



MEng in Automation Engineering, University of Bologna

Academic Year 2012-2013

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This is a collection of past exam questions. Some of the questions are taken from the course text books.¹ For the time being, solutions are not provided.

Be aware that "Midterm" and "Final" exams only cover part of the syllabus. A "Standard" exam instead covers all the syllabus. Exam rules and organization of the course are summarized in the first set of slides.²

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¹Abraham Silberschatz, Peter B. Galvin, Greg Gagne. **Operating System Concepts**, 8th or 9th Edition. International Student Version. Wiley 2010 (2013), and Giorgio C. Buttazzo. **Hard Real-Time Computing Systems: Predictable Scheduling Algorithms** and **Applications**, 3rd Edition. Springer 2011

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First Midterm. April 5, 2013

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 Name

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Part I Quizzes (2 points)

Mark each of the following statements **True** or **False**. Explain your answer in one sentence (if you wish).

Q1) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ After a fork(), the child process and the parent process have no shared address space.

Explanation (optional):

Q2)

 \mathbf{F}

RPCs use a message-based communication scheme to provide a remote service.

Explanation (optional):



 $\begin{array}{c|c} \mathbf{T} & \text{A disadvantage of the M:M threading model is} \\ \hline \mathbf{F} & \text{that developers cannot create as many threads} \\ \text{as necessary, since kernel threads cannot run in} \\ \text{parallel on a multiprocessor.} \end{array}$

Explanation (optional):

Q4) T Ordinary pipes continue to exist even after the processes have finished communicating and have terminated.

Explanation (optional):

Part II Open questions (4 points)

- O1) Illustrate the **microkernel** approach to OS design. Comment on advantages and disadvantages.
- O2) Describe the differences among **short-term**, **mediumterm**, and **long term scheduling**.
- O3) There are many possible CPU-scheduling algorithms. How could we select one particular algorithm for a particular system? Discuss various **evaluation methods**.

Part III Exercise (3 points)

Suppose that processes P_1, P_2, \ldots, P_5 arrive for execution at the times indicated in Table 1. Each process will run for the amount of time listed, and will be assigned a priority ranging from **0** (highest) to **10** (lowest). No more processes will arrive until the last process completes.

In answering the questions, base all decisions on the information you have at the time the decision must be made.

Table 1: Process arrival/CPU-burst times and priorities.

D	A · 1 · TD ·	D / T	D
Process	<u>Arrival Time</u>	Burst Time	<u>Priority</u>
P_1	0.0	8	10
P_2	0.4	4	2
P_3	0.5	1	10
P_4	0.8	2	1
P_5	1.0	2	5

E1) Draw **four Gantt charts** that illustrate the execution of these processes using the following scheduling algorithms:

E1.1) FCFS;

- E1.2) preemptive SJF;
- E1.3) preemptive priority (SJF if priority is equal);

E1.4) RR (quantum=2).

- E2) What is the **turnaround time** of each process for each of these four scheduling algorithms?
- E3) What is the **waiting time** of each process for each of these four scheduling algorithms?
- E4) Which of the algorithms results in the **maximum** overall turnaround time (over all processes)?

Part IV Code analysis (2 points)

The program below uses the Phreads API.

- C1) What would be the output from the program at LINE A, LINE B, and LINE C?
- C2) How many processes/threads would be active by the time LINE B is executed?

Justify your answers. If there are different possible answers, explain what the possibilities are.

```
#include <sys/types.h>
#include <sys/wait.h>
#include <pthread.h>
#include <stdio.h>
#include <unistd.h>
int value = 5;
void *runner1(void *param);
void *runner2(void *param);
int main()
{
    pthread_t tid1, tid2;
    pthread_attr_t attr1, attr2;
    pthread_attr_init(&attr1);
    pthread_create(&tid1,&attr1,runner1,NULL);
    pthread_attr_init(&attr2);
    pthread_create(&tid2,&attr2,runner2,NULL);
    printf("A: value = %d\n", value); /* LINE A */
    pthread_join(tid1,NULL);
    pthread_join(tid2,NULL);
    return 0;
}
void *runner1(void *param) {
    value += 10;
    printf("B: value = %d\n", value); /* LINE B */
    pthread_exit(0);
}
void *runner2(void *param) {
    value += 10;
    printf("C: value = %d\n", value); /* LINE C */
    pthread_exit(0);
}
```

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Part I Quizzes (2 points)

Mark each of the following statements **True** or **False**. Explain your answer in one sentence (if you wish).

Q1) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ After a fork(), the child process and the parent process have no open files in common.

Explanation (optional):

 $Q2) \begin{array}{|c|c|c|c|c|} \hline \mathbf{T} & \mathbf{A} & \mathbf{rendezvous} & \mathrm{can} & \mathrm{be} & \mathrm{obtained} & \mathrm{using} & \mathrm{a} \\ \hline \mathbf{F} & \mathrm{blocking} & \mathrm{send}() & \mathrm{and} & \mathrm{blocking} & \mathrm{receive}(). \end{array}$

Explanation (optional):

TA disadvantage of the many-to-one threading
model is that the entire process will block if a
thread makes a blocking system call.

Explanation (optional):

Q3)

TA wait() system call is used to make a processQ4)Fwait for an input/output device to become ready.

Explanation (optional):

Part II Open questions (4 points)

- O1) What is the purpose of **interrupts**? Explain how interrupt-driven system operation can be obtained using **dual mode** operation and **system calls**.
- O2) Explain scheduling queues.
- O3) Describe the differences between **direct** communication and **indirect** communication in message-based systems.

Part III Exercise (3 points)

Suppose that processes P_1, P_2, \ldots, P_5 arrive for execution at the times indicated in Table 1. Each process will run for the amount of time listed, and will be assigned a priority ranging from **0** (highest) to **10** (lowest). No more processes will arrive until the last process completes.

In answering the questions, base all decisions on the information you have at the time the decision must be made.

Table 1: Process arrival/CPU-burst times and priorities.

Process	<u>Arrival Time</u>	Burst Time	Priority
P_2	$0.0 \\ 0.4$	8 4	$\frac{10}{2}$
P_3	0.5	1	10
P_4	0.8	2	1
P_5	1.0	2	5

- E1) Draw **four Gantt charts** that illustrate the execution of these processes using the following scheduling algorithms:
 - E1.1) nonpreemptive SJF;
 - E1.2) preemptive SJF;
 - E1.3) preemptive priority (FCFS if priority is equal);

E1.4) RR (quantum=4).

- E2) What is the **turnaround time** of each process for each of these four scheduling algorithms?
- E3) What is the **waiting time** of each process for each of these four scheduling algorithms?
- E4) Which of the algorithms results in the **minimum average waiting time** (over all processes)?

Part IV Code analysis (2 points)

The program below uses the Phreads API.

- C1) What would be the output from the program at LINE A, LINE B, and LINE C?
- C2) How many processes/threads would be active by the time LINE B is executed?

Justify your answers. If there are different possible answers, explain what the possibilities are.

```
#include <sys/types.h>
#include <sys/wait.h>
#include <pthread.h>
#include <stdio.h>
#include <unistd.h>
int value = 5;
void *runner(void *param);
int main()
{
  pid_t pid;
   pthread_t tid;
   pthread_attr_t attr;
   printf("A: value = %d\n", value); /* LINE A */
  pid = fork();
   if (pid == 0) {
      pthread_attr_init(&attr);
      pthread_create(&tid,&attr,runner,NULL);
      pthread_join(tid,NULL);
      printf("B: value = %d\n", value); /* LINE B */
      return 0;
   }
   else if (pid > 0) {
      wait(NULL);
      printf("C: value = %d\n", value); /* LINE C */
      return 0;
   }
   return 0;
}
void *runner(void *param) {
   value += 10;
   pthread_exit(0);
}
```

Second Midterm. May 13, 2013

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Part I Quizzes (2 points)

Mark each of the following statements **True** or **False**. Explain your answer in one sentence (if you wish).

Q1) $[\mathbf{T}]{\mathbf{F}}$

Q2)

A process **cannot be executed** if its logical address space is bigger than the size of the physical memory.

Explanation (optional):

T An **inverted page table** contains, in each entry, a page number and a frame number.

Explanation (optional):

 $\begin{array}{c|c} \mathbf{T} & \text{Paging eliminates internal fragmentation.} \\ \hline \mathbf{F} & \end{array}$

Explanation (optional):

 $\begin{array}{c|c} \mathbf{P} & \mathbf{T} & \mathbf{Deadlock} \text{ cannot occur among processes that} \\ \hline \mathbf{F} & \text{need at most one (non-shareable) resource each.} \end{array}$

Explanation (optional):

Part II Open questions (3 points)

O1) Why do some operating systems use **spinlocks** as a synchronisation mechanism only on multiprocessor systems and not on single-processor systems?

- O2) What is the cause of **thrashing**? How does the system detect thrashing? Once it detects thrashing, what can the system do to eliminate the problem?
- O3) Explain how data can be transferred from a device to the main memory using a **direct memory access** (DMA) controller.

Part III Exercises (3 points)

E1) Consider the following snapshot of a system:

$P_1 \\ P_2 \\ P_3 \\ P_4$	$\begin{array}{c} \underline{Allocation} \\ A \ B \ C \ D \\ 0 \ 0 \ 1 \ 2 \\ 1 \ 0 \ 0 \ 0 \\ 1 \ 3 \ 5 \ 4 \\ 0 \ 0 \ 0 \ 1 \end{array}$	$ \begin{array}{r} $	$\begin{array}{c} Request \\ \hline A \ B \ C \ D \\ 0 \ 0 \ 0 \ 1 \\ 0 \ 1 \ 1 \ 0 \\ 1 \ 0 \ 0 \ 0 \\ 2 \ 2 \ 0 \ 0 \end{array}$
-	$\frac{Available}{1\ 2\ 2\ 0}$		

- E1.1) Is the system in deadlock?
- E1.2) Is the system in a safe state?
- E1.3) Can P_3 's request be safely granted immediately?
- E1.4) If P_3 's request is granted immediately, does the system enter a deadlock?

Be sure to motivate your answers.

- E2) Given five memory partitions of 100 KB, 500 KB, 200 KB, 300 KB, and 600 KB (in order), how would the **first-fit**, **best-fit**, and **worst-fit** algorithms place processes of 210 KB, 420 KB, 110 KB, and 430 KB (in order)? Which algorithm makes the most efficient use of memory?
- E3) Consider the following reference string:

1, 2, 3, 4, 5, 3, 4, 1, 6, 7, 8, 7, 8, 9, 7, 8, 9, 5, 6, 5, 7.

Suppose you have **four page frames**. How may page faults occur for the LRU page replacement algorithm? Is that the minimum possible number of page faults?

Part IV Code analysis (3 points)

The **Cigarette-Smokers Problem** is a well-known process synchronisation problem that can defined as follows:

Consider a system with three *smoker* pro-Each smoker continuously rolls a cesses. cigarette (make_cigarette()) and then smokes it (smoke()). But to roll a cigarette, the smoker needs three resources: tobacco, paper, and matches. One of the *smokers* has an infinite amount of paper, another has infinite tobacco. and the third has infinite matches. In order to provide a given smoker with the missing two resources, so he can roll a cigarette, a number of other processes synchronise with one another and with the smokers. At one time, only one smoker can acquire the missing two resources. Smokers cannot accumulate resources for future use. Several smokers can smoke at the same time, but each can smoke at most one cigarette at a time. The following pseudo-code shows a possible solution with nine processes: three *smokers*, three *pushers*, and three

A1) Show a possible execution that reaches LINE A. Be sure to indicate which instructions are executed by which process before LINE A is executed.

agents. All nine processes execute concurrently.

- A2) Is the mutex semaphore needed? What happens if we remove all occurrences of wait(mutex) and signal(mutex) from this solution?
- A3) Show how other possible synchronisation issues–in particular, **deadlock** and **starvation**–are solved (or show what synchronisation issues are unsolved, if any).

```
/* semaphores and shared global variables */
semaphore agentSem = 1, mutex = 1;
semaphore tobacco = 0, paper = 0, match = 0;
semaphore paper_and_matches = 0,
    tobacco_and_matches = 0,
    tobacco_and_paper = 0;
Boolean isPaper = FALSE, isTobacco = FALSE,
    isMatches = FALSE;
/* smoker with tobacco */
while(TRUE) {
    wait(paper_and_matches);
    make_cigarette();
    signal(agentSem);
                        /* LINE A */
    smoke();
3
/* smoker with paper */
while(TRUE) {
    wait(tobacco_and_matches);
    make_cigarette();
    signal(agentSem);
    smoke();
}
/* smoker with matches */
while(TRUE) {
    wait(tobacco_and_paper);
    make_cigarette();
    signal(agentSem);
    smoke();
```

}

```
/* tobacco agent */
while(TRUE) {
    wait(agentSem);
    signal(paper);
    signal(matches);
}
/* paper agent */
while(TRUE) {
   wait(agentSem);
    signal(tobacco);
    signal(matches);
}
/* matches agent */
while(TRUE) {
    wait(agentSem);
    signal(tobacco);
    signal(paper);
3
/* tobacco pusher */
while(TRUE) {
   wait(tobacco);
   wait(mutex);
    if(isPaper) {
        isPaper = FALSE;
        signal(tobacco_and_paper);
    }
    else if(isMatches) {
        isMatches = FALSE;
        signal(tobacco_and_matches);
    3
    else isTobacco = TRUE;
    signal(mutex);
}
/* paper pusher */
while(TRUE) {
    wait(paper);
    wait(mutex);
    if(isTobacco) {
        isTobacco = FALSE;
        signal(tobacco_and_paper);
    }
    else if(isMatches) {
        isMatches = FALSE;
        signal(paper_and_matches);
    }
    else isPaper = TRUE;
    signal(mutex);
}
/* matches pusher */
while(TRUE) {
   wait(matches);
   wait(mutex);
    if(isPaper) {
        isPaper = FALSE;
        signal(paper_and_matches);
   7
    else if(isTobacco) {
        isTobacco = FALSE:
        signal(tobacco_and_matches);
    else isMatches = TRUE;
    signal(mutex);
}
```

Second Midterm. May 13, 2013

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${ m Part \ I} \ { m Quizzes} \ (2 \ { m points})$

Mark each of the following statements **True** or **False**. Explain your answer in one sentence (if you wish).

Q1) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ A hashed page table contains, in each entry, a pointer to a list.

Explanation (optional):

Q2) T Deadlock cannot occur among processes that request (non-shareable) resources only when they have none.

Explanation (optional):

Q3) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ Paging permits pages to be of arbitrary size.

Explanation (optional):

Q4) **T** The **working-set model** is used to prevent thrashing while at the same time optimising CPU utilisation.

Explanation (optional):

Part II Open questions (3 points)

O1) How does the signal() operation on condition variables associated with monitors differ from the signal() operation defined for semaphores?

- O2) Under what circumstances do **page faults** occur? Describe the actions taken from the operating system when a page fault occurs.
- O3) Consider a system consisting of four resources of the same type that are shared by three processes, each of which needs at most two resources. Show that the system is **deadlock free**.

Part III Exercises (3 points)

E1) Consider the following snapshot of a system:

P_1 P_2 P_3 P_4	$\begin{array}{c} \underline{Allocation} \\ A \ B \ C \ D \\ 0 \ 0 \ 1 \ 2 \\ 1 \ 3 \ 5 \ 4 \\ 1 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 1 \end{array}$	$ \begin{array}{r} $	$\begin{array}{c} Request \\ \hline A \ B \ C \ D \\ 0 \ 0 \ 0 \ 1 \\ 1 \ 0 \ 0 \ 0 \\ 0 \ 1 \ 1 \ 0 \\ 2 \ 2 \ 0 \ 0 \end{array}$
- 4	$\frac{Available}{1\ 2\ 2\ 0}$		

- E1.1) Is the system in deadlock?
- E1.2) Is the system in a safe state?
- E1.3) Can P_2 's request be safely granted immediately?
- E1.4) If P_2 's request is granted immediately, does the system enter a deadlock?

Be sure to motivate your answers.

- E2) Consider a **logical address space** of 32 pages with 1,024 words per page, mapped onto a **physical memory** of 16 frames. How many bits are required in the logical address? How many bits are required in the physical address?
- E3) Consider the following reference string:

4, 2, 3, 4, 5, 3, 4, 1, 6, 7, 8, 9, 7, 8, 9, 5, 6, 5, 7, 5, 6.

Suppose you have **four page frames**. How may page faults occur for the LRU page replacement algorithm? Is that the minimum possible number of page faults?

Part IV Code analysis (3 points)

The **Cigarette-Smokers Problem** is a well-known process synchronisation problem that can defined as follows:

Consider a system with three *smoker* pro-Each smoker continuously rolls a cesses. cigarette (make_cigarette()) and then smokes it (smoke()). But to roll a cigarette, the smoker needs three resources: tobacco, paper, and matches. One of the *smokers* has an infinite amount of paper, another has infinite tobacco. and the third has infinite matches. In order to provide a given smoker with the missing two resources, so he can roll a cigarette, a number of other processes synchronise with one another and with the smokers. At one time, only one smoker can acquire the missing two resources. Smokers cannot accumulate resources for future use. Several smokers can smoke at the same time, but each can smoke at most one cigarette at a time. The following pseudo-code shows a possible solution with nine processes: three *smokers*, three *pushers*, and three agents. All nine processes execute concurrently.

- A1) Show a possible execution that reaches LINE A. Be sure to indicate which instructions are executed by which process before LINE A is executed.
- A2) Is the mutex semaphore needed? What happens if we remove all occurrences of wait(mutex) and signal(mutex) from this solution?
- A3) Show how other possible synchronisation issues–in particular, **deadlock** and **starvation**–are solved (or show what synchronisation issues are unsolved, if any).

```
/* semaphores and shared global variables */
semaphore agentSem = 1, mutex = 1;
semaphore tobacco = 0, paper = 0, match = 0;
semaphore paper_and_matches = 0,
    tobacco_and_matches = 0,
    tobacco_and_paper = 0;
Boolean isPaper = FALSE, isTobacco = FALSE,
    isMatches = FALSE;
/* smoker with tobacco */
while(TRUE) {
    wait(paper_and_matches);
    make_cigarette();
    signal(agentSem);
    smoke();
3
/* smoker with paper */
while(TRUE) {
    wait(tobacco_and_matches);
    make_cigarette();
    signal(agentSem);
                        /* LINE A */
    smoke();
}
/* smoker with matches */
while(TRUE) {
    wait(tobacco_and_paper);
    make_cigarette();
    signal(agentSem);
    smoke();
}
```

```
/* tobacco agent */
while(TRUE) {
    wait(agentSem);
    signal(paper);
    signal(matches);
}
/* paper agent */
while(TRUE) {
   wait(agentSem);
    signal(tobacco);
    signal(matches);
}
/* matches agent */
while(TRUE) {
    wait(agentSem);
    signal(tobacco);
    signal(paper);
3
/* tobacco pusher */
while(TRUE) {
   wait(tobacco);
   wait(mutex);
    if(isPaper) {
        isPaper = FALSE;
        signal(tobacco_and_paper);
    }
    else if(isMatches) {
        isMatches = FALSE;
        signal(tobacco_and_matches);
    3
    else isTobacco = TRUE;
    signal(mutex);
}
/* paper pusher */
while(TRUE) {
    wait(paper);
    wait(mutex);
    if(isTobacco) {
        isTobacco = FALSE;
        signal(tobacco_and_paper);
    }
    else if(isMatches) {
        isMatches = FALSE;
        signal(paper_and_matches);
    }
    else isPaper = TRUE;
    signal(mutex);
}
/* matches pusher */
while(TRUE) {
   wait(matches);
   wait(mutex);
    if(isPaper) {
        isPaper = FALSE;
        signal(paper_and_matches);
   7
    else if(isTobacco) {
        isTobacco = FALSE:
        signal(tobacco_and_matches);
    else isMatches = TRUE;
    signal(mutex);
}
```

First+Second Midterm. May 13, 2013

Q6)

Q8)

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 Name
 Q7)

 Registration No.
 Q7)

 E-mail
 Q7)

Part I Quizzes (4 points)

Mark each of the following statements **True** or **False**. Explain your answer in one sentence (if you wish).

Q1) T A rendezvous can be obtained using a blocking send() and a blocking receive().

Explanation (optional):

Q2) T A disadvantage of the M:M threading model is that developers cannot create as many threads as necessary, since kernel threads cannot run in parallel on a multiprocessor.

Explanation (optional):

Q3) T Immediately after a fork() is executed, the child process and the parent process have no shared variables.

Explanation (optional):

Q4)TNamed pipes continue to exist even after the
processes have finished communicating and have
terminated.

Explanation (optional):

Q5) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ Paging eliminates internal fragmentation.

Explanation (optional):

TDeadlock cannot occur among processes thatFneed at most one (non-shareable) resource each.

Explanation (optional):

T The working-set model is used to prevent thrashing while at the same time optimising CPU utilisation.

Explanation (optional):

TA hashed page table contains, in each entry,Fa pointer to a list.

Explanation (optional):

Part II Open questions (7 points)

- O1) Illustrate the **modular kernel** approach to OS design. Comment on advantages and disadvantages.
- O2) There are many possible CPU-scheduling algorithms. How could we select one particular algorithm for a particular system? Discuss various **evaluation methods**.
- O3) Under what circumstances do **page faults** occur? Describe the actions taken from the operating system when a page fault occurs.
- O4) Explain how data can be transferred from a device to the main memory using a **direct memory access** (**DMA**) controller.
- O5) Consider a system consisting of four resources of the same type that are shared by three processes, each of which needs at most two resources. Show that the system is **deadlock free**.

Part III Exercises (6 points)

E1) Suppose that processes P_1, P_2, \ldots, P_5 arrive for execution at the times indicated in Table 1. Each process will run for the amount of time listed, and will be assigned a priority ranging from **0** (highest) to **10** (lowest). No more processes will arrive until the last process completes.

Table 1: Process arrival/CPU-burst times and priorities.

Process	<u>Arrival Time</u>	<u>Burst Time</u>	<u>Priority</u>
P_1	0.0	8	7
P_2	0.4	4	2
P_3	0.5	1	7
P_4	0.8	2	1
P_5	1.0	2	5

Draw **four Gantt charts** that illustrate the execution of these processes using the following scheduling algorithms:

- E1.1) nonpreemptive SJF;
- E1.2) preemptive SJF;
- E1.3) preemptive priority (FCFS if priority is equal);
- E1.4) RR (quantum=4).

In answering the questions, base all decisions on the information you have at the time the decision must be made.

E2) Consider the following snapshot of a system:

$P_1 \\ P_2 \\ P_3 \\ P_4$	$\begin{array}{c} \underline{Allocation} \\ A \ B \ C \ D \\ 0 \ 0 \ 0 \ 1 \\ 0 \ 0 \ 1 \ 2 \\ 1 \ 3 \ 5 \ 4 \\ 1 \ 0 \ 0 \ 0 \end{array}$	$\begin{array}{c} \underline{Max} \\ A \ B \ C \ D \\ 2 \ 2 \ 0 \ 1 \\ 0 \ 0 \ 2 \ 3 \\ 2 \ 3 \ 5 \ 6 \\ 1 \ 2 \ 2 \ 0 \end{array}$	$\begin{array}{c} \underline{Request} \\ A \ B \ C \ D \\ 2 \ 2 \ 0 \ 0 \\ 0 \ 0 \ 1 \\ 1 \ 0 \ 0 \ 0 \\ 0 \ 1 \ 1 \ 0 \end{array}$
	$\frac{Available}{1\ 2\ 2\ 0}$		

- E1.1) Is the system in deadlock?
- E1.2) Is the system in a safe state?
- E1.3) Can P_3 's request be safely granted immediately?
- E1.4) If P_3 's request is granted immediately, does the system enter a deadlock?

Be sure to motivate your answers.

E3) Consider the following reference string:

1, 2, 3, 4, 5, 3, 4, 1, 6, 7, 8, 7, 8, 9, 7, 8, 9, 5, 4, 5, 4, 2.

Suppose you have **four page frames**. How may page faults occur for the LRU page replacement algorithm? Is that the minimum possible number of page faults?

Part IV Code analysis (5 points)

- C1) The program below uses the Phreads API.
 - C1.1) What would be the output from the program at LINE A, LINE B, and LINE C?
 - C1.2) How many processes/threads would be active by the time LINE B is executed?

Be sure to justify your answers.

```
#include <sys/types.h>
#include <sys/wait.h>
#include <pthread.h>
#include <stdio.h>
#include <unistd.h>
int val = 10;
void *runner(void *param);
int main()
ſ
   pid_t pid;
   pthread_t tid;
   pthread_attr_t attr;
   printf("A: value = %d\n", val); /* LINE A */
   pid = fork();
   if (pid == 0) {
      pthread_attr_init(&attr);
      pthread_create(&tid,&attr,runner,NULL);
      pthread_join(tid,NULL);
      printf("B: value = %d\n", val); /* LINE B */
      return 0;
   }
   else if (pid > 0) {
      wait(NULL);
      printf("C: value = %d\n", val); /* LINE C */
      return 0:
   }
   return 0;
}
void *runner(void *param) {
   val += 20;
   pthread_exit(0);
}
```

C2) The **Cigarette-Smokers Problem** is a well-known process synchronisation problem, defined as follows:

Consider a system with three *smoker* processes. Each smoker continuously rolls a cigarette (make_cigarette()) and then smokes it (smoke()). But to roll a cigarette, the smoker needs three resources: tobacco, paper, and matches. One of the *smokers* has an infinite amount of paper, another has infinite tobacco, and the third has infinite matches.

In order to provide a given smoker with the missing two resources, so he can roll a cigarette, a number of other processes synchronise with one another and with the smokers.

At one time, only one smoker can acquire the missing two resources. Smokers cannot accumulate resources for future use. Several smokers can smoke at the same time, but each can smoke at most one cigarette at a time.

The following pseudo-code shows a possible solution with nine processes: three *smokers*, three *pushers*, and three *agents*. All nine processes execute concurrently.

- C2.1) Show a possible execution that reaches LINE A. Be sure to indicate which instructions are executed by which process before LINE A is executed.
- C2.2) Is the mutex semaphore needed? What happens if we remove all occurrences of wait(mutex) and signal(mutex) from this solution?
- C2.3) Show how other possible synchronisation issuesin particular, **deadlock** and **starvation**-are solved (or show what synchronisation issues are unsolved, if any).

```
/* semaphores and shared global variables */
semaphore agentSem = 1, mutex = 1;
semaphore tobacco = 0, paper = 0, match = 0;
semaphore paper_and_matches = 0,
    tobacco_and_matches = 0,
    tobacco_and_paper = 0;
Boolean isPaper = FALSE, isTobacco = FALSE,
    isMatches = FALSE;
/* smoker with tobacco */
while(TRUE) {
    wait(paper_and_matches);
    make_cigarette();
    signal(agentSem);
    smoke();
}
/* smoker with paper */
while(TRUE) {
    wait(tobacco_and_matches);
    make_cigarette();
    signal(agentSem);
    smoke();
}
/* smoker with matches */
while(TRUE) {
    wait(tobacco_and_paper);
    make_cigarette();
    signal(agentSem);
                        /* LINE A */
    smoke();
```

}

```
/* tobacco agent */
while(TRUE) {
    wait(agentSem);
    signal(paper);
    signal(matches);
7
/* paper agent */
while(TRUE) {
    wait(agentSem);
    signal(tobacco);
    signal(matches);
}
/* matches agent */
while(TRUE) {
    wait(agentSem);
    signal(tobacco);
    signal(paper);
}
/* tobacco pusher */
while(TRUE) {
    wait(tobacco);
    wait(mutex);
    if(isPaper) {
        isPaper = FALSE;
        signal(tobacco_and_paper);
    }
    else if(isMatches) {
        isMatches = FALSE;
        signal(tobacco_and_matches);
    }
    else isTobacco = TRUE;
    signal(mutex);
}
/* paper pusher */
while(TRUE) {
    wait(paper);
    wait(mutex);
    if(isTobacco) {
        isTobacco = FALSE;
        signal(tobacco_and_paper);
    }
    else if(isMatches) {
        isMatches = FALSE;
        signal(paper_and_matches);
    }
    else isPaper = TRUE;
    signal(mutex);
}
/* matches pusher */
while(TRUE) {
    wait(matches);
    wait(mutex);
    if(isPaper) {
        isPaper = FALSE;
        signal(paper_and_matches);
    }
    else if(isTobacco) {
        isTobacco = FALSE;
        signal(tobacco_and_matches);
    3
    else isMatches = TRUE;
    signal(mutex);
}
```

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Frequently used formulas and tables

Some of the following formulas and tables may be useful in solving some of the exercises.

Schedulability Analysis (Extended)

$$\begin{aligned} \forall i = 1, \dots, n \quad & \sum_{h:P_h > P_i} \frac{C_h}{T_h} + \frac{C_i + B_i}{T_i} \le i(2^{1/i} - 1) \\ \forall i = 1, \dots, n \quad & \prod_{h:P_h > P_i} \left(\frac{C_h}{T_h} + 1\right) \left(\frac{C_i + B_i}{T_i} + 1\right) \le 2 \\ \forall i = 1, \dots, n \quad & \sum_{h:P_h > P_i} \frac{C_h}{T_h} + \frac{C_i + B_i}{T_i} \le 1 \end{aligned}$$

Response Time Analysis (Extended)

$$\begin{cases} R_i^{(0)} = C_i + B_i + \sum_{k=1}^{i-1} C_k \\ R_i^{(s)} = C_i + B_i + I_i^{(s-1)} = C_i + B_i + \sum_{k=1}^{i-1} \left\lceil \frac{R_i^{(s-1)}}{T_k} \right\rceil C_k \end{cases}$$
Q4)

Processor Demand Test

$$g(0,L) = \sum_{i=1}^{n} \left\lfloor \frac{L - D_i + T_i}{T_i} \right\rfloor C_i$$
$$L^* = \frac{1}{1 - U} \sum_{i=1}^{n} (T_i - D_i) U_i$$

Tables

n	$n(2^{1/n}-1)$
1	1.000
2	0.828
3	0.780
4	0.757
5	0.743
6	0.735
7	0.279
8	0.724
9	0.721
10	0.718

Part I Quizzes (2 points)

Mark each of the following statements **True** or **False**. Explain your answer in one sentence (if you wish).

Q1) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ The Stack Resource Policy may stop a task allowed by the Non-Preemptive Protocol.

Explanation (optional):



 \mathbf{T}

 \mathbf{F}

 \mathbf{T}

 \mathbf{F}

Given a set of independent aperiodic tasks, with arbitrary arrival times, any algorithm that executes the tasks in order of nondecreasing relative deadlines is optimal with respect to minimising the maximum lateness.

Explanation (optional):

Q3) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ Push-through blocking cannot affect a highestpriority task.

Explanation (optional):

For independent preemptive periodic tasks under fixed priorities, the critical instant of a given task occurs when all higher priority tasks have all different activation times.

Explanation (optional):

Q5) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ The processor utilization's least upper bound U_{lub} distinguishes between feasible and infeasible task sets.

Explanation (optional):

Q6) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ EDF is a simpler but more rigid scheduling algorithm than Timeline scheduling.

Explanation (optional):

Part II Open questions (3 points)

- O1) Discuss the main properties of the Stack Resource Policy protocol.
- O2) Compare advantages and disadvantages of complete tree-search algorithms (such as Bratley's) with respect to heuristic algorithms (such as the one used in the *Spring* kernel) for real-time task scheduling.

Part III Exercises (6 points)

E1) Let $\Gamma_1 = \tau_1, \ldots, \tau_6$ be a set of preemptable, aperiodic tasks with precedence constraints, to be executed on a single-processor machine. **Figure 1** shows release time a_i , worst-case computation time C_i , absolute deadline d_i , relative to a_i , and precedence relations of each task τ_i in Γ_1 .

Γ_1	$ au_1$	$ au_2$	$ au_3$	$ au_4$	$ au_5$	$ au_6$
a_i	0	6	4	13	0	10
C_i	5	4	3	4	1	1
d_i	20	20	19	18	20	18
prec				$\tau_2 \to \tau_4$	$\tau_1 \rightarrow \tau_5$	$\tau_4 \rightarrow \tau_6$
				$\tau_3 \rightarrow \tau_4$		$\tau_5 \rightarrow \tau_6$

Figure 1: Characteristics of the Γ_1 task set.

Show the minimum lateness schedule for Γ_1 , using a Gantt chart. Be sure to motivate your answer.

E2) Consider a set of periodic tasks $\Gamma_2 = \tau_1, \ldots, \tau_4$, to be scheduled on a single-processor machine. Figure 2 shows period T_i and worst-case computation time C_i of each task τ_i .

Γ_2	T_i	C_i
$ au_1$	3	1
$ au_2$	4	1
$ au_3$	6	1
$ au_4$	12	2

Figure 2: Characteristics of the Γ_2 task set.

E2.1) Is Γ_2 feasible under fixed priorities?

E2.2) Is Γ_2 feasible under dynamic priorities?

Let us now assume the following relative deadlines for τ_2, τ_3, τ_4 : $D_2 = 2, D_3 = 5, D_4 = 10$, whereas $T_1 = D_1 = 3$. Let us call Γ'_2 this new task set (see **Figure 3**).

- E2.3) Is Γ'_2 feasible under fixed priorities?
- E2.4) Is Γ'_2 feasible under dynamic priorities?

Be sure to motivate your answer.

Γ_2'	T_i	C_i	D_i
$ au_1$	3	1	3
$ au_2$	4	1	2
$ au_3$	6	1	5
$ au_4$	12	2	10

Figure 3: Characteristics of the Γ'_2 task set.

E3) Consider a task set Γ_3 , composed of 5 periodic tasks τ_1, \ldots, τ_5 that share 4 resources a, b, c, d and execute on a single-processor machine. Γ_3 's tasks are represented in **Figure 4**. Each resource is accessed in mutual exclusion using the Priority Ceiling Protocol (PCP).

T 1	а			
T2	á	a	d	
T 3	C	ł	b	с
T 4	с		5	_
T5	t)	С	

Figure 4: Graphical representation of critical sections in Γ_3 .

Figure 5 shows phase Φ_i , period $T_i = D_i$, worst-case computation time C_i , and a description of the access windows to the shared resources of each task τ_i , in terms of start time $t(R_k)$ and duration δ_{i,R_k} of the critical section for each task τ_i and each resource R_k .

Γ_3	$ \Phi_i $	T_i	C_i	t(a)	$\delta_{i,a}$	$\mid t(b)$	$\delta_{i,b}$	t(c)	$\delta_{i,c}$	t(d)	$\delta_{i,d}$
$ au_1$	8	20	5	1	3						
$ au_2$	6	30	6	1	4					3	1
$ au_3$	4	40	6			3	1	5	1	1	4
$ au_4$	2	50	3					1	1		
$ au_5$	0	60	6			1	4	3	1		

Figure 5: Characteristics of the Γ_3 task set.

E3.1) Using a Gantt chart, show the schedule under RM+PCP, from time 0 until completion of the first instance of τ_5 . Below the Gantt chart, show how τ_5 's active priority p_5 evolves.

Final Exam. June 12, 2013



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Frequently used formulas and tables

Some of the following formulas and tables may be useful in solving some of the exercises.

Schedulability Analysis (Extended)

$$\begin{aligned} \forall i &= 1, \dots, n \quad \sum_{h: P_h > P_i} \frac{C_h}{T_h} + \frac{C_i + B_i}{T_i} \le i(2^{1/i} - 1) \\ \forall i &= 1, \dots, n \quad \prod_{h: P_h > P_i} \left(\frac{C_h}{T_h} + 1\right) \left(\frac{C_i + B_i}{T_i} + 1\right) \le 2 \\ \forall i &= 1, \dots, n \quad \sum_{h: P_h > P_i} \frac{C_h}{T_h} + \frac{C_i + B_i}{T_i} \le 1 \end{aligned}$$

Response Time Analysis (Extended)

$$\begin{cases} R_i^{(0)} = C_i + B_i + \sum_{k=1}^{i-1} C_k & Q4 \\ R_i^{(s)} = C_i + B_i + I_i^{(s-1)} = C_i + B_i + \sum_{k=1}^{i-1} \left\lceil \frac{R_i^{(s-1)}}{T_k} \right\rceil C_k \end{cases}$$

Processor Demand Test

$$g(0,L) = \sum_{i=1}^{n} \left\lfloor \frac{L - D_i + T_i}{T_i} \right\rfloor C_i$$
$$L^* = \frac{1}{1 - U} \sum_{i=1}^{n} (T_i - D_i) U_i$$

Tables

n	$n(2^{1/n}-1)$
1	1.000
2	0.828
3	0.780
4	0.757
5	0.743
6	0.735
7	0.279
8	0.724
9	0.721
10	0.718

Part I Quizzes (2 points)

Mark each of the following statements True or False. Explain your answer in one sentence (if you wish).

Under the Priority Ceiling Protocol, a task \mathbf{T} Q1) can be blocked only before it starts executing, \mathbf{F} never once it has started.

Explanation (optional):

 \mathbf{T} Q2) \mathbf{F}

For each task set, there exists always one and only one optimal scheduling algorithm (in the sense of feasibility).

Explanation (optional):

Preemption generally does not increase the Q3) complexity of a scheduling problem.

Explanation (optional):

For independent preemptive periodic tasks Т under fixed priorities, the critical instant of a \mathbf{F} given task occurs when all higher priority tasks have the same activation time as its own.

Explanation (optional):



A task set consisting of three tasks, τ_1 , τ_2 , and τ_3 , with identical period, is RM-feasible if and only if the total processor utilisation is at most

Explanation (optional):

т Q6)

Q5)

Priority Inversion is a phenomenon that cannot F occur if tasks are independent.

Explanation (optional):

Part II Open questions (3 points)

- O1) What are the main unsolved problems of the Priority Inheritance Protocol? Use examples to illustrate the point.
- O2) Compare advantages and disadvantages of RM with respect to EDF.

Part III Exercises (6 points)

E1) Let $\Gamma_1 = \tau_1, \ldots, \tau_6$ be a set of preemptable, aperiodic tasks with precedence constraints, to be executed on a single-processor machine. **Figure 1** shows release time a_i , worst-case computation time C_i , absolute deadline d_i , relative to a_i , and precedence relations of each task τ_i in Γ_1 .

Γ_1	$ au_1$	$ au_2$	$ au_3$	$ au_4$	$ au_5$	$ au_6$
a_i	0	6	4	13	0	10
C_i	5	4	3	4	1	1
d_i	20	20	19	18	20	18
prec				$\tau_2 \to \tau_4$	$\tau_1 \rightarrow \tau_5$	$\tau_4 \rightarrow \tau_6$
				$\tau_3 \rightarrow \tau_4$		$\tau_5 \to \tau_6$

Figure 1: Characteristics of the Γ_1 task set.

Show the minimum lateness schedule for Γ_1 , using a Gantt chart. Be sure to motivate your answer.

E2) Consider a set of periodic tasks $\Gamma_2 = \tau_1, \ldots, \tau_4$, to be scheduled on a single-processor machine. Figure 2 shows period T_i and worst-case computation time C_i of each task τ_i .

Γ_2	T_i	C_i
$ au_1$	3	1
$ au_2$	4	1
$ au_3$	6	1
$ au_4$	12	2

Figure 2: Characteristics of the Γ_2 task set.

E2.1) Is Γ_2 feasible under fixed priorities?

E2.2) Is Γ_2 feasible under dynamic priorities?

Let us now assume the following relative deadlines for τ_2, τ_3, τ_4 : $D_2 = 2, D_3 = 5, D_4 = 10$, whereas $T_1 = D_1 = 3$. Let us call Γ'_2 this new task set (see **Figure 3**).

E2.3) Is Γ'_2 feasible under fixed priorities?

E2.4) Is Γ'_2 feasible under dynamic priorities?

Be sure to motivate your answer.

Γ_2'	T_i	C_i	D_i
$ au_1$	3	1	3
$ au_2$	4	1	2
$ au_3$	6	1	5
$ au_4$	12	2	10

Figure 3: Characteristics of the Γ'_2 task set.

E3) Consider a task set Γ_3 , composed of 5 periodic tasks τ_1, \ldots, τ_5 that share 4 resources a, b, c, d and execute on a single-processor machine. Γ_3 's tasks are represented in **Figure 4**. Each resource is accessed in mutual exclusion using the Stack Resource Policy (SRP).

T 1		а		
T 2	á	a	d	
T 3	(ł	b	с
T 4	с]	
T5	t)	С	

Figure 4: Graphical representation of critical sections in Γ_3 .

Figure 5 shows phase Φ_i , period $T_i = D_i$, worst-case computation time C_i , and a description of the access windows to the shared resources of each task τ_i , in terms of start time $t(R_k)$ and duration δ_{i,R_k} of the critical section for each task τ_i and each resource R_k .

Γ_3	$ \Phi_i $	T_i	C_i	t(a)	$\delta_{i,a}$	$\mid t(b)$	$\delta_{i,b}$	t(c)	$\delta_{i,c}$	t(d)	$\delta_{i,d}$
$ au_1$	8	20	5	1	3						
$ au_2$	6	30	6	1	4					3	1
$ au_3$	4	40	6			3	1	5	1	1	4
$ au_4$	2	50	3					1	1		
$ au_5$	0	60	6			1	4	3	1		

Figure 5: Characteristics of the Γ_3 task set.

E3.1) Using a Gantt chart, show the schedule under EDF+SRP, from time 0 until completion of the first instance of τ_5 . Below the Gantt chart, show how the system ceiling Π_s evolves.

Standard Exam. June 12, 2013



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Frequently used formulas and tables

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Response Time Analysis (Extended)

$$\begin{cases} R_i^{(0)} = C_i + B_i + \sum_{k=1}^{i-1} C_k \\ R_i^{(s)} = C_i + B_i + I_i^{(s-1)} = C_i + B_i + \sum_{k=1}^{i-1} \left\lceil \frac{R_i^{(s-1)}}{T_k} \right\rceil C_k \end{cases}$$

Processor Demand Test

$$g(0,L) = \sum_{i=1}^{n} \left\lfloor \frac{L - D_i + T_i}{T_i} \right\rfloor C_i$$
$$L^* = \frac{1}{1 - U} \sum_{i=1}^{n} (T_i - D_i) U_i$$

Tables

n	$n(2^{1/n}-1)$
1	1.000
2	0.828
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7	0.279
8	0.724
9	0.721
10	0.718

Part I Quizzes (8 pts)

Mark each of the following statements True or False. Explain your answer in one sentence (if you wish).

In the indirect communication IPC scheme, a communication link may be associated with at \mathbf{F} most two processes.

Explanation (optional):



An advantage of multithreading is an increased responsiveness in interactive applications.

Explanation (optional):

 \mathbf{T} All named pipes created by a process P are Q3) automatically removed from the file system \mathbf{F} after P terminates.

Explanation (optional):

Paging eliminates external fragmentation. Q4) \mathbf{F}

Explanation (optional):

 \mathbf{T} Deadlock cannot occur among processes that Q5)need at most two (non-shareable) resources \mathbf{F} each.

Explanation (optional):

 \mathbf{T} The working-set model is used to prevent Q6)thrashing while at the same time optimising \mathbf{F} CPU utilisation.

Explanation (optional):



 \mathbf{T}

For independent preemptive periodic tasks with fixed priorities, the critical instant of a given task occurs when all higher priority tasks have the same activation time as its own.

Explanation (optional):

 $\begin{array}{c|c} \hline \mathbf{T} & \text{Preemption generally does not increase the} \\ \hline \mathbf{F} & \text{complexity of a scheduling problem.} \end{array}$

Explanation (optional):

Q9) $\begin{bmatrix} \mathbf{T} \\ \mathbf{F} \end{bmatrix}$ The processor utilization's least upper bound U_{lub} distinguishes between feasible and infeasible task sets.

Explanation (optional):

Q10) T Priority Inversion is a phenomenon that can occur only when there are tasks sharing non-preemptible resources.

Explanation (optional):

Q11) T Ceiling blocking cannot affect top-priority tasks.

Explanation (optional):

Q12) T Under the Priority Ceiling Protocol, a task can be blocked only before it starts executing, never once it has started.

Explanation (optional):

Part II Open questions (10 pts)

- O1) Describe the content of a Process Control Block.
- O2) Illustrate the Dining Philosophers Problem. Show a possible solution using semaphores. Discuss three different ways to prevent deadlock.
- O3) What are the Priority Inheritance Protocol's main unsolved problems? Use examples to illustrate the point.

Part III Exercises (13 pts)

E1) Consider the following reference string:

1, 2, 3, 4, 5, 3, 4, 1, 6, 7, 8, 7, 8, 9, 7, 8, 9, 5, 6, 5, 7.

Suppose you have four page frames. How may page faults occur for the LRU page replacement algorithm? Is that the minimum possible number of page faults?

Be sure to motivate your answer.

E2) Let $\Gamma_2 = \tau_1, \ldots, \tau_6$ be a set of nonpreemptable, aperiodic and synchronous tasks with precedence constraints, to be executed on a single-processor machine. **Figure 1** shows worst-case computation time C_i , absolute deadline d_i , and precedence relations of each task τ_i in Γ_2 .

Γ_2	$ au_1$	$ au_2$	$ au_3$	$ au_4$	$ au_5$	$ au_6$
C_i	5	4	3	4	1	1
d_i	20	20	19	18	20	18
prec				$\tau_2 \rightarrow \tau_4$	$\tau_1 \rightarrow \tau_5$	$\tau_4 \rightarrow \tau_6$
				$\tau_3 \rightarrow \tau_4$		$\tau_5 \rightarrow \tau_6$

Figure 1: Characteristics of the Γ_2 task set.

Show the minimum lateness schedule for Γ_2 , using a Gantt chart.

Be sure to motivate your answer.

E3) Consider a task set Γ_3 , composed of 5 periodic tasks τ_1, \ldots, τ_5 that share 4 resources a, b, c, d and execute on a single-processor machine. Γ_3 's tasks are represented in **Figure 2**. Each resource is accessed in mutual exclusion using the Priority Ceiling Protocol (PCP).

T1		а		
T 2	á	1	d	
T 3	C	ł	b	с
T 4	с		Г	_
T 5	t)	С	

Figure 2: Graphical representation of critical sections in Γ_3 .

Figure 3 shows phase Φ_i , period $T_i = D_i$, worst-case computation time C_i , and a description of the access windows to the shared resources of each task τ_i , in terms of start time $t(R_k)$ and duration δ_{i,R_k} of the critical section for each task τ_i and each resource R_k .

Γ_3	$ \Phi_i $	T_i	C_i	t(a)	$\delta_{i,a}$	$\mid t(b)$	$\delta_{i,b}$	$\mid t(c)$	$\delta_{i,c}$	t(d)	$\delta_{i,d}$
$ au_1$	8	20	5	1	3						
$ au_2$	6	30	6	1	4					3	1
$ au_3$	4	40	6			3	1	5	1	1	4
$ au_4$	2	50	3					1	1		
$ au_5$	0	60	6			1	4	3	1		

Figure 3: Characteristics of the Γ_3 task set.

- E3.1) What is the worst-case blocking time B_i for each task $\tau_i \in \Gamma_3$?
- E3.2) Is Γ_3 feasible with RM+PCP?
- E3.3) Using a Gantt chart, show the schedule under RM+PCP, from time 0 until completion of the first instance of τ_5 . Below the Gantt chart, show how τ_5 's active priority p_5 evolves.

Be sure to motivate your answer.