

## Effect of CO<sub>2</sub> laser cutting process parameters on edge quality and operating cost of AISI316L

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### ABSTRACT

Laser cutting is a popular manufacturing process utilized to cut various types of materials economically. The width of laser cut or kerf, quality of the cut edges and the operating cost are affected by laser power, cutting speed, assist gas pressure, nozzle diameter and focus point position as well as the work-piece material. In this paper CO<sub>2</sub> laser cutting of stainless steel of medical grade AISI316L has been investigated. Design of experiment (DOE) was implemented by applying Box-Behnken design to develop the experiment lay-out. The aim of this work is to relate the cutting edge quality parameters namely: upper kerf, lower kerf, the ratio between them, cut section roughness and operating cost to the process parameters mentioned above. Then, an overall optimization routine was applied to find out the optimal cutting setting that would enhance the quality or minimize the operating cost. Mathematical models were developed to determine the relationship between the process parameters and the edge quality features. Also, process parameters effects on the quality features have been defined. Finally, the optimal laser cutting conditions have been found at which the highest quality or minimum cost can be achieved.

KEYWORDS: CO<sub>2</sub> laser cutting, AISI316L, optimization.

### 1- INTRODUCTION

Laser beam cutting (LBC) process has a wide range of applications in different manufacturing processes in industry due to its advantages of high cut quality and cost effectiveness through mass-production rate [1]. The material to be cut is locally melted by the focused laser beam. The melt is then blown away with the aid of assist gas, which flow coaxially with the laser beam, forming a kerf. In metal cutting procedures, different types of assist gases

are used such as oxygen and nitrogen. The selection of an appropriate gas type or a mixture of gases with a given mixing percentage is fundamental to minimize the cutting cost by increasing the cutting speed [1-2]. Changing the assist gas composition and its effect on laser cutting of 3 mm mild steel has been studied by Chen [3]. The gas mixtures used were composed of oxygen, argon, nitrogen and helium. He reported that using oxygen with high purity along with laser power of 1500 W is required for high performance laser cutting for this material. Ghany and Newishy [4] have investigated the effect of pulsed and continuous wave (CW) Nd-YAG laser cutting of austenitic stainless steel sheets using nitrogen or oxygen as an assist gas. It was shown that the laser cutting quality depends mainly on the laser power, pulse frequency, cutting speed and focus position. Compared to oxygen, nitrogen produced a brighter and smoother cut surface with smaller kerf, although it did not prove to be economical. The effect of varying the process input parameters on the quality characteristics such as kerf width and its variation along the cut was the interest of many studies. Chen [5] has investigated CO<sub>2</sub> laser cutting of 3 mm-thick mild steel sheet. It was reported that as the laser power increases and cutting speed decreases the kerf width increases. He also observed that oxygen or air leads to wider kerf, however, a narrow kerf could be obtained by using inert gas as an assist gas. The same variation in the kerf width with cutting speed, laser power, and type of gas and pressure has been found by Ghany and Newishy in their experiment [4]. Uslan [6] has found that increasing the laser power intensity enhances the kerf width size and this is more pronounced with reducing cutting speed. It was reported that a small variation in laser power results in a large variation in the kerf size. He reported that the influence of cutting speed less than that corresponding to the laser power. Also, he mentioned that by using defocused laser beam, which in retrain reduces the laser power density, would increase the kerf width size. Yilbas [7] has mentioned that increasing laser power and energy coupling factor increase the kerf width size. Also, he reported that any increase in the cutting speed reduces the kerf width. It was found that the laser power has a highly significant effect on the kerf size. Yilbas [8] reported that increasing laser beam scanning speed reduces the kerf width, while the kerf width increases with increasing laser power. It was reported that the main effects of all the parameters employed have a significant influence on the cut quality. Dilthey et al. [9] have mentioned that when cutting stainless steel, exact adjustment of focus position and gas jet is essential in order to obtain dross free cutting. Also, they reported that the corrosion resistance is at risk when cutting stainless steel with oxygen but the cutting speed is high or vice

versa when cutting stainless steel using inert gas. Yilbas and Rashid [10] have monitored the dross ejection from the kerf, the frequency of the dross ejection correlated with the striation frequency and out of flatness. It was mentioned that the cutting speed and thickness have a significant effect on the out of flatness. They indicated that the cut quality can be improved by varying the combination of pulse frequency and output intensity. Radovanovic and Dasic [11] have observed that the surface roughness increases along with the sheet thickness, but decreases with increasing the laser power when cutting mild steel. Neimeyer et al. [12] have indicated that the average surface roughness may be best at high cutting speed and low assist gas pressure. They confirmed that the workpiece thickness showed little effect on the cut surface quality. It was concluded that the profiles of the cut surface of the top and bottom edges yield the same values for average surface roughness, despite the significant visual difference in the striation pattern.

In order to obtain the desirable high level of cutting edge quality it is important to choose the optimal combinations of the process parameters as these parameters have an effect on the output characteristics or quality features namely: upper kerf, lower kerf and cutting edge roughness etc. In this case, a systematic study based on Design of experiment (DOE) is required to find out the functional relationship between the output characteristics and the process input parameters with the minimum number of experiments. Several investigations were performed using systematic approaches to optimize the LBC process. Dubey and Yadava [13] have applied Taguchi method and RSM to optimize the LBC process of thin sheet of high silicon-alloy steel, taking into account multi-performance characteristics. Also, the same authors [14] have applied Taguchi method to investigate the effect of LBC process parameters on the kerf width, kerf deviation and kerf taper when cutting nickel-based super-alloy sheets. Their aim was to optimize the process. Yilbas [15] has reported the effect of cutting parameters on kerf size variations of thick sheet metals. He proposed a factorial analysis to identify the main effects and interactions of the parameters. It is found that laser output power and oxygen gas pressure have significant effect on the percentage of kerf width variation. Eltawahni et al. [16, 17 and 18] have applied RSM to investigated and optimize the LBC of ultrahigh molecular weight polyethylene, medium density fibreboard and Polymethyl-methacrylate. They concluded that the higher cutting speed does not always improve the efficiency of the LBC. Finally they presented the optimal cutting conditions for both economical and high quality cut. Other researchers have highlighted the importance of modelling and optimizing the laser cutting process for different materials [19-21].

Thus, the aim of this paper is to apply RSM to develop mathematical models to predict the width of upper kerf, lower kerf, the ratio between the upper and lower kerfs, cut section roughness and operating cost for CW CO<sub>2</sub> laser cutting of AISI316 austenitic stainless steel. The second aim is to use the developed models to optimize the cutting operation. The laser cutting input parameters taken into consideration are laser power (A), cutting speed (B), focal point position (C), gas pressure (D) and nozzle diameter (E).

## 2. EXPERIMENTAL DESIGN

The experiment was designed based on a three level Box-Behnken design with full replication [22 and 23]. Laser power (1 - 1.5 kW), cutting speed (1000 - 3000 mm/min), focal point position (-4 to -2 mm), nitrogen pressure (10 – 15 bar) and nozzle diameter (1, 1.5 and 2 mm) are the process input parameters. Table 1 shows LBC parameters and experimental design levels used. RSM was applied to the experimental data using statistical software, Design-Expert V7. Second order polynomials were fitted to the experimental data to obtain the regression equations. The sequential F-test, lack-of-fit test and other adequacy measures were used to select the best fit. A step-wise regression method was used to fit the second order polynomial Eq. 1 to the experimental data and to find the significant model terms [23, 24]. The same statistical software was used to generate the statistical and response plots as well as the optimization.

$$Y = b_o + \sum b_i \chi_i + \sum b_{ii} \chi_{ii}^2 + \sum b_{ij} \chi_i \chi_j \quad (1)$$

Table 1: Process variables and experimental design levels used.

| Parameter            | Code | Unit   | -1   | 0    | +1   |
|----------------------|------|--------|------|------|------|
| Laser power          | A    | kW     | 1    | 1.25 | 1.5  |
| Cutting speed        | B    | mm/min | 1000 | 2000 | 3000 |
| Focal point position | C    | mm     | -4   | -3   | -2   |
| Nitrogen pressure    | D    | Bar    | 10   | 12.5 | 15   |
| Nozzle diameter*     | E    | mm     | 1    | 1.5  | 2    |

\* Categorical factor.

### **3. EXPERIMENTAL WORK**

#### **3.1 Laser Cutting**

Austenitic stainless steel in sheet form of standard grade of AISI316L was used as workpiece material. The sheet dimensions were 500 x 500 mm with thickness of 2 mm. Trial runs of laser cutting were performed by varying one of the process factors at-a-time to determine the range of each factor. Full cut, keeping the kerf width, cutting edge striations and dross to a minimum; were the criteria of selecting the working ranges. The main experiment was performed according to the design matrix in a random order to avoid any systematic error. A CW 1.5 kW CO<sub>2</sub> Rofin laser provided by Mechtronic Industries Ltd and a focusing lens with focal length of 127 mm were used to perform the cut. Nitrogen gas was supplied coaxially as an assist gas with different pressures. Specimens were cut from the plate for each condition. The specimen shape was designed in order to allow the measurement of the responses in a precise and easy way. The upper and lower kerf widths were measured using an optical microscope which has an accuracy of 0.001 and allows measurements in both the x-axis and y-axis directions. The average of five measurements of both kerf widths was recorded for all runs. The ratio of the upper kerf to the lower kerf was calculated for each run using the averaged data. The arithmetic average roughness parameter,  $R_a$ , values were measured using a surface roughness tester model TR-200. Five consistent surface roughness values of each specimen were measured at the centre of the cut surface and an average was calculated for each specimen. The design matrix and the average measured responses are shown in Table 2 and 3.

Table 2: Design matrix.

| <b>Factors</b> |            |                  |                      |                  |                   |                  |
|----------------|------------|------------------|----------------------|------------------|-------------------|------------------|
| <b>Std</b>     | <b>Run</b> | <b>A,<br/>kW</b> | <b>B,<br/>mm/min</b> | <b>C,<br/>mm</b> | <b>D,<br/>Bar</b> | <b>E,<br/>mm</b> |
| 1              | 21         | 1                | 1000                 | -3               | 12.5              | 1.5              |
| 2              | 33         | 1.5              | 1000                 | -3               | 12.5              | 1.5              |
| 3              | 41         | 1                | 3000                 | -3               | 12.5              | 1.5              |
| 4              | 45         | 1.5              | 3000                 | -3               | 12.5              | 1.5              |
| 5              | 40         | 1.25             | 2000                 | -4               | 10                | 1.5              |
| 6              | 23         | 1.25             | 2000                 | -2               | 10                | 1.5              |
| 7              | 5          | 1.25             | 2000                 | -4               | 15                | 1.5              |
| 8              | 25         | 1.25             | 2000                 | -2               | 15                | 1.5              |
| 9              | 2          | 1.25             | 1000                 | -3               | 12.5              | 1                |
| 10             | 34         | 1.25             | 3000                 | -3               | 12.5              | 1                |
| 11             | 1          | 1.25             | 1000                 | -3               | 12.5              | 2                |
| 12             | 19         | 1.25             | 3000                 | -3               | 12.5              | 2                |
| 13             | 17         | 1                | 2000                 | -4               | 12.5              | 1.5              |
| 14             | 24         | 1.5              | 2000                 | -4               | 12.5              | 1.5              |
| 15             | 18         | 1                | 2000                 | -2               | 12.5              | 1.5              |
| 16             | 8          | 1.5              | 2000                 | -2               | 12.5              | 1.5              |
| 17             | 7          | 1.25             | 2000                 | -3               | 10                | 1                |
| 18             | 6          | 1.25             | 2000                 | -3               | 15                | 1                |
| 19             | 15         | 1.25             | 2000                 | -3               | 10                | 2                |
| 20             | 12         | 1.25             | 2000                 | -3               | 15                | 2                |
| 21             | 39         | 1.25             | 1000                 | -4               | 12.5              | 1.5              |
| 22             | 30         | 1.25             | 3000                 | -4               | 12.5              | 1.5              |
| 23             | 20         | 1.25             | 1000                 | -2               | 12.5              | 1.5              |
| 24             | 36         | 1.25             | 3000                 | -2               | 12.5              | 1.5              |
| 25             | 3          | 1                | 2000                 | -3               | 10                | 1.5              |
| 26             | 46         | 1.5              | 2000                 | -3               | 10                | 1.5              |
| 27             | 4          | 1                | 2000                 | -3               | 15                | 1.5              |
| 28             | 28         | 1.5              | 2000                 | -3               | 15                | 1.5              |
| 29             | 38         | 1.25             | 2000                 | -4               | 12.5              | 1                |
| 30             | 29         | 1.25             | 2000                 | -2               | 12.5              | 1                |
| 31             | 27         | 1.25             | 2000                 | -4               | 12.5              | 2                |
| 32             | 11         | 1.25             | 2000                 | -2               | 12.5              | 2                |
| 33             | 13         | 1                | 2000                 | -3               | 12.5              | 1                |
| 34             | 16         | 1.5              | 2000                 | -3               | 12.5              | 1                |
| 35             | 37         | 1                | 2000                 | -3               | 12.5              | 2                |
| 36             | 42         | 1.5              | 2000                 | -3               | 12.5              | 2                |
| 37             | 10         | 1.25             | 1000                 | -3               | 10                | 1.5              |
| 38             | 9          | 1.25             | 3000                 | -3               | 10                | 1.5              |
| 39             | 14         | 1.25             | 1000                 | -3               | 15                | 1.5              |
| 40             | 26         | 1.25             | 3000                 | -3               | 15                | 1.5              |
| 41             | 43         | 1.25             | 2000                 | -3               | 12.5              | 1.5              |
| 42             | 35         | 1.25             | 2000                 | -3               | 12.5              | 1.5              |
| 43             | 32         | 1.25             | 2000                 | -3               | 12.5              | 1.5              |
| 44             | 22         | 1.25             | 2000                 | -3               | 12.5              | 1.5              |
| 45             | 31         | 1.25             | 2000                 | -3               | 12.5              | 1.5              |
| 46             | 44         | 1.25             | 2000                 | -3               | 12.5              | 1.5              |

Table 3: Average of experimentally measured responses for AISI316L.

| No. | upper kerf, mm | Lower kerf, mm | Ratio | Ra, $\mu\text{m}$ | Operating cost, €/m |
|-----|----------------|----------------|-------|-------------------|---------------------|
| 1   | 0.296          | 0.203          | 1.461 | 0.792             | 2.8921              |
| 2   | 0.325          | 0.227          | 1.435 | 0.732             | 2.9056              |
| 3   | 0.222          | 0.147          | 1.512 | 1.648             | 0.9640              |
| 4   | 0.241          | 0.216          | 1.119 | 0.804             | 0.9685              |
| 5   | 0.263          | 0.183          | 1.435 | 1.735             | 1.1890              |
| 6   | 0.221          | 0.224          | 0.988 | 0.394             | 1.1890              |
| 7   | 0.293          | 0.218          | 1.348 | 2.161             | 1.7099              |
| 8   | 0.265          | 0.157          | 1.688 | 0.693             | 1.7099              |
| 9   | 0.300          | 0.233          | 1.288 | 0.967             | 1.3360              |
| 10  | 0.194          | 0.145          | 1.341 | 0.734             | 0.4453              |
| 11  | 0.321          | 0.191          | 1.685 | 0.870             | 5.0868              |
| 12  | 0.223          | 0.167          | 1.337 | 0.814             | 1.6956              |
| 13  | 0.264          | 0.184          | 1.430 | 1.633             | 1.4461              |
| 14  | 0.307          | 0.212          | 1.450 | 0.910             | 1.4528              |
| 15  | 0.196          | 0.206          | 0.952 | 0.665             | 1.4461              |
| 16  | 0.231          | 0.245          | 0.940 | 0.409             | 1.4528              |
| 17  | 0.196          | 0.147          | 1.333 | 0.556             | 0.5522              |
| 18  | 0.264          | 0.209          | 1.265 | 0.610             | 0.7838              |
| 19  | 0.254          | 0.171          | 1.488 | 0.633             | 2.0803              |
| 20  | 0.289          | 0.190          | 1.521 | 0.490             | 3.0065              |
| 21  | 0.321          | 0.246          | 1.304 | 0.733             | 2.8988              |
| 22  | 0.250          | 0.182          | 1.371 | 1.039             | 0.9663              |
| 23  | 0.309          | 0.258          | 1.199 | 0.781             | 2.8988              |
| 24  | 0.180          | 0.173          | 1.042 | 0.578             | 0.9663              |
| 25  | 0.197          | 0.162          | 1.216 | 1.033             | 1.1856              |
| 26  | 0.235          | 0.188          | 1.246 | 0.481             | 1.1923              |
| 27  | 0.251          | 0.155          | 1.625 | 0.835             | 1.7065              |
| 28  | 0.314          | 0.192          | 1.634 | 0.449             | 1.7133              |
| 29  | 0.268          | 0.182          | 1.470 | 0.942             | 0.6680              |
| 30  | 0.242          | 0.216          | 1.122 | 0.620             | 0.6680              |
| 31  | 0.305          | 0.200          | 1.523 | 0.582             | 2.5434              |
| 32  | 0.263          | 0.230          | 1.145 | 0.744             | 2.5434              |
| 33  | 0.237          | 0.171          | 1.384 | 0.755             | 0.6646              |
| 34  | 0.281          | 0.186          | 1.511 | 0.634             | 0.6714              |
| 35  | 0.272          | 0.197          | 1.377 | 0.697             | 2.5400              |
| 36  | 0.303          | 0.186          | 1.630 | 0.522             | 2.5468              |
| 37  | 0.315          | 0.180          | 1.750 | 1.211             | 2.3779              |
| 38  | 0.211          | 0.174          | 1.213 | 0.743             | 0.7926              |
| 39  | 0.350          | 0.246          | 1.419 | 0.883             | 3.4198              |
| 40  | 0.264          | 0.159          | 1.659 | 0.479             | 1.1399              |
| 41  | 0.325          | 0.168          | 1.935 | 0.757             | 1.4494              |
| 42  | 0.312          | 0.167          | 1.863 | 0.613             | 1.4494              |
| 43  | 0.289          | 0.161          | 1.797 | 0.561             | 1.4494              |
| 44  | 0.301          | 0.174          | 1.735 | 0.694             | 1.4494              |
| 45  | 0.302          | 0.171          | 1.763 | 0.601             | 1.4494              |
| 46  | 0.297          | 0.193          | 1.539 | 0.683             | 1.4494              |

### 3.2 Estimating the Operating Cost

Laser cutting operating costs can be estimated as cutting per hour or per unit length. The laser system used in this work utilized CO<sub>2</sub> using a static volume of laser gases of approximately 7.5 litre every 72 hours. For this laser system with 1.5 kW maximum outputs power the operating costs generally falls into the categories listed in Table 4. The operating cost calculation does not account for any unscheduled breakdown and maintenance, such as a breakdown in the table motion controller or PC hard disc replacement [17]. The total approximated operating cost per hour as a function of process parameters can be estimated by  $2.654+1.376xP + 9.60x10^{-3}xF$ . However, the total approximated operating cost per unit length of the cut is given by Eq. 1, assuming 85% utilization. Eq. 2 was used to calculate the cutting cost per meter for all samples.

Table 4: Operating costs break down when nitrogen is used.

| Element of cost                    | Calculations                                                                                                 | Cutting cost €/hr                       |
|------------------------------------|--------------------------------------------------------------------------------------------------------------|-----------------------------------------|
| Laser electrical power             | $(20.88 \text{ kVA})(0.8 \text{ pf})(\text{€}0.12359/\text{kWhr}) \times (P/1.5)$                            | 1.376xP                                 |
| Chiller electrical power           | $(11.52 \text{ kVA})(0.8 \text{ pf})(\text{€} 0.12359/\text{kWhr})$                                          | 1.139                                   |
| Motion controller power            | $(4.8 \text{ kVA})(0.8 \text{ pf})(\text{€} 0.12359/\text{kWhr})$                                            | 0.475                                   |
| Exhaust system power               | $(0.9 \text{ kWhr})(\text{€} 0.12359/\text{kWhr})$                                                           | 0.111                                   |
| Laser gas LASPUR208                | $\{(\text{€}1043.93/ \text{bottle})/(1500\text{litre}/\text{bottle})\} \times 7.5 \text{ litre}/72\text{hr}$ | 0.072                                   |
| Gas bottle rental                  | $(\text{€}181.37/720\text{hr})$                                                                              | 0.252                                   |
| Chiller additives                  | $(\text{€}284.80/\text{year})/(8760 \text{ hr}/\text{year})$                                                 | 0.033                                   |
| Compressed nitrogen                | $\text{€}9.60 \times 10^{-3}/\text{litre} \times F[\text{litre}/\text{hr}]$                                  | $9.60 \times 10^{-3} \times F$          |
| Nozzle tip                         | $(\text{€}7.20/200\text{hr})$                                                                                | 0.036                                   |
| Exhaust system filters             | $(\text{€}5/100\text{hr})$                                                                                   | 0.05                                    |
| Focus lens                         | $(\text{€}186/\text{lens})/(1000\text{hr})$                                                                  | 0.186                                   |
| Maintenance labour (with overhead) | $(12 \text{ hr}/2000\text{hrs operation})(\text{€}50/\text{hr})$                                             | 0.30                                    |
| Total operation cost per hour      |                                                                                                              | $2.654+1.376xP + 9.60 \times 10^{-3}xF$ |

$$\text{Cutting cost}[\text{Euro}/\text{m}] = \frac{2.654 + 1.376 \times P [\text{kW}] + 9.60 \times 10^{-3} \times F[\text{l}/\text{hr}]}{(0.85) \times S[\text{mm}/\text{min}][60\text{min}/\text{hr}][\text{m}/1000\text{mm}]} \quad (1)$$

$$\text{cutting cost}[\text{Euro}/\text{m}] = \frac{2.654 + 1.376 \times P + 9.60 \times 10^{-3} \times F}{0.051 \times S} \quad (2)$$

Where

P: used out put power in kW.

F: flow rate in l/hr.

S: cutting speed in mm/min.



The compressed nitrogen will flow in a supersonic manner within the pressure range used in this work. Consequently, the flow rate in [l/hr] of this fluid through a nozzle can be easily calculated from Eq. 3 [1].

$$\text{Flow Rate [l/hr]} = F = 492 \times d^2 (p_g + 1) \quad (3)$$

**Where:**

$d$ : Nozzle diameter [mm].

$P_g$ : Nozzle supply pressure [bar].

## **4. Results and Discussion**

### **4.1 Analysis of Variance**

Design expert software V7 was used to analyze the measured responses. The fit summary output indicates that for all responses, the quadratic models are statistically recommended for further analysis as they have the maximum predicted and adjusted  $R^2$  [23 and 24]. The test for significance of the regression models, the test for significance on individual model coefficients and the lack of fit test were performed using the same statistical package for all responses. By selecting the step-wise regression method, the insignificant model terms can be automatically eliminated. The resulting ANOVA tables (Tables 5 to 9) for the reduced quadratic models outline the analysis of variance for each response and illustrate the significant model terms. The same tables show also the other adequacy measures  $R^2$ , Adjusted  $R^2$  and Predicted  $R^2$ .

The entire adequacy measures are close to 1 which are in reasonable agreement and indicates adequate models [16, 17 and 24]. The adequate precision compares the range of the predicted value at the design points to the average prediction error. In all cases the values of adequate precision ratios are dramatically greater than 4. An adequate precision ratio above 4 indicates that the model is adequate [23 and 25]. An adequate model means that the reduced model has successfully passed all the required statistical tests and can be used to predict the responses or to optimize the process etc.

For the upper kerf model the analysis of variance indicates that the main effect of all the following factors, quadratic effect of laser power ( $A^2$ ), cutting speed ( $B^2$ ), focal position ( $C^2$ ) and nitrogen pressure ( $D^2$ ) are the most significant model terms associated with this response. However, the interaction effect between cutting speed and nitrogen pressure (BC) is also affecting this response. While, for the lower kerf model, the analysis indicates that the main

effect of all factors, the quadratic effect of ( $A^2$ ), ( $B^2$ ), ( $C^2$ ) and the interaction effect between (AE), (BD), (BE), (CD) and (DE) are the significant model terms. The analysis demonstrates that the cutting speed has the main role on the lower kerf width, then the laser power. For the ratio model, the analysis demonstrates that, the main effect of all the following factors, the quadratic effect of ( $A^2$ ), ( $B^2$ ), ( $C^2$ ), ( $D^2$ ) and the interaction effect between (BD) and (CD) are the significant model terms. All the findings for kerf width are in agreement with the results reported in [4, 7, 8 and 9]. Then, for the roughness model, it is evident from the analysis that the main effect of the laser power (A), cutting speed (B), focal point position (C), nitrogen pressure (D), the quadratic effects of cutting speed ( $B^2$ ), focal position ( $C^2$ ) and nitrogen pressure ( $D^2$ ) are the significant terms. However, cutting speed is the factor which has the most significant effect on the roughness a funding which agrees with [11]. The focal position and laser power also affect the roughness notably. All the above findings are in agreement with the results found in [11]. Finally, for the operating cost model the results demonstrate that the main effect of laser power (A), cutting speed (B), nitrogen pressure (D), nozzle diameter (E), the interaction effects of laser power with nitrogen pressure (AD), laser power with nozzle diameter (AE), nitrogen pressure with nozzle diameter (DE), the quadratic effect of cutting speed ( $B^2$ ) and nitrogen pressure ( $D^2$ ) are the significant model terms related to operating cost. The final mathematical models in terms of actual factors as determined by design expert software are shown in Eqs 4-18:

Table 5: ANOVA table for upper kerf width reduced quadratic model.

| Source            | Sum of Squares | DF | Mean Square               | F Value | Prob > F |             |
|-------------------|----------------|----|---------------------------|---------|----------|-------------|
| Model             | 0.0741         | 11 | 0.0067                    | 31.060  | < 0.0001 | Significant |
| A                 | 0.0057         | 1  | 0.0057                    | 26.297  | < 0.0001 |             |
| B                 | 0.0353         | 1  | 0.0353                    | 162.761 | < 0.0001 |             |
| C                 | 0.0083         | 1  | 0.0083                    | 38.202  | < 0.0001 |             |
| D                 | 0.0100         | 1  | 0.0100                    | 46.132  | < 0.0001 |             |
| E                 | 0.0076         | 2  | 0.0038                    | 17.493  | < 0.0001 |             |
| BC                | 0.0008         | 1  | 0.0008                    | 3.835   | 0.0584   |             |
| $A^2$             | 0.0050         | 1  | 0.0050                    | 23.150  | < 0.0001 |             |
| $B^2$             | 0.0011         | 1  | 0.0011                    | 5.203   | 0.0289   |             |
| $C^2$             | 0.0048         | 1  | 0.0048                    | 22.195  | < 0.0001 |             |
| $D^2$             | 0.0047         | 1  | 0.0047                    | 21.465  | < 0.0001 |             |
| Residual          | 0.0074         | 34 | 0.0002                    |         |          |             |
| Lack of Fit       | 0.0066         | 29 | 0.0002                    | 1.469   | 0.3583   | Not Sig.    |
| Pure Error        | 0.0008         | 5  | 0.0002                    |         |          |             |
| Cor Total         | 0.0814         | 45 |                           |         |          |             |
| $R^2 = 0.910$     |                |    | $Pred R^2 = 0.839$        |         |          |             |
| $Adj R^2 = 0.880$ |                |    | $Adeq Precision = 20.808$ |         |          |             |

Table 6: ANOVA table for lower kerf width reduced quadratic model.

| Source                     | Sum of Squares | DF | Mean Square                 | F Value  | Prob > F |             |
|----------------------------|----------------|----|-----------------------------|----------|----------|-------------|
| Model                      | 0.0323         | 17 | 0.0019                      | 9.711    | < 0.0001 | Significant |
| A                          | 0.0032         | 1  | 0.0032                      | 16.378   | 0.0004   |             |
| B                          | 0.0111         | 1  | 0.0111                      | 56.578   | < 0.0001 |             |
| C                          | 0.0006         | 1  | 0.0006                      | 3.197    | 0.0846   |             |
| D                          | 0.0006         | 1  | 0.0006                      | 3.050    | 0.0917   |             |
| E                          | 0.0003         | 2  | 0.0001                      | 0.726    | 0.4929   |             |
| AE                         | 0.0011         | 2  | 0.0006                      | 2.872    | 0.0733   |             |
| BD                         | 0.0016         | 1  | 0.0016                      | 8.322    | 0.0075   |             |
| BE                         | 0.0010         | 2  | 0.0005                      | 2.683    | 0.0859   |             |
| CD                         | 0.0026         | 1  | 0.0026                      | 13.046   | 0.0012   |             |
| DE                         | 0.0015         | 2  | 0.0008                      | 3.926    | 0.0314   |             |
| A <sup>2</sup>             | 0.0008         | 1  | 0.0008                      | 3.951    | 0.0567   |             |
| B <sup>2</sup>             | 0.0020         | 1  | 0.0020                      | 10.486   | 0.0031   |             |
| C <sup>2</sup>             | 0.0079         | 1  | 0.0079                      | 40.47176 | < 0.0001 |             |
| Residual                   | 0.0055         | 28 | 0.000195                    |          |          |             |
| Lack of Fit                | 0.004871       | 23 | 0.000212                    | 1.758863 | 0.2768   | Not Sig.    |
| Pure Error                 | 0.000602       | 5  | 0.00012                     |          |          |             |
| Cor Total                  | 0.037744       | 45 |                             |          |          |             |
| R <sup>2</sup> = 0.855     |                |    | Pred R <sup>2</sup> = 0.542 |          |          |             |
| Adj R <sup>2</sup> = 0.767 |                |    | Adeq Precision = 12.065     |          |          |             |

Table 7: ANOVA table for ratio reduced quadratic model.

| Source                     | Sum of Squares | DF | Mean Square                 | F Value  | Prob > F |             |
|----------------------------|----------------|----|-----------------------------|----------|----------|-------------|
| Model                      | 1.9997         | 12 | 0.1666                      | 9.091    | < 0.0001 | Significant |
| A                          | 0.0000         | 1  | 0.0000                      | 0.000    | 0.9861   |             |
| B                          | 0.0560         | 1  | 0.0560                      | 3.057    | 0.0897   |             |
| C                          | 0.3178         | 1  | 0.3178                      | 17.339   | 0.0002   |             |
| D                          | 0.1387         | 1  | 0.1387                      | 7.568    | 0.0096   |             |
| E                          | 0.2862         | 2  | 0.1431                      | 7.806    | 0.0017   |             |
| BD                         | 0.1507         | 1  | 0.1507                      | 8.223    | 0.0072   |             |
| CD                         | 0.1547         | 1  | 0.1547                      | 8.442    | 0.0065   |             |
| A <sup>2</sup>             | 0.3558         | 1  | 0.3558                      | 19.408   | 0.0001   |             |
| B <sup>2</sup>             | 0.2954         | 1  | 0.2954                      | 16.118   | 0.0003   |             |
| C <sup>2</sup>             | 0.9395         | 1  | 0.9395                      | 51.256   | < 0.0001 |             |
| D <sup>2</sup>             | 0.1395         | 1  | 0.1395                      | 7.610    | 0.0094   |             |
| Residual                   | 0.6049         | 33 | 0.0183                      |          |          |             |
| Lack of Fit                | 0.5138         | 28 | 0.0184                      | 1.007827 | 0.5597   | Not Sig.    |
| Pure Error                 | 0.0910         | 5  | 0.018209                    |          |          |             |
| Cor Total                  | 2.604571       | 45 |                             |          |          |             |
| R <sup>2</sup> = 0.855     |                |    | Pred R <sup>2</sup> = 0.511 |          |          |             |
| Adj R <sup>2</sup> = 0.683 |                |    | Adeq Precision = 12.300     |          |          |             |

Table 8: ANOVA table for roughness reduced quadratic model.

| Source                     | Sum of Squares | DF | Mean Square                 | F Value | Prob > F |                           |
|----------------------------|----------------|----|-----------------------------|---------|----------|---------------------------|
| Model                      | 4.1410         | 7  | 0.5916                      | 17.8507 | < 0.0001 | Significant               |
| A                          | 0.2806         | 1  | 0.2806                      | 8.4681  | 0.0060   |                           |
| B                          | 1.2778         | 1  | 1.2778                      | 38.5585 | < 0.0001 |                           |
| C                          | 0.9195         | 1  | 0.9195                      | 27.7462 | < 0.0001 |                           |
| D                          | 0.0735         | 1  | 0.0735                      | 2.2188  | 0.1446   |                           |
| B <sup>2</sup>             | 1.5248         | 1  | 1.5248                      | 46.0097 | < 0.0001 |                           |
| C <sup>2</sup>             | 0.1089         | 1  | 0.1089                      | 3.2856  | 0.0778   |                           |
| D <sup>2</sup>             | 0.2081         | 1  | 0.2081                      | 6.2789  | 0.0166   |                           |
| Residual                   | 1.2593         | 38 | 0.0331                      |         |          |                           |
| Lack of Fit                | 1.2331         | 33 | 0.0374                      | 7.1325  | 0.0184   | Not Sig. at $\alpha=0.01$ |
| Pure Error                 | 0.0262         | 5  | 0.0052                      |         |          |                           |
| Cor Total                  | 5.4004         | 45 |                             |         |          |                           |
| R <sup>2</sup> = 0.767     |                |    | Pred R <sup>2</sup> = 0.635 |         |          |                           |
| Adj R <sup>2</sup> = 0.734 |                |    | Adeq Precision = 16.956     |         |          |                           |

Table 9: ANOVA table for operating cost reduced quadratic model.

| Source                     | Sum of Squares | DF | Mean Square                 | F Value     | Prob > F |             |
|----------------------------|----------------|----|-----------------------------|-------------|----------|-------------|
| Model                      | 12.884206      | 12 | 1.0737                      | 15774705.83 | < 0.0001 | Significant |
| A                          | 0.000105       | 1  | 0.0001                      | 1542.23     | < 0.0001 |             |
| B                          | 4.827796       | 1  | 4.8278                      | 70930617.16 | < 0.0001 |             |
| D                          | 0.525086       | 1  | 0.5251                      | 7714639.87  | < 0.0001 |             |
| E                          | 7.256601       | 2  | 3.6283                      | 53307470.27 | < 0.0001 |             |
| AD                         | 0.000001       | 1  | 0.0000                      | 10.97       | 0.0022   |             |
| AE                         | 0.000016       | 2  | 0.0000                      | 117.16      | < 0.0001 |             |
| DE                         | 0.000095       | 2  | 0.0000                      | 698.08      | < 0.0001 |             |
| B <sup>2</sup>             | 0.204422       | 1  | 0.2044                      | 3003398.42  | < 0.0001 |             |
| D <sup>2</sup>             | 0.002628       | 1  | 0.0026                      | 38618.03    | < 0.0001 |             |
| Residual                   | 0.000002       | 33 | 6.81E-08                    |             |          |             |
| Cor Total                  | 12.884209      | 45 |                             |             |          |             |
| R <sup>2</sup> = 0.855     |                |    | Pred R <sup>2</sup> = 0.511 |             |          |             |
| Adj R <sup>2</sup> = 0.683 |                |    | Adeq Precision = 12.300     |             |          |             |

The mathematical models for nozzle diameter of 1 mm are as follows:

$$\begin{aligned}
 \text{Upper Kerf} = & -1.27254 + 1.03467 * \text{Laser power} - 4.47361\text{E-}005 * \text{Cutting speed} \\
 & -0.13479 * \text{Focal position} + 0.10236 * \text{Nitrogen pressure} \\
 & -1.44167\text{E-}005 * \text{Cutting speed} * \text{Focal position} - 0.38367 * \text{Laser power}^2 \\
 & -1.13681\text{E-}008 * \text{Cutting speed}^2 - 0.023479 * \text{Focal position}^2 \\
 & -3.69444\text{E-}003 * \text{Nitrogen pressure}^2
 \end{aligned} \tag{4}$$

$$\begin{aligned} \text{Lower Kerf} = & 0.81013 - 0.33202 * \text{Laser power} - 2.14646\text{E-}006 * \text{Cutting speed} \\ & + 0.30630 * \text{Focal position} - 1.76667\text{E-}003 * \text{Nitrogen pressure} \\ & - 8.06667\text{E-}006 * \text{Cutting speed} * \text{Nitrogen pressure} \\ & - 0.010100 * \text{Focal position} * \text{Nitrogen pressure} \\ & + 0.14481 * \text{Laser power}^2 + 1.47449\text{E-}008 * \text{Cutting speed}^2 \\ & + 0.028967 * \text{Focal position}^2 \end{aligned} \quad (5)$$

$$\begin{aligned} \text{Ratio} = & -12.12985 + 8.07832 * \text{Laser power} - 2.93788\text{E-}004 * \text{Cutting speed} \\ & - 3.09299 * \text{Focal position} + 0.62368 * \text{Nitrogen pressure} \\ & + 7.76458\text{E-}005 * \text{Cutting speed} * \text{Nitrogen pressure} \\ & + 0.078674 * \text{Focal position} * \text{Nitrogen pressure} \\ & - 3.23038 * \text{Laser power}^2 - 1.83990\text{E-}007 * \text{Cutting speed}^2 \\ & - 0.32810 * \text{Focal position}^2 - 0.020228 * \text{Nitrogen pressure}^2 \end{aligned} \quad (6)$$

$$\begin{aligned} \text{Ra} = & 6.52117 - 0.52975 * \text{Laser power} - 1.28860\text{E-}003 * \text{Cutting speed} \\ & + 0.39008 * \text{Focal position} - 0.60755 * \text{Nitrogen pressure} \\ & + 3.92802\text{E-}007 * \text{Cutting speed}^2 + 0.10497 * \text{Focal position}^2 \\ & + 0.023217 * \text{Nitrogen pressure}^2 \end{aligned} \quad (7)$$

$$\begin{aligned} \text{Ln(Operating cost)} = & -0.048359 + 0.028837 * \text{Laser power} - 1.12461\text{E-}003 * \\ & \text{Cutting speed} + 0.13613 * \text{Nitrogen pressure} - \\ & 6.91362\text{E-}004 * \text{Laser power} * \text{Nitrogen pressure} + \\ & 1.43825\text{E-}007 * \text{Cutting speed}^2 - 2.60941\text{E-}003 * \\ & \text{Nitrogen pressure}^2 \end{aligned} \quad (8)$$

The mathematical models for nozzle diameter of 1.5 mm are as follows:

$$\begin{aligned} \text{Upper Kerf} = & -1.23634 + 1.03467 * \text{Laser power} - 4.47361\text{E-}005 * \text{Cutting speed} \\ & - 0.13479 * \text{Focal position} + 0.10236 * \text{Nitrogen pressure} \\ & - 1.44167\text{E-}005 * \text{Cutting speed} * \text{Focal position} - 0.38367 * \\ & \text{Laser power}^2 - 1.13681\text{E-}008 * \text{Cutting speed}^2 - 0.023479 * \\ & \text{Focal position}^2 - 3.69444\text{E-}003 * \text{Nitrogen pressure}^2 \end{aligned} \quad (9)$$

$$\begin{aligned} \text{Lower Kerf} = & 0.86483 - 0.28769 * \text{Laser power} + 1.61035\text{E-}005 * \text{Cutting speed} \\ & + 0.30630 * \text{Focal position} - 0.013622 * \text{Nitrogen pressure} \\ & - 8.06667\text{E-}006 * \text{Cutting speed} * \text{Nitrogen pressure} \\ & - 0.010100 * \text{Focal position} * \text{Nitrogen pressure} \\ & + 0.14481 * \text{Laser power}^2 + 1.47449\text{E-}008 * \text{Cutting speed}^2 \\ & + 0.028967 * \text{Focal position}^2 \end{aligned} \quad (10)$$

$$\begin{aligned} \text{Ratio} = & - 11.9074 + 8.07832 * \text{Laser power} - 2.93788\text{E-}004 * \text{Cutting speed} \\ & - 3.09299 * \text{Focal position} + 0.62368 * \text{Nitrogen pressure} \\ & + 7.76458\text{E-}005 * \text{Cutting speed} * \text{Nitrogen pressure} \\ & + 0.078674 * \text{Focal position} * \text{Nitrogen pressure} \\ & - 3.23038 * \text{Laser power}^2 - 1.83990\text{E-}007 * \text{Cutting speed}^2 \\ & - 0.32810 * \text{Focal position}^2 - 0.020228 * \text{Nitrogen pressure}^2 \end{aligned} \quad (11)$$

$$\begin{aligned} \text{Ra} = & 6.52117 - 0.52975 * \text{Laser power} - 1.28860\text{E-}003 * \text{Cutting speed} \\ & + 0.39008 * \text{Focal position} - 0.60755 * \text{Nitrogen pressure} \\ & + 3.92802\text{E-}007 * \text{Cutting speed}^2 + 0.10497 * \text{Focal position}^2 \\ & + 0.023217 * \text{Nitrogen pressure}^2 \end{aligned} \quad (12)$$

$$\begin{aligned} \text{Ln(Operating cost)} = & +0.70636 + 0.018053 * \text{Laser power} - 1.12461\text{E-}003 * \\ & \text{Cutting speed} + 0.13877 * \text{Nitrogen pressure} \\ & - 6.91362\text{E-}004 * \text{Laser power} * \text{Nitrogen pressure} + \\ & 1.43825\text{E-}007 * \text{Cutting speed}^2 - 2.60941\text{E-}003 * \\ & \text{Nitrogen pressure}^2 \end{aligned} \quad (13)$$

The mathematical models for nozzle diameter of 2 mm are as follows:

$$\begin{aligned} \text{Upper Kerf} = & -1.24154 + 1.03467 * \text{Laser power} - 4.47361\text{E-}005 * \text{Cutting speed} \\ & - 0.13479 * \text{Focal position} + 0.10236 * \text{Nitrogen pressure} \\ & - 1.44167\text{E-}005 * \text{Cutting speed} * \text{Focal position} - 0.38367 * \text{Laser power}^2 \\ & - 1.13681\text{E-}008 * \text{Cutting speed}^2 - 0.023479 * \text{Focal position}^2 \\ & - 3.69444\text{E-}003 * \text{Nitrogen pressure}^2 \end{aligned} \quad (14)$$

$$\begin{aligned} \text{Lower Kerf} = & 0.92446 - 0.38535 * \text{Laser power} - 3.00202\text{E-}005 * \text{Cutting speed} \\ & + 0.30630 * \text{Focal position} - 0.010300 * \text{Nitrogen pressure} \\ & - 8.06667\text{E-}006 * \text{Cutting speed} * \text{Nitrogen pressure} \\ & - 0.010100 * \text{Focal position} * \text{Nitrogen pressure} \\ & + 0.14481 * \text{Laser power}^2 + 1.47449\text{E-}008 * \text{Cutting speed}^2 \\ & + 0.028967 * \text{Focal position}^2 \end{aligned} \quad (15)$$

$$\begin{aligned} \text{Ratio} = & -12.0057 + 8.07832 * \text{Laser power} - 2.93788\text{E-}004 * \text{Cutting speed} \\ & - 3.09299 * \text{Focal position} + 0.62368 * \text{Nitrogen pressure} \\ & + 7.76458\text{E-}005 * \text{Cutting speed} * \text{Nitrogen pressure} \\ & + 0.078674 * \text{Focal position} * \text{Nitrogen pressure} \\ & - 3.23038 * \text{Laser power}^2 - 1.83990\text{E-}007 * \text{Cutting speed}^2 \\ & - 0.32810 * \text{Focal position}^2 - 0.020228 * \text{Nitrogen pressure}^2 \end{aligned} \quad (16)$$

$$\begin{aligned}
 R_a = & 6.52117 - 0.52975 * \text{Laser power} - 1.28860\text{E-}003 * \text{Cutting speed} \\
 & + 0.39008 * \text{Focal position} - 0.60755 * \text{Nitrogen pressure} \\
 & + 3.92802\text{E-}007 * \text{Cutting speed}^2 + 0.10497 * \text{Focal position}^2 \\
 & + 0.023217 * \text{Nitrogen pressure}^2
 \end{aligned}
 \tag{17}$$

$$\begin{aligned}
 \text{Ln(Operating cost)} = & +1.26155 + 0.013946 * \text{Laser power} \\
 & - 1.12461\text{E-}003 * \text{Cutting speed} \\
 & + 0.13975 * \text{Nitrogen pressure} \\
 & - 6.91362\text{E-}004 * \text{Laser power} * \text{Nitrogen pressure} \\
 & + 1.43825\text{E-}007 * \text{Cutting speed}^2 \\
 & - 2.60941\text{E-}003 * \text{Nitrogen pressure}^2
 \end{aligned}
 \tag{18}$$

#### 4.2 Validation of the models.

To confirm the adequacy of the developed models, three confirmation experiments were carried out using new randomly selected test conditions, each within the experiment range defined earlier in chapter 4. Using the point prediction option in the software, the values of all responses of the validation experiments were predicted using the previous developed models and compared with the experimentally measured responses values for these confirmation experiments. Table 10 summarizes the experimental conditions, actual experimental values, predicted values and percentage error in prediction. It is evident that the models can adequately describe the responses within the ranges considered as the maximum error percent in prediction is 9.292% which is in good agreement. All the **percentage errors** are in agreement with the values reported in [16 and 17].

Table 10: Confirmation experiments for AISI 316L.

| Exp. No. | A   | B    | C  | D    | E |           | Upper kerf | Lower kerf | ratio  | R <sub>a</sub> | Cost    |
|----------|-----|------|----|------|---|-----------|------------|------------|--------|----------------|---------|
| 1        | 1   | 3000 | -3 | 12.5 | 1 | Actual    | 0.159      | 0.138      | 1.152  | 1.582          | 0.4431  |
|          |     |      |    |      |   | Predicted | 0.167      | 0.145      | 1.104  | 1.469          | 0.4432  |
|          |     |      |    |      |   | Error %   | -5.036     | -5.179     | 4.210  | 7.164          | -0.0247 |
| 2        | 1.5 | 1000 | -3 | 12.5 | 1 | Actual    | 0.286      | 0.237      | 1.207  | 0.704          | 1.3428  |
|          |     |      |    |      |   | Predicted | 0.299      | 0.248      | 1.223  | 0.639          | 1.3431  |
|          |     |      |    |      |   | Error %   | -4.431     | -4.703     | -1.364 | 9.292          | -0.024  |
| 3        | 1.5 | 1000 | -3 | 15   | 2 | Actual    | 0.317      | 0.261      | 1.215  | 0.773          | 6.0197  |
|          |     |      |    |      |   | Predicted | 0.332      | 0.238      | 1.120  | 0.716          | 6.0207  |
|          |     |      |    |      |   | Error %   | -4.600     | 8.884      | 7.788  | 7.387          | -0.016  |

### 4.3 Effect of process parameters on the responses

#### 4.3.1 Upper kerf

The perturbation plot for the upper kerf width is shown in Fig. 1. The perturbation plot helps to compare the effect of all factors at a particular point in the design space. This type of display does not show the effect of interactions. The lines represent the behaviours of each factor, while holding the others constant (i.e. centre point by default). In the case of more than one factor this type of display could be used to find those factors that most affect the response. It is evident from Fig. 1 that the upper kerf width increases as the laser power and gas pressure increase, which agrees with [6, 7 and 8], yet above the centre values of both factors the upper kerf becomes stable. However, the upper kerf width sharply decreases as the cutting speed increases. This is in a good agreement with [7 and 8]. In the case of the focal point position, it is notable that as the focal position increases up to the centre point ( $C = -3$  mm) the upper kerf slightly increases, but, as the focal point increases beyond this point the upper kerf begins to decrease.

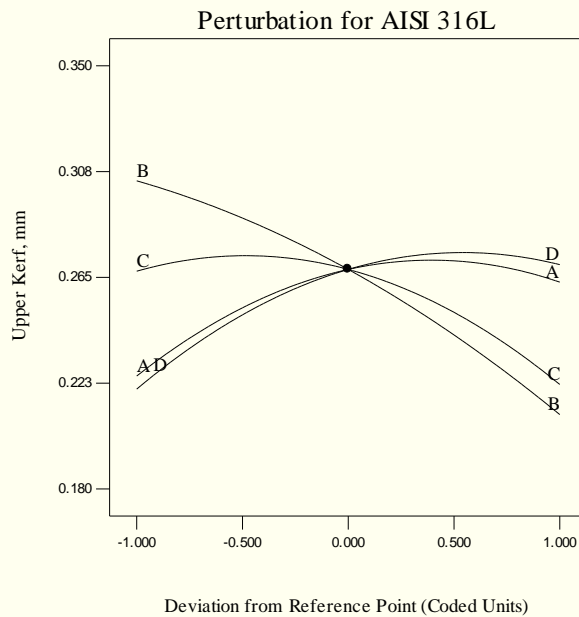


Fig. 1: Perturbation plot showing the effect of process parameters on upper kerf width.

Table 11 presents the overall percentage change in the upper kerf width as a result of changing each factor from its lowest value to its highest value while keeping the other factor at their centre values. It is evident from Table 11 that the cutting speed is the main factor influencing the upper kerf width, this result agrees with the results found in [7 and 8]. Fig. 2 is a



contour graph demonstrating the effect of both laser power and cutting speed on the upper kerf width at two nozzle diameters 1 and 1.5 mm. In fact, all the investigated LBC parameters are found to affect the upper kerf, and this outcome agrees with [4].

Table 11: Percentage change in upper kerf as each factor increases.

| Factor            | Percentage change in upper kerf, % |
|-------------------|------------------------------------|
| Laser power       | Increases by 16.75                 |
| Cutting speed     | Decreases by 30.92                 |
| Focal position    | Decreases by 17.01                 |
| Nitrogen pressure | Increases by 22.72                 |
| Nozzle diameter   | Increases by 11.56                 |

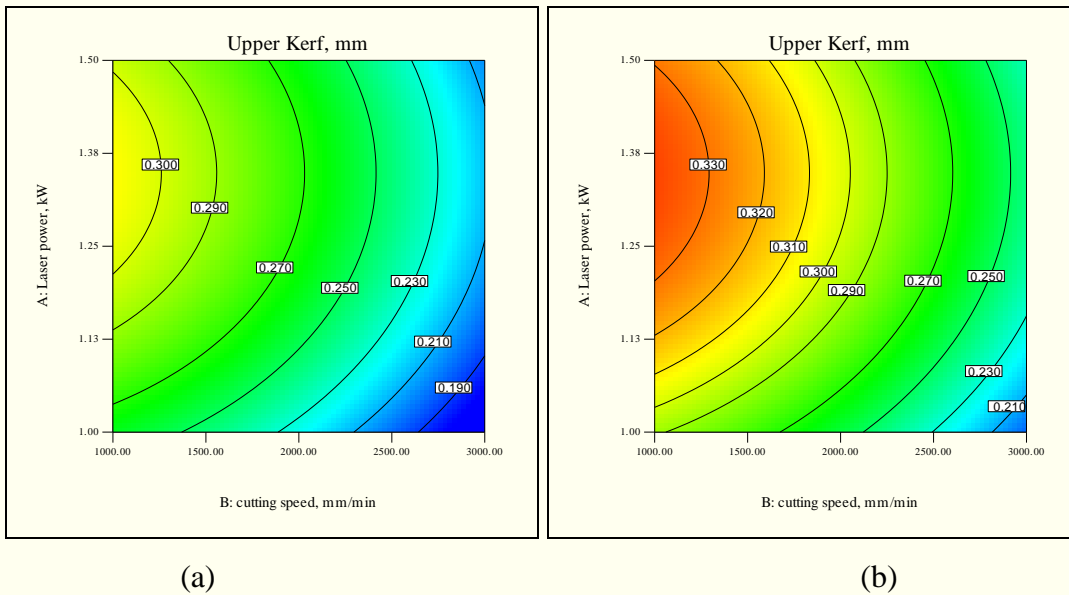


Fig. 2: Contours plot showing the effect of laser power and cutting speed on the upper kerf width at different nozzle diameters (a) 1 mm and (b) 1.5 mm.

#### 4.3.2 Lower kerf

It is clear from Fig. 3 that the lower kerf width increases as the laser power and the gas pressure increase. However, this response decreases with the increase in the focal point position up to the midpoint (i.e. -3 mm) and then starts to increase as the focal point position increases from -3 mm towards -2 mm. This incident could be related to the interaction between the gas

pressure and the focal point position, which will be discussed later. Also, the lower kerf decreases as the cutting speed increases this is in agreement with findings reported in [8].

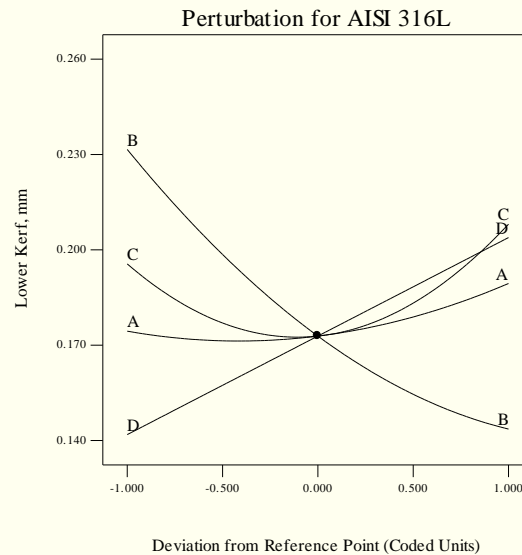


Fig. 3: Perturbation plot showing the effect of process parameters on lower kerf width.

The interaction plots help the researchers to find the best parameter settings that lead to the smaller possible lower kerf or the desirable response value. Fig. 4 demonstrates the interaction effect between the cutting speed and nitrogen pressure on the lower kerf width. It is clear that at low cutting speeds below 2100 mm/min a smaller lower kerf width of 0.170 mm could be obtained if the lowest nitrogen pressure of 10 bar is used. On the other hand, at higher cutting speeds above 2100 mm/min the smallest lower kerf width of 0.14 mm could be produced if the highest nitrogen pressure of 15 bar was supplied. At cutting speeds of about 2100 mm/min both levels of nitrogen pressure have the same effect on the lower kerf width. Fig. 5 shows the interaction effect between the focal point position and the nitrogen pressure. It is evident that the use of a wider laser beam (i.e. focal position of - 4 mm) leads a small lower kerf width of 0.17 only if the lowest gas pressure of 10 bar is applied. On the other hand, using a narrower laser beam (i.e. focal position of - 2 mm) results in a small lower kerf width only when the highest nitrogen pressure of 15 bar was applied. However, the nitrogen pressure would have the same effect on the lower kerf width if a focal point position just above -3 mm was employed. Dilthey et al. [9] have reported that exact adjustment of focal position and gas jet is essential, which supports the above findings. It is clear from the interaction graph shown in Fig. 6 that when using

a nozzle diameter of 1.5 mm there is no significant difference between the lower kerf width values produced by supplying either level of nitrogen pressures. **This supports the idea of fixing the nozzle diameter to 1.5 mm in the optimization for the first criterion.** It is evident from Table 12 that the nitrogen pressure and cutting speed are the main factors influencing the lower kerf width.

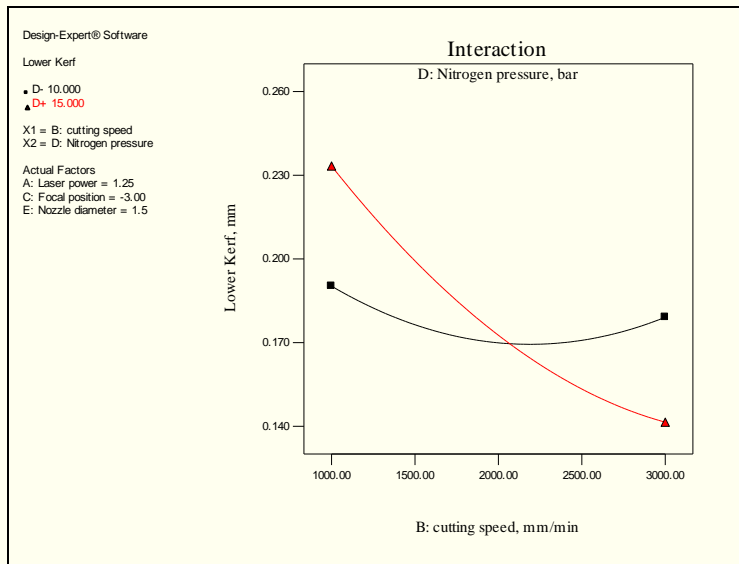


Fig. 4: Interaction plot showing the interaction between the cutting speed and the nitrogen pressure on the lower kerf.

Table 12: Percentage change in lower kerf as each factor increases.

| Factor            | Percentage change in lower kerf, % |
|-------------------|------------------------------------|
| Laser power       | Increases by 8.60                  |
| Cutting speed     | Decreases by 38.00                 |
| Focal position    | Increases by 6.39                  |
| Nitrogen pressure | Increases by 43.71                 |
| Nozzle diameter   | Increases by 3.09                  |

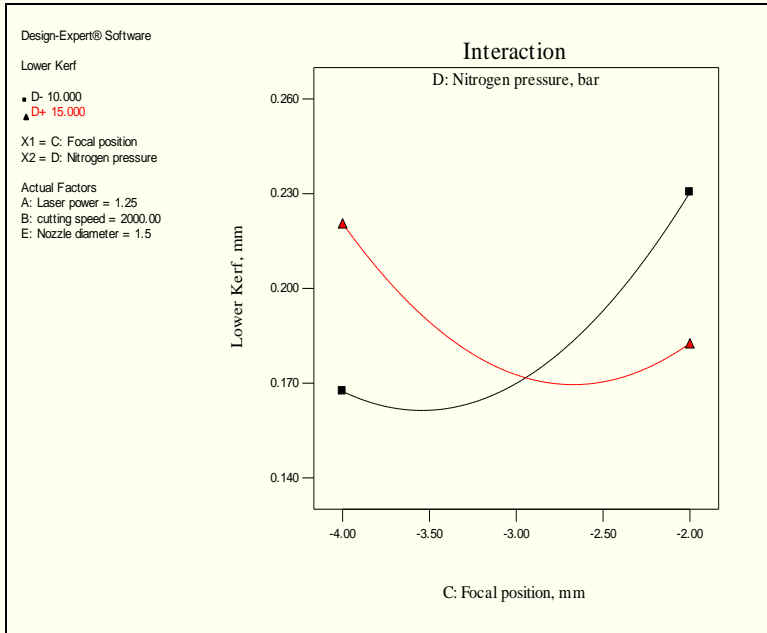


Fig. 5: Interaction plot showing the interaction between the focal position and the nitrogen pressure on the lower kerf.

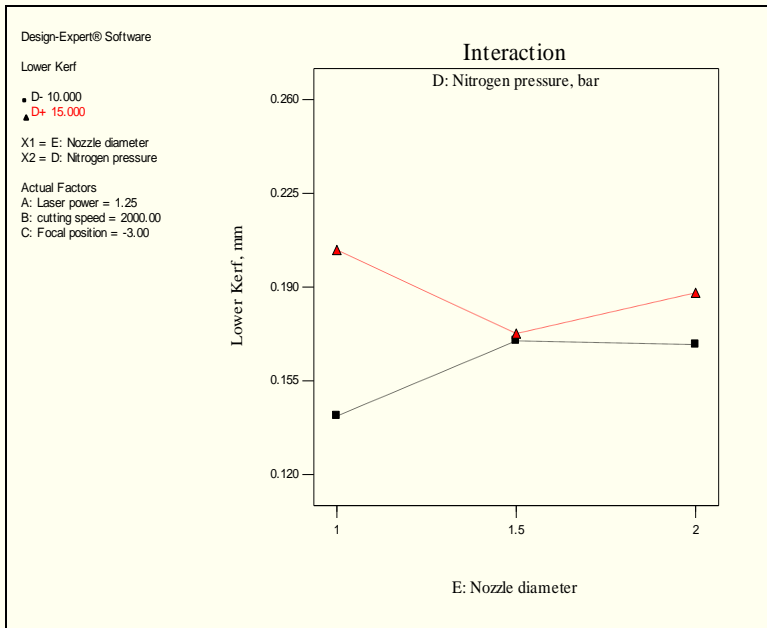


Fig. 6: Interaction plot showing the interaction between the nozzle diameter and the nitrogen pressure on the lower kerf.

### 4.3.3 Ratio

Fig. 7 is an interaction plot showing the influence of cutting speed and nitrogen pressure on the ratio. It is apparent that by using cutting speeds below 1520 mm/min the ratio would be less (close to one) if the highest nitrogen pressure of 15 bar was supplied. Above this value of cutting speed the ratio would be less if the lowest nitrogen pressure of 10 bar was used. The same trend was noticed as the nozzle diameter changed. From the interaction graph shown in Fig. 8 it is obvious that by using focal position below -3.48 mm the ratio would be close to one if the highest nitrogen pressure of 15 bar was used. Above -3.48 the ratio would be close to one as the lowest nitrogen pressure of 10 bar was used. It is evident from Table 13 that the focal position and nitrogen pressure are the main factors influencing the ratio. These findings are in fair agreement with results reported in [10]. The results show that the range of the ratio lays between 0.94 and 1.93 for AISI316L. Therefore, a target ratio of one in this case will be a desirable goal when searching for the optimal condition to obtain a square cut edge.

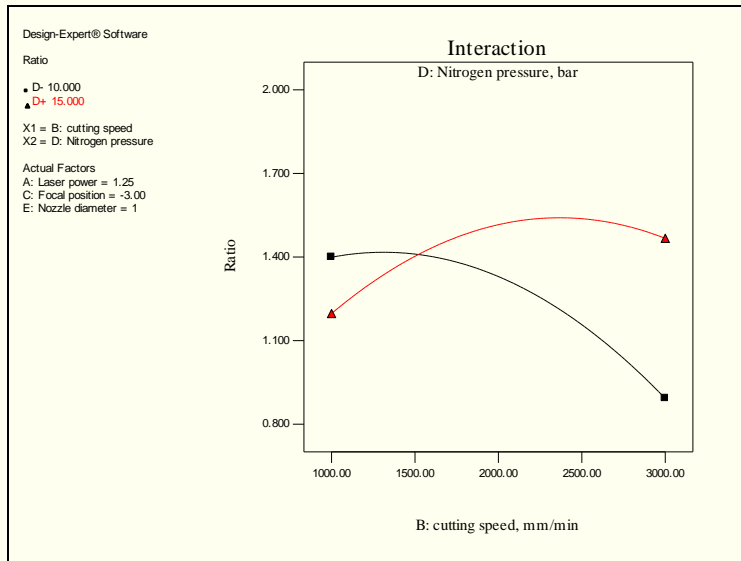


Fig. 7: Interaction plot showing the interaction between the cutting speed and the nitrogen pressure on the ratio.

Table 13: Percentage change in ratio as each factor increases.

| Factor            | Percentage change in ratio, % |
|-------------------|-------------------------------|
| Laser power       | Increases by 0.09             |
| Cutting speed     | Decreases by 8.31             |
| Focal position    | Decreases by 20.69            |
| Nitrogen pressure | Increases by 14.00            |
| Nozzle diameter   | Increases by 8.02             |

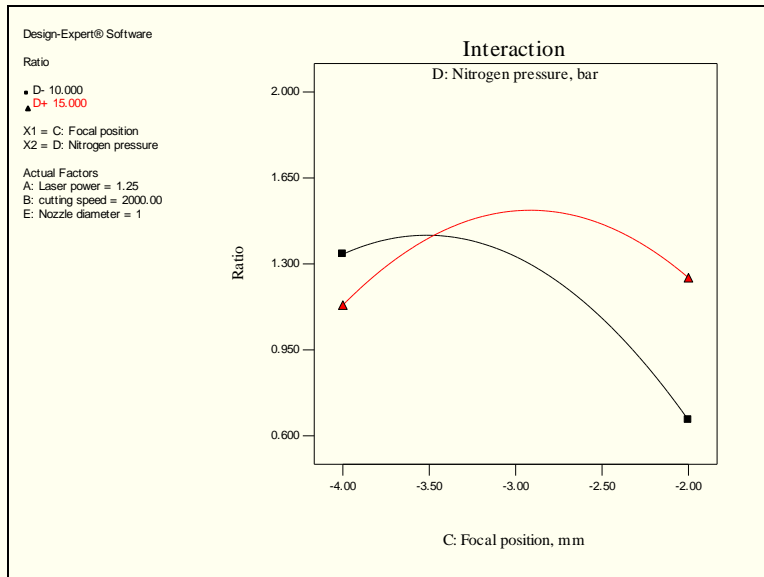


Fig. 8: Interaction plot showing the interaction between the focal position and the nitrogen pressure on the ratio.

#### 4.3.4 Surface roughness

Fig. 9 is a perturbation plot showing the effect of all laser cutting parameters on the roughness of the cut surface. It is evident from the results that the  $R_a$  value decreases as the laser power, focal point position and nitrogen pressure increase; these findings are in agreement with [11] and disagree with [12]. However, the  $R_a$  value starts to rise as the nitrogen pressure increases above 13.4 bar as can be seen in Fig. 9. Moreover, the roughness decreases slightly as the cutting speed increases up to 1505 mm/min, which agrees with [12]. Between 1505 – 1740 mm/min the surface roughness values become stable, and then they remarkably increase as the cutting speed increases above 1740 mm/min, which disagrees with [12]. The results confirm that the nozzle diameter has no significant effect on the roughness of the cut surface in contrast to the apparent

results in Fig. 9. It is clear from Table 14 that the cutting speed, focal position and laser power are the main factors influencing the cut surface roughness.

Table 14: Percentage change in roughness as each factor increases.

| Factor            | Percentage change in $R_a$ , % |
|-------------------|--------------------------------|
| Laser power       | Decreases by 33.39             |
| Cutting speed     | Increases by 73.31             |
| Focal position    | Decreases by 47.68             |
| Nitrogen pressure | Decreases by 15.52             |
| Nozzle diameter   | No effect                      |

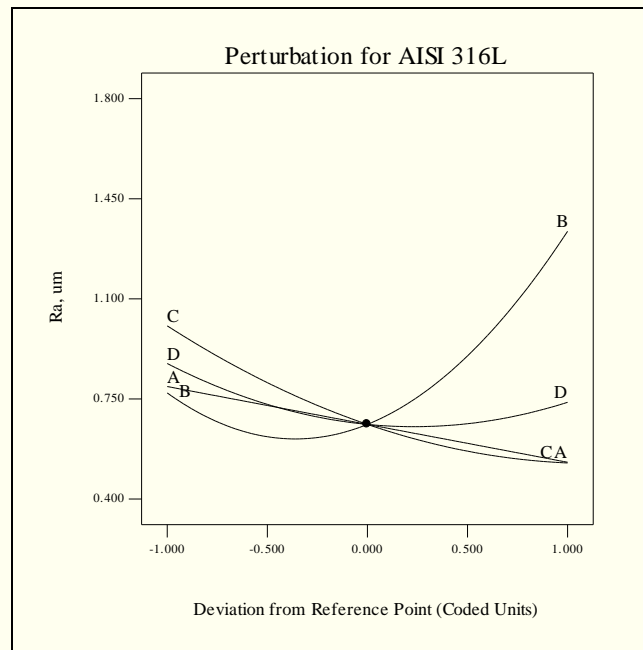


Fig. 9: Perturbation plot showing the effect of process parameters on roughness.

#### 4.3.5 Operating cost

The perturbation plot would help to compare the effect of all the factors at a particular point in the design space. It is evident from Fig.10, that in the case of cutting speed, steep curvatures indicate that the responses are too sensitive to this factor. Also, Fig. 10a-c demonstrates the importance of the nozzle diameter with respect to the operating cost, while the steep slopes in the case of laser power and nitrogen pressure indicate that the operating cost is

less sensitive to these factors. In addition, the results indicate that as the laser power, nitrogen pressure and nozzle diameter increase the operating cost increases too. On the other hand, as the cutting speed increases the operating cost decreases sharply. These results are intuitive because more electrical power will be consumed as the laser power increases. Also, more gas will be consumed as both the nitrogen pressure and the nozzle diameter increase. However, the cost will decrease as the cutting speed increases due to the fact that the cutting will be performed in less time, and consequently, less electrical power and nitrogen gas will be consumed. Fig. 10 is a perturbation plot illustrating the above findings. It is apparent that the nozzle diameter, cutting speed and nitrogen pressure are the key factors affecting the operating cost. Moreover, these changes in the operating cost in terms of percentages are presented in Table 15 as each factor increases from its lowest level to its highest level. It is clear that the focal position has no effect on the operating cost.

On balance, it is evident from the above results for AISI316L that all the process parameters considered in this research affect the quality features somehow. Furthermore, in some cases, these parameter may interact in such a way that it becomes too hard to find the best cutting conditions which lead to the desired quality features. Therefore, an overall optimization should be performed for this material which would account for the minimization of the surface roughness, kerf widths and operating cost etc, or the maximization of the cut edge squareness. It is notable that the main factors affecting the operating cost are: nozzle diameter, cutting speed and minor effect of laser power



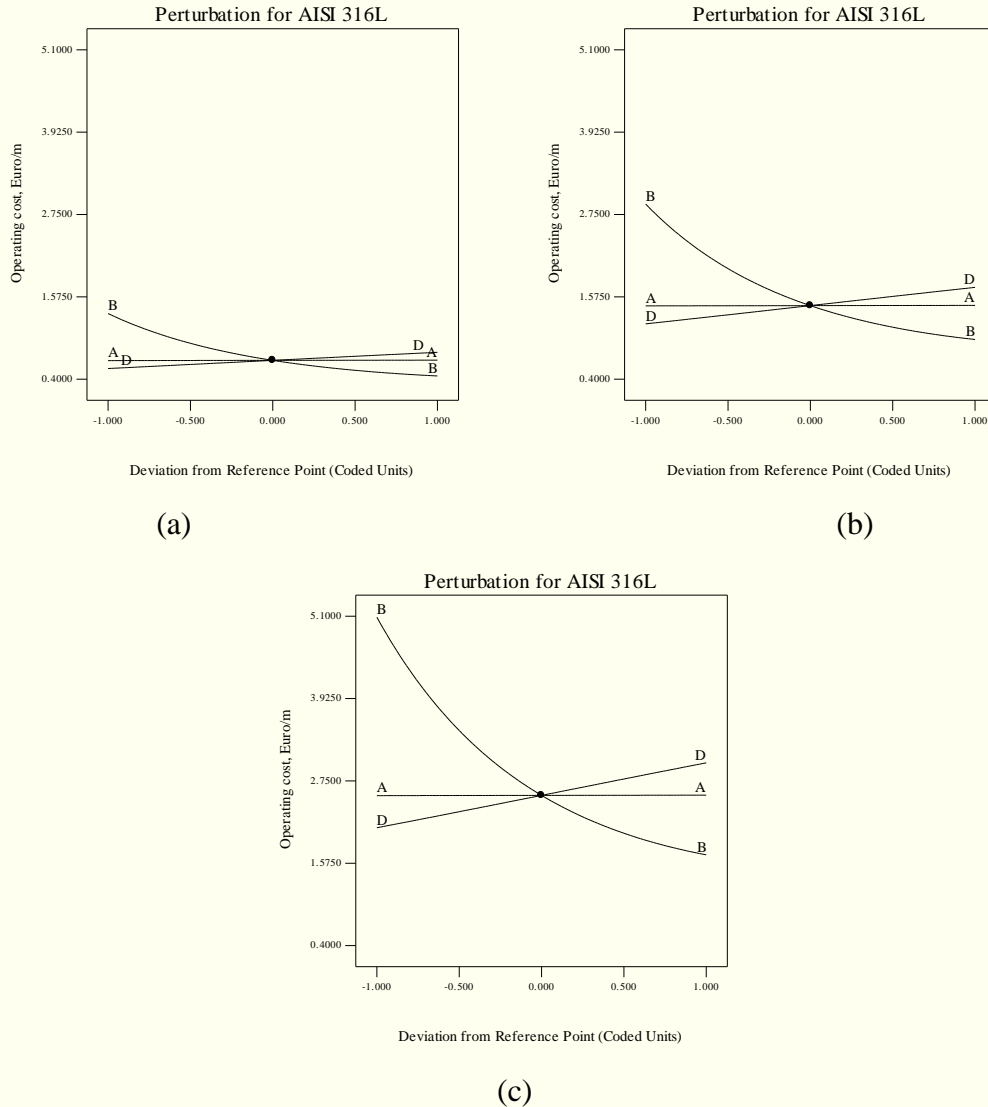


Fig. 10: Perturbation plot illustrating the effect of process factors on operating cost at different nozzle diameters (a) 1 mm, (b) 1.5 mm and (c) 2 mm.

Table 15: Percentage change in cost as each factor increases.

| Factor            | Percentage change in cost, % |
|-------------------|------------------------------|
| Laser power       | Increases by 1.01            |
| Cutting speed     | Decreases by 66.67           |
| Focal position    | No effect                    |
| Nitrogen pressure | Increases by 41.92           |
| Nozzle diameter   | Increases by 280.59          |

## 5. OPTIMIZATION

Laser cutting is a multi-input and multi-output process that needs to be assessed carefully in order to achieve the most desirable results. Planning the fabrication of parts based on quality of the final cut surface alone may have important cost implications, which should be evaluated. Based on the previously presented results and discussion it is clear that there are many factors and their interactions, which affect the process. Thus, an in-depth optimization is required. To run any optimization it is important to know the following: the effect of each factor and its interaction effect with the other factors on the responses, the output of the process (i.e. responses) and finally the desirable criterion (i.e. the goal). In the numerical optimization for this research two criteria were used. The difference between these two criteria is that in the first criterion there were no restrictions on the process input parameters and the output quality features were set to achieve the highest quality in terms of surface roughness and cut edge perpendicularity (referring to this criterion as Quality). In the second criterion, the cost of the cutting is the main issue; consequently, some restrictions have been put on the process input parameters which have an effect on the operating cost. Also, regarding the second criterion, the operating cost was set to be a minimum with no restrictions on the other responses (referring to this criterion as Cost). This multi-responses optimization is solved via the desirability approach explained earlier in chapter 3, which is built in the Design expert software. Two types of optimization layout are available in Design expert. The first one, the numerical optimization feature, which finds a point or more in the factors domain that, would maximize the overall desirability (i.e. objective function). The second one, the graphical optimization, where the optimal range of each response has to be brought from the numerical optimization results in order to present them graphically. The graphical optimization allows visual selection of the optimal cutting conditions according to certain criterion. Graphical optimization results in plots called overlay plots. These plots are extremely practical for technical use at the workshop and help the operator to choose the optimal values of the laser cutting parameters to achieve the desirable response values for each material. The green/shaded areas on the overlay plots are the regions that meet the proposed criteria.

For this material the two optimization criteria are presented in Table 16. As seen in Table 16, that each factor and response have allocated a specific goal and importance. The nozzle

diameter was set at 1.5 mm. This value was chosen because it was found to be the best nozzle diameter that would lead to kerf widths close to each other, and consequently, a square cut edge.

### **5.1 Numerical optimization**

Table 17 shows the optimal setting of the process parameters and the corresponding response values for both criteria for 2 mm AISI316L. It is noticeable that to obtain the superior quality cut with predicted ratio as close as possible to one and  $Ra \approx 0.405 \mu\text{m}$ . The laser power has to be 1.49 kW with cutting speed between 1538-1661 mm/min, a focal point position of -2.02 mm, nitrogen pressure of around 11.4 bar and nozzle diameter of 1.5 mm have to be applied. Alternatively, if the reduction in the cutting cost is essential, it is confirmed that, a laser power of 1.02 kW has to be applied with cutting speed from 1900 to 2968 mm/min, a focal point position ranged from -3.92 mm to -2.85 mm, nitrogen pressure ranged between 10.4-12.9 bar and a nozzle diameter of 1 mm have to be used. It is clear that the roughness of cut section produced by using the setting of the first criterion is on average 65.8% smoother than the one produced by using the conditions of the second criterion. On the other hand, the cutting operating cost in the second criterion is on average 71% cheaper than that of the first criterion.

### **5.2 Graphical optimization**

As mentioned earlier the range of each response has been chosen from the numerical optimization results in Table 17. These ranges were brought into the graphical optimization. Figures 11 and 12 show green areas which are the regions that comply with the first and second criteria respectively.

Table 16: Criteria for numerical optimization of AISI316L.

| Factor or response      | First criterion (Quality) |            | Second criterion (Cost) |            |
|-------------------------|---------------------------|------------|-------------------------|------------|
|                         | Goal                      | Importance | Goal                    | Importance |
| Laser power             | Is in range               | 3          | Minimize                | 5          |
| Cutting speed           | Is in range               | 3          | Maximize                | 5          |
| Focal position          | Is in range               | 3          | Is in range             | 3          |
| N <sub>2</sub> pressure | Is in range               | 3          | Minimize                | 3          |
| Nozzle Diameter         | Equal to 1.5              | 3          | Minimize                | 5          |
| Upper Kerf              | Is in range               | 3          | Is in range             | 3          |
| Lower Kerf              | Is in range               | 3          | Is in range             | 3          |
| Ratio                   | Target to 1               | 5          | Is in range             | 3          |
| Roughness               | Minimize                  | 5          | Is in range             | 3          |
| Operating cost          | Is in range               | 3          | Minimize                | 5          |

Table 17: Optimal cutting conditions as obtained by Design-Expert for 2 mm thick AISI316L.

|                                      | No. | A, kW | B, mm/min | C, mm | D, bar | E, mm | Upper kerf, mm | Lower kerf, mm | Ratio | Ra, mm | Cost, €/m | Desirability |
|--------------------------------------|-----|-------|-----------|-------|--------|-------|----------------|----------------|-------|--------|-----------|--------------|
| 1 <sup>st</sup> criterion<br>Quality | 1   | 1.49  | 1635      | -2.02 | 11.3   | 1.5   | 0.26           | 0.251          | 1     | 0.409  | 1.66      | 1            |
|                                      | 2   | 1.49  | 1636      | -2.01 | 11.4   | 1.5   | 0.26           | 0.251          | 1     | 0.402  | 1.67      | 1            |
|                                      | 3   | 1.49  | 1650      | -2.01 | 11.4   | 1.5   | 0.26           | 0.251          | 1     | 0.401  | 1.66      | 1            |
|                                      | 4   | 1.49  | 1661      | -2.02 | 11.4   | 1.5   | 0.258          | 0.25           | 1     | 0.409  | 1.63      | 1            |
|                                      | 5   | 1.49  | 1538      | -2    | 11.4   | 1.5   | 0.265          | 0.254          | 1     | 0.409  | 1.78      | 1            |
| 2 <sup>nd</sup> criterion<br>Cost    | 1   | 1.02  | 2575      | -3.32 | 11.7   | 1     | 0.198          | 0.145          | 1.243 | 1.195  | 0.48      | 0.8311       |
|                                      | 2   | 1.22  | 2968      | -3.92 | 11.4   | 1     | 0.208          | 0.146          | 1.099 | 1.685  | 0.41      | 0.7927       |
|                                      | 3   | 1.03  | 2106      | -3.11 | 11.1   | 1     | 0.21           | 0.151          | 1.31  | 0.919  | 0.57      | 0.7754       |
|                                      | 4   | 1.02  | 2831      | -3.08 | 12.9   | 1     | 0.19           | 0.15           | 1.246 | 1.303  | 0.48      | 0.7721       |
|                                      | 5   | 1.04  | 1900      | -2.85 | 10.4   | 1     | 0.198          | 0.154          | 1.199 | 0.878  | 0.60      | 0.7625       |

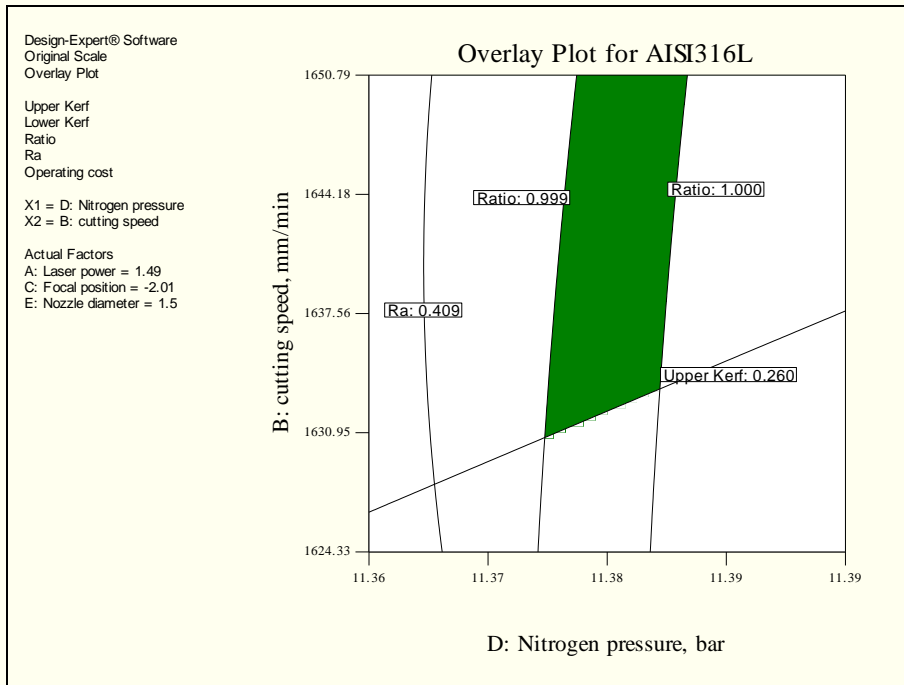


Fig. 11: Overlay plot shows the region of optimal cutting condition based on the first criterion for 2 mm AISI316L.

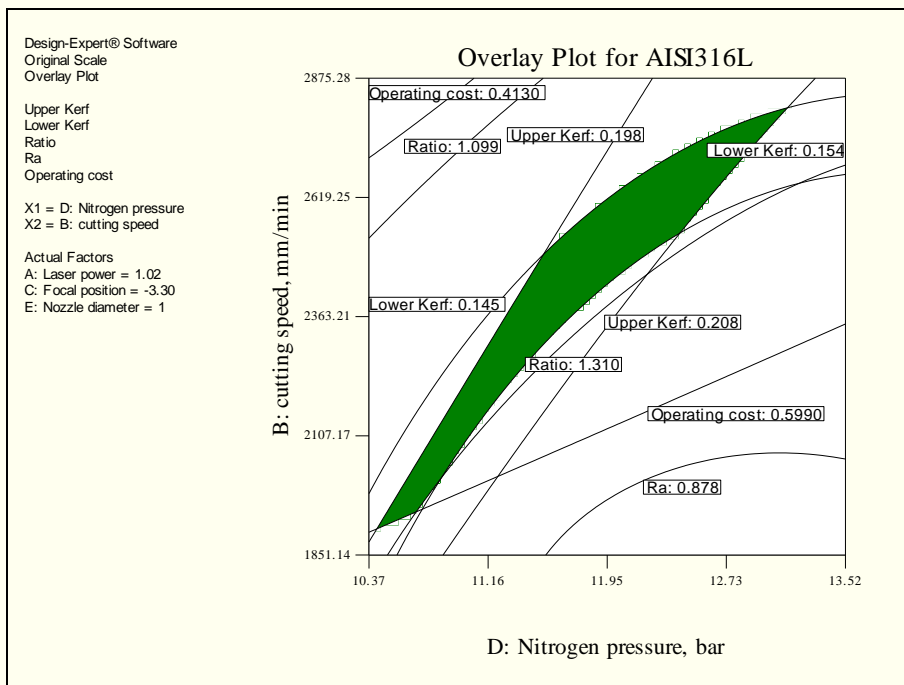


Fig. 12: Overlay plot shows the region of optimal cutting condition based on the second criterion for 2 mm AISI316L.

## **CONCLUSIONS**

The following points can be concluded from this work within the factors limits:

1. The upper kerf width increases as the laser power, nitrogen pressure and nozzle diameter increase, and it decreases as the cutting speed and focal position increase. However, the cutting speed is the main factor affecting the upper kerf.
2. The laser power, nitrogen pressure and focal position have a positive effect on the lower kerf width. While, the cutting speed has a negative effect.
3. The ratio increases as the laser power, nitrogen pressure and nozzle diameter increase, and it decreases as the cutting speed and focal position increases.
4. The roughness value increases as the cutting speed increases and it decreases as the other parameters increases. However, the nozzle diameter has no significant effect on the roughness.
5. The optimal cutting setting for AISI316L are laser power of 1.49 kW, cutting speed between 1538 and 1661 mm/min, a focal point position of - 2.02 mm, nitrogen pressure of around 11.4 bar and nozzle diameter of 1.5 mm if the quality is important. The cut section roughness is on average 65.8% smoother if this setting was applied.
6. The economical optimal settings are laser power of 1.02 kW, cutting speed from 1900 to 2968 mm/min, a focal point position ranged from -3.92 mm to -2.85 mm, nitrogen pressure ranged between 10.4 and 12.9 bar and a nozzle diameter of 1 mm.
7. A reduction of about 71% in the cutting operating cost could be achieved, if the economical setting is considered.

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