## UNIVERSITY OF BOLOGNA – FACULTY OF ENGINEERING INTERNATIONAL MASTER COURSE IN CIVIL ENGINEERING 2010/2011 \*\*\* Finite Element Analysis \*\*\*

## LAB 2: 2D ELLIPTIC PROBLEMS

Download from <u>http://campus.cib.unibo.it/cgi/lista</u> (ricerca per docente -> Lanza) the **FEA\_LAB2.zip** file, then unzip it.

In FreeFem++, find approximate solutions of the following 2-D elliptic BVP (Boundary Value Problem) by means of the GFEM (Galerkin Finite Element Method) with linear and quadratic elements:

1) Homogeneous Dirichlet BVP:

$$\begin{cases} -\Delta u(x, y) = f(x, y) & (x, y) \in \Omega = unit \ circle & Poisson's \ equation \\ u(x, y) = 0 & (x, y) \in \partial\Omega & Homogeneous \ Dirichlet \ Boundary \ Conditions \end{cases}$$

where f(x, y) = 1

Compare the approximate solutions obtained by changing the domain triangulation (compute the  $L^2$  and  $H^1$  errors) with the exact solution:

$$u(x, y) = \frac{1 - x^2 - y^2}{4}$$