 The model presented in this paper demonstrates the utility of mathematical models in
620 the understanding of disease epidemiology and population dynamics of fungal
621 pathogens in natural plant communities. By developing a flexible model with different
622 forms of pathogen-induced mortality it has been possible to explore the long-term
623 dynamics of a biennial host in the presence of a systemic, partially-sterilising
624 pathogen. For other natural pathosystems sharing some or all of these characteristics it
625 would be theoretically possible to analyse and predict the pathogen's impact on the
626 dynamics of the host population.

627

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632

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779

780 **APPENDICIES**

781 **Appendix 1. Derivation of the *SIR* model**

782
$$S_{\alpha,t} = \frac{aR_{\omega,t-1}}{1 + \lambda R_{\omega,t-1}} \quad (\text{A1})$$

783
$$S_{\omega,t} = (1 - b)S_{\alpha,t}e^{-cI_{\omega,t}} \quad (\text{A2})$$

784
$$E_{\alpha,t} = 0 \quad (\text{A3})$$

785
$$E_{\omega,t} = (1 - b)S_{\alpha,t} [1 - e^{-cI_{\omega,t}}] \quad (\text{A4})$$

786
$$I_{\alpha,t} = (1 - d)(1 - \beta e^{-\sigma I_{\alpha,t}})pE_{\omega,t-1} \quad (\text{A5})$$

787
$$I_{\omega,t} = (1 - b)(1 - \beta e^{-\sigma I_{\alpha,t}})I_{\alpha,t} \quad (\text{A6})$$

788
$$R_{\alpha,t} = (1 - d)[(1 - p)E_{\omega,t-1} + S_{\omega,t-1}] \quad (\text{A7})$$

789
$$R_{\omega,t} = (1 - b)R_{\alpha,t} \quad (\text{A8})$$

790

791 The subscripts α and ω refer to the beginning of season and end of season
792 respectively, and t is time.

793 By substituting in expressions to reduce the number of equations, and rearranging in
794 terms of α and scaling from $t \rightarrow t+1$, it is possible to exclude α and ω terminology,
795 and also make the equation for E obsolete as (at the beginning of the season second
796 year plants are either I (with probability p) or R (with probability of $1-p$)).

797

798 **Appendix 2. Derivation of the implicit expression for stable steady state values**

799 Where the pathogen is able to invade it is possible to obtain implicit steady-state
800 expressions for I^* by setting $I_{t+1}=I_t$ and solving (and dropping time subscripts).

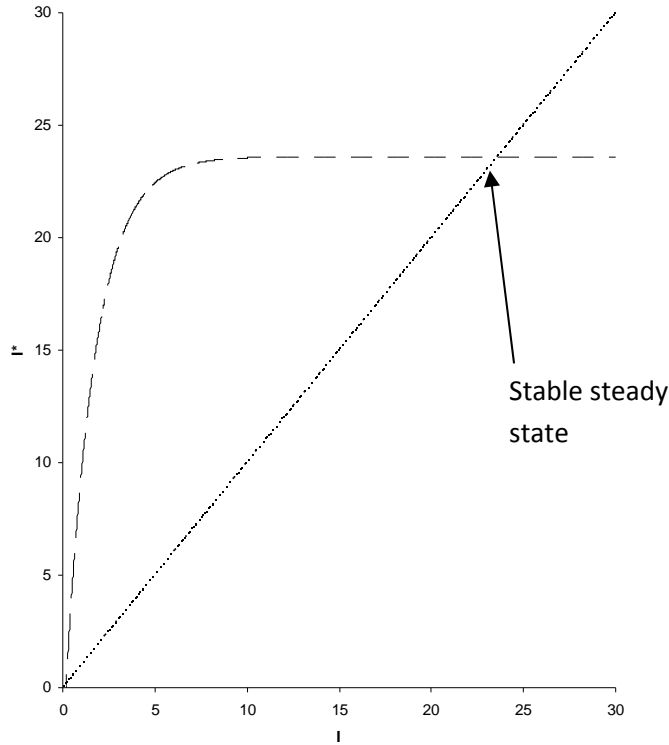
801 When pathogen-induced mortality is constant between and within seasons ($\sigma = 0$):

$$802 \quad I^* = \frac{p(1-\beta)[1 - e^{-c(1-b)(1-\beta)I^*}]}{\lambda(1-b)} \left\{ a(1-b)^2(1-d) - \frac{1}{1-p[1 - e^{-c(1-b)(1-\beta)I^*}]} \right\} \quad (\mathbf{A9})$$

803 The solutions for I^* are obtained graphically by plotting both sides of the equation for
804 given parameter values and determining the point of intersection.

805 Expressions for the other two forms of pathogen-induced mortality can be obtained in
806 a similar way.

807 An example of solving stable-state values for I^* Solutions for constant disease-
808 induced mortality between and within season, $a=30$, $b=0.3$, $c=0.99$, $d=0.3$, $p=0.9$,
809 $\lambda=0.5$, $\beta=0.1$.



810

811 **Appendix 3 Derivation of the second order recurrence relationship**

812 Rearranging equation 1 for the system without disease, a recurrence relationship is
 813 obtained that represents the relationship between individuals in sequential years:

814
$$\frac{1}{S_{t+1}} = \frac{1 + \lambda(1-b)R_t}{a(1-b)R_t} = \frac{\lambda}{a(1-b)} + \frac{1}{a(1-b)R_t} \quad (\text{A10})$$

815 Therefore there is a linear relationship between S_{t+1}^{-1} against R_t^{-1} with a gradient of

816 $\frac{1}{a(1-b)}$ and an intercept $\frac{\lambda}{a(1-b)}$. Rearranging the equation for $R_{t+1} = (1-b)(1-d)S_t$

817 in terms of S_t , rescaling to $t+1$, and substituting in equation A10 gives:

818
$$\frac{1}{R_{t+2}} = \frac{1}{a(1-b)^2(1-d)R_t} + \frac{\lambda}{a(1-b)^2(1-d)}. \quad (\text{A11})$$

819

820 In the presence of disease

821
$$I_{t+1} + R_{t+1} = S_t(1-b)(1-d) \quad (\text{A12})$$

822 Re-arranging and re-scaling to $t+1$ gives:

$$823 \quad \frac{1}{S_{t+1}} = \frac{(1-b)(1-d)}{I_{t+2} + R_{t+2}}$$

824

825 Inserting into equation A10, obtains the second-order recurrence equation:

$$826 \quad \frac{1}{I_{t+2} + R_{t+2}} = \frac{1}{a(1-b)^2(1-d)R_t} + \frac{\lambda}{a(1-b)^2(1-d)} \quad (\text{A13})$$

827 Following the same procedure a recurrence relationship for the case where there is
828 pathogen-induced mortality is obtained.

829

830

831 **FIGURES**

832 Fig 1 Schematic representations of the compartmentalised SEIR model:

833

834 Fig 2a) The population dynamics of the mean number of infected second year plants
835 of *T. pratensis* recorded in plots with manure and/or fishmeal nutrient regimes (—★—)
836 and chemical applications (—■—) demonstrating the outbreak nature of infected host
837 plants between 1995 – 2008. b) The estimated population sizes of healthy second year
838 *T. pratensis* between the years 1995 – 2008 with interpolated values for years 1999,
839 2000 and 2005.

840

841 Fig 3. Examples of simulation outcomes using the constant pathogen induced
842 mortality model demonstrating: a) healthy S, R and infected (I) plant populations
843 approach steady states monotonically for medium host performance and medium
844 pathogenicity; b) infected plants become extinct from the population for medium host
845 performance and low pathogenicity; and c) the host population becomes extinct for
846 high host performance and high pathogenicity. (—S, - - -I, ...R). Corresponding
847 parameter values for the simulations are given in Table 2.

848

849 Fig 4. Illustrations of population cycles obtained when using parameters for high
 850 pathogenicity and medium host characteristics adapting the model to include: a) no
 851 pathogen induced mortality, b) constant pathogen disease induced mortality. c)
 852 variable pathogen induced mortality ($\text{---}S$, $\text{- - -}I$, $\dots R$). Corresponding parameter
 853 values for the simulations are given in Table 2.

854

855 Fig 5. The influence of altering β , S and the product pc on the invasion criterion. For
 856 simplicity $b=d$ at a default value of 0.3.

857

858 Fig 6. Values of I^* for varying values of a) p b) c and c) β . d) demonstrates a coloured
 859 contour plot demonstrating the region of steady-states and values for corresponding pc
 860 and β .

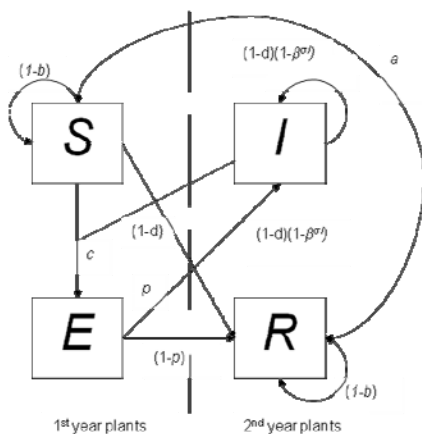
861

862 Fig. 7. The recurrence relationship fitted to observed data with the interpolated points
 863 (\diamond) for 1999 and 2000 indicating a linear inverse relationship between the number of
 864 healthy second year individuals (R_t) and the number of healthy and infected second
 865 year individuals two years later ($R_{t+2}+I_{t+2}$)

866

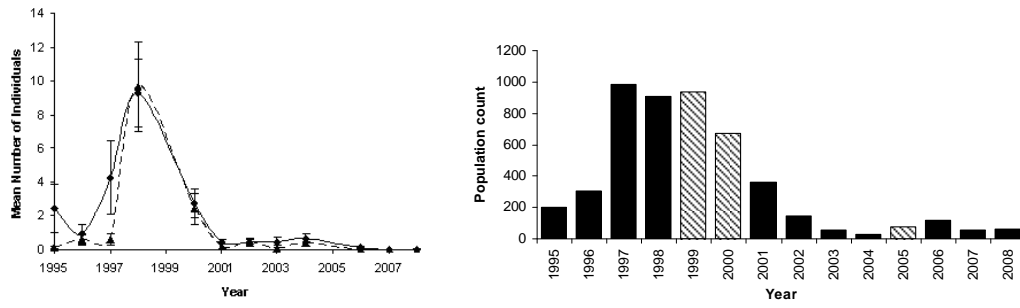
867 Fig. 8. Simulation outcomes under high pathogenicity and low host performance
 868 without pathogen-induced mortality or seedling emergence density-dependency,
 869 producing an outcome similar to an “outbreak” dynamic ($\text{---}S$, $\text{- - -}I$, $\dots R$)

870



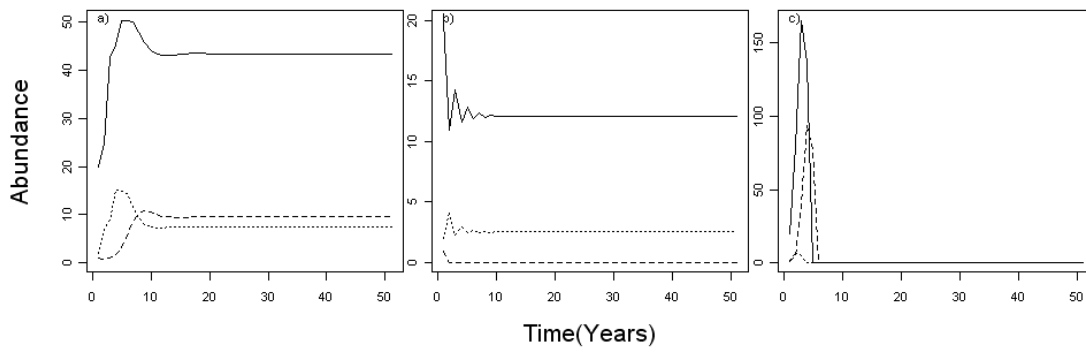
871

872 Fig. 1.



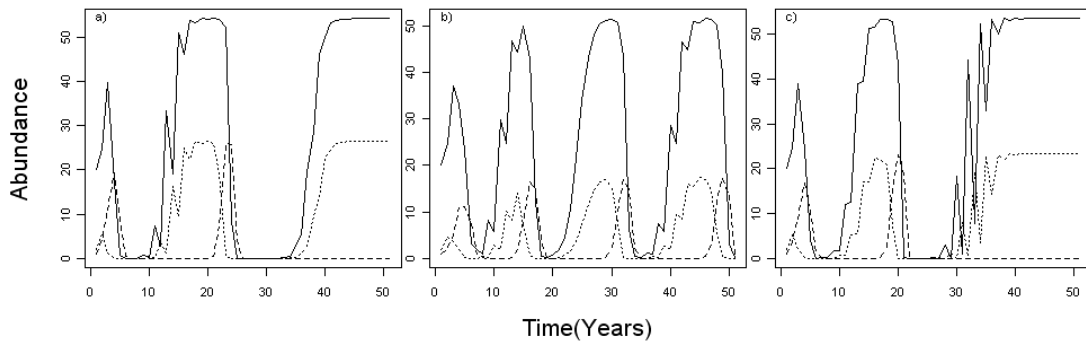
873

874 Fig. 2



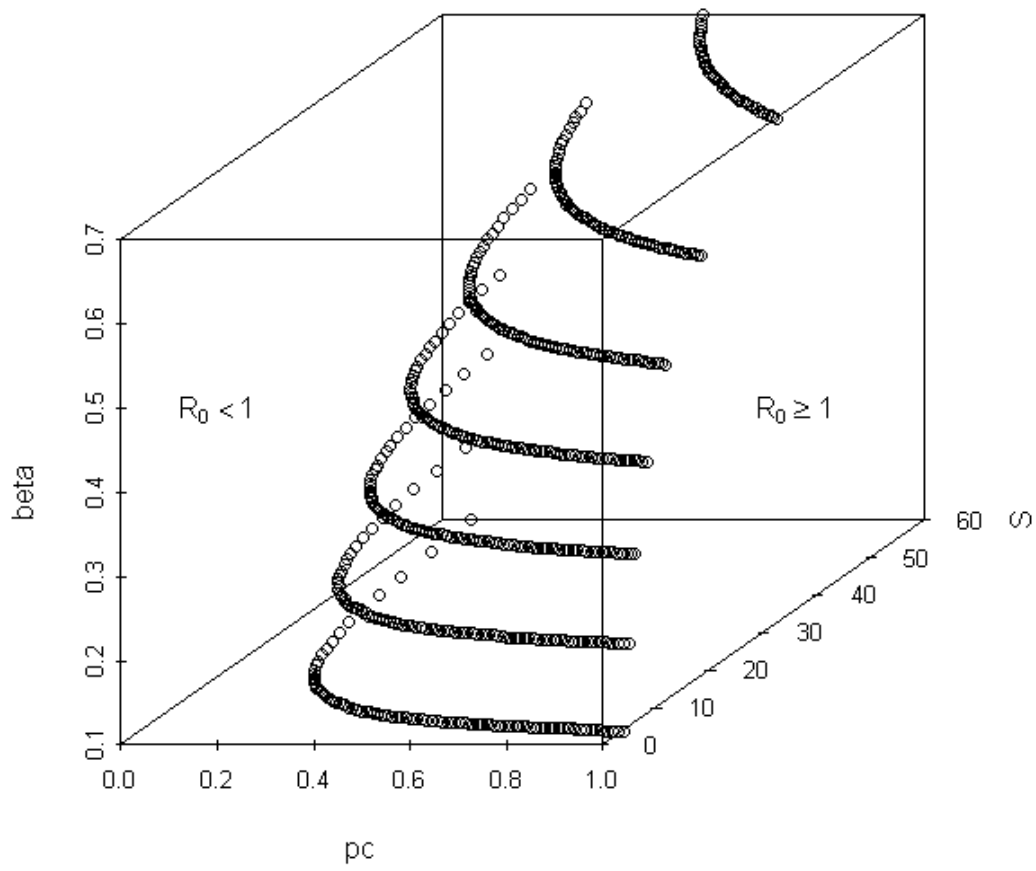
875 Fig. 3

876

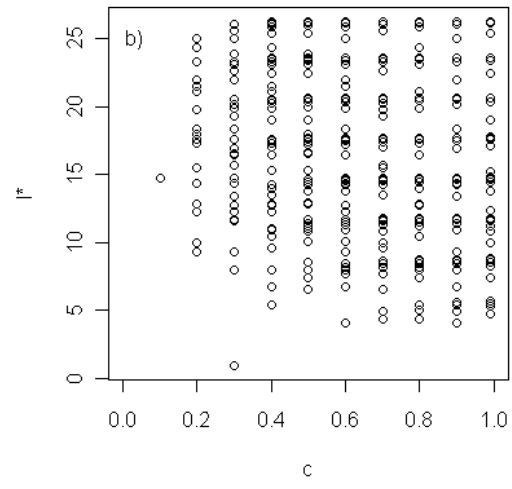
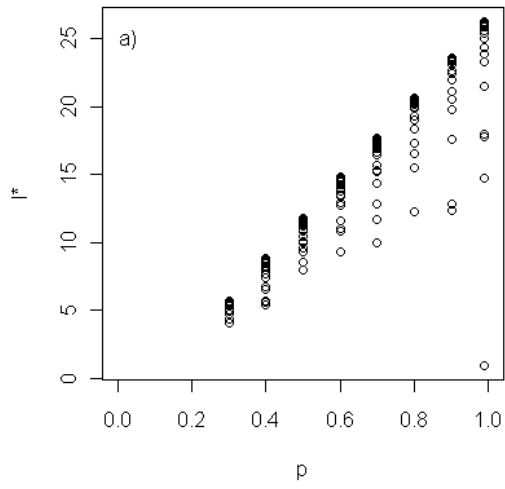


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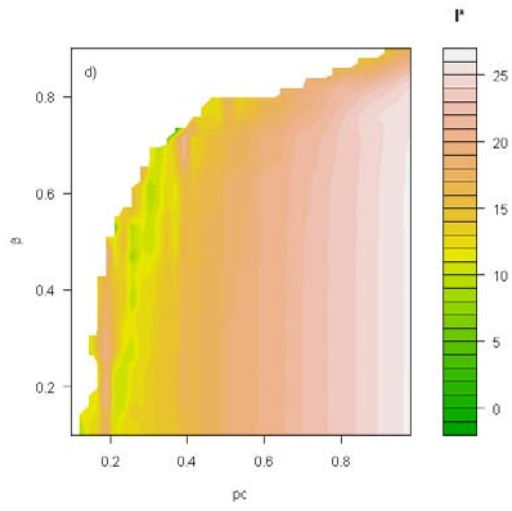
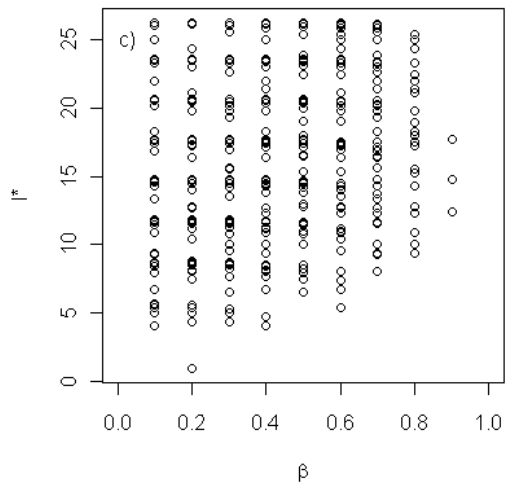
878 Fig. 4



879
880 **Fig. 5**

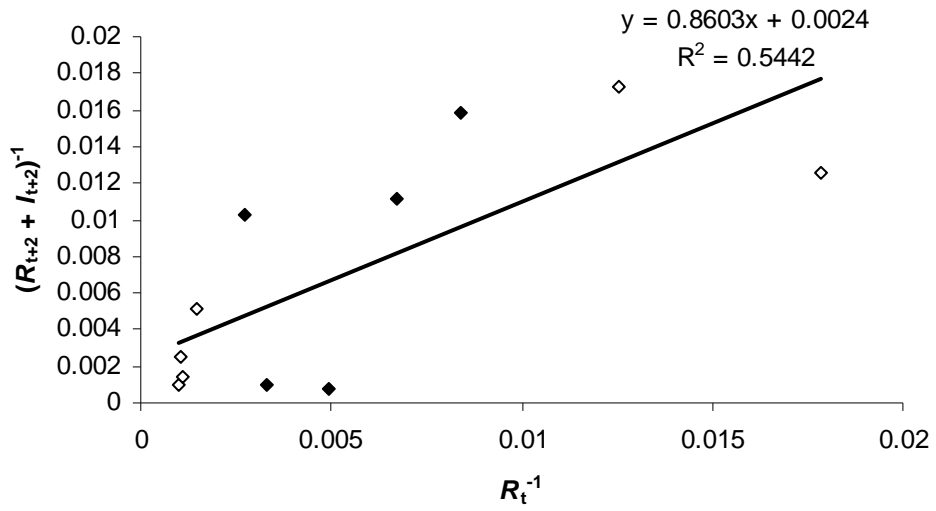


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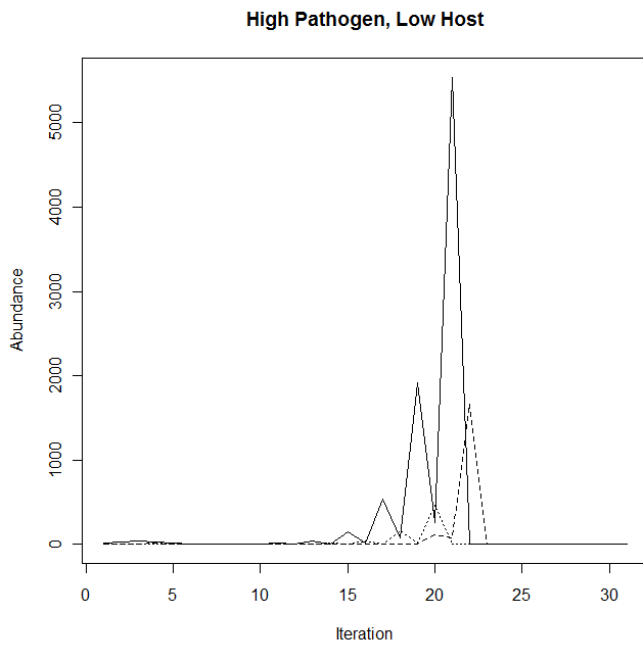
883 **Fig. 6**



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885 **Fig. 7**

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888 **Fig. 8**

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894 Table 1. Parameters and their value ranges used to assess the model system

Parameter	Explanation	Default value	Source	Range Investigated
S_0	Initial number of 1 st year susceptible individuals.	20	PGE survey	
E_0	Initial number of exposed 1 st year individuals.	0	PGE survey	
I_0	Initial number of Infectious 2 nd year individuals.	1	PGE survey	
R_0	Initial number of non-infectious 2 nd year individuals.	2	PGE survey	
a	Seedling recruitment per non-infectious 2 nd year individuals	30	<i>T. pratensis</i> seed set mean of 26.7 (Salama <i>et al.</i> 2010)	20 – 60
b	Within-season mortality rate	0.3	0.5 reported for <i>T. pratensis</i> (Mahesh, Upudhyaya & Turkington, 1996)	0.1 – 0.8
d	Between-season mortality rate	0.3	0.88 reported for <i>T. pratensis</i> (Mahesh, Upudhyaya & Turkington,	0.1 – 0.6

<i>But c</i>	Transmission probability	rate	0.3	1996) Variable depending on temperature for <i>P. lagenophorae</i> (Kolnaar & Van den Bosch, 2001)	0.1 – 0.8
<i>p</i>	Probability of exposed individuals becoming infectious		0.7	Greenhouse trials indicate a maximum of 18% of inoculated plants become infectious, however note there is no evidence that inoculated plants had sufficient exposure for pathogen uptake.	0.3 – 1.0
λ	Density-dependent parameter		0.5	PGE survey	0.2 – 1.0

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899

900 **Table 2. Parameter ranges for low, medium and high host performance and**
 901 **pathogenicity parameters. The pathogenicity parameters relate to the biology of**
 902 **the pathogen and its relationship with the host, whilst host performance is life-**
 903 **history parameters that are independent of pathogen presence**

904

	Low	Medium	High
Pathogen			
c	0.1	0.3	0.8
p	0.3	0.7	1.0
β	0.1	0.2	0.3
Host			
a	20	30	60
b	0.4	0.3	0.1
d	0.5	0.3	0.1
λ	1.0	0.5	0.2

916

917 **Table 3. Summary of regression analysis of the recurrence relationship derived**
 918 **from the pathogen-induced mortality between and within season or only between**
 919 **season model forms with varying β values. (AIC: Akaike's information criterion,**
 920 **m : gradient,)**

β	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
R^2	0.56	0.58	0.59	0.61	0.62	0.64	0.66	0.68	0.71
AIC	-56.3	-56.4	-56.5	-56.6	-56.7	-56.9	-57.0	-57.2	-57.5
m	0.86	0.87	0.87	0.88	0.89	0.90	0.91	0.93	0.95

921

922