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1 **Title: Analysis of Time-dependent Deformation in Tunnels using the Convergence-**  
2 **Confinement Method**

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9 Key words:

10 *long-term behaviour, time-dependency, creep, visco-elastic parameters*

11

12 **ABSTRACT**

13 During the excavation of a tunnel the accumulated wall displacement and the loading of tunnel  
14 support is the result of both the tunnel advance (round length and cycle time) and the time-  
15 dependent behaviour of the surrounding rock mass. The current approach to analyze the tunnel  
16 wall displacement increase is based on the Convergence-Confinement Method (CCM) performed  
17 with either analytical (closed form solutions) or the usage of the Longitudinal Displacement  
18 Profiles. This approach neglects the influence of time-dependency resulting in delayed  
19 deformation that may manifest even minutes or hours after excavation. Failure to consider the  
20 added displacements in the preliminary design can result in false selecting the time of installation  
21 and the type of support system causing safety issues to the working personnel, leading to cost  
22 overruns and project delivery delays. This study focuses on investigating and analyzing the total  
23 displacements around a circular tunnel in a visco-elastic medium by performing an isotropic  
24 axisymmetric finite difference modelling, proposing a new yet simplified approach that  
25 practitioners can use taking into account the effect of time.

26 **1 INTRODUCTION**

27 Understanding the nature and origin of deformations due to an underground opening requires, as  
28 Panet (1993) noted, both knowledge of the rock-support interaction and interpretation of field data.  
29 Monitoring and measurement of tunnel wall displacements has shown that deformation initiates  
30 during excavation and may continue long after the tunnel construction is completed. This tunnel

31 wall movement, also known as convergence, is the result of both the tunnel face advancement  
32 and the time-dependent behaviour of the rock mass. Many researchers (Fenner, 1938; Parcher,  
33 1964; Lombardi, 1975; Brown et al. 1983; Corbetta et al. 1991; Duncan-Fama, 1993; Panet, 1993,  
34 1995; Peila and Oreste, 1995; Carranza and Fairhurst, 2000, Alejano et al. 2009; Vrakas and  
35 Angnostou, 2014; Cai et al. 2015; Cui et al. 2015 etc.) have studied the interaction between the  
36 rock mass and the applied support. They have proposed various methodologies that are  
37 commonly used as a preliminary tool for quickly assessing the system behaviour (between the  
38 surrounding rock mass and support) during both the design and construction process of  
39 underground projects (Gschwandtner and Galler, 2009). In addition, most of these solutions are  
40 based on the well-known and widely used Convergence-Confinement Method (CCM). CCM is a  
41 two-dimensional simplified approach that can be used to simulate three-dimensional problems as  
42 the rock-support interaction in tunnels. More specifically, CCM is widely utilized to estimate the  
43 required load capacity of the proposed support system. The traditional approach of this  
44 methodology involves the Ground Reaction Curve and the Longitudinal Displacement Profile that  
45 when used in combination with the Support Characteristic Curve (SCC) they provide information  
46 on the required support load in regards to the tunnel face location as a percentage of the  
47 anticipated maximum tunnel wall displacement. Gschwandtner and Galler (2010) suggested a  
48 new approach for using the CCM while considering the time-dependent material of the support  
49 by investigating different support scenarios of rockbolts and shotcrete, investigating how the  
50 behaviour of the support system changes over time. However, even the more commonly applied  
51 simplified formulations of CCM do not explicitly capture the time-dependent component of rock  
52 mass deformation. Time-dependent closure, for instance due to creep, can have a significant  
53 impact on support loading. Failure to account for these additional loads and deformations can  
54 result in unexpected failures, causing safety issues for the working personnel, leading to cost  
55 overruns and project delivery delays. Questions of the applicability of such methods when dealing  
56 with time-dependent rheological rockmasses are addressed in this paper by investigating the total  
57 observed displacement on tunnel walls in an isotropic visco-elastic medium, taking into  
58 consideration both the tunnel advancement and cumulated deformation due to the rheological  
59 behaviour of the material over time.

## 60 **1.1 Ground Reaction Curve (GRC) and Longitudinal Displacement Profile (LDP)** 61 **Calculations**

62 An important component of the CCM method is the Ground Reaction Curve (GRC). This is a  
63 characteristic line that records the decrease of an apparent (fictitious) internal (radial) support  
64 pressure, from the in situ pressure to zero when considering the unsupported case of a circular

65 tunnel after excavation. This pressure reflects the tunnel excavation process as the tunnel is being  
66 excavated (out-of-section) past the section of interest and continues to be excavated beyond the  
67 reference position (usually the location of the tunnel face) as shown on the right part of Figure 1.  
68 The internal pressure ( $p_i$ ) acts radially on the tunnel profile (from the inside) and represents the  
69 support resistance needed to hinder any further displacement at that specific location  
70 (Vlachopoulos and Diederichs, 2009). In reality, this pressure represents an idealized sum of the  
71 contribution of the nearby unexcavated tunnel core (surrounding rock mass) and any applied  
72 support installed and is zero for a fully excavated unsupported tunnel. The GRC depends on the  
73 rock mass behaviour. It is assumed to be linear for an elastic material but it varies if the material  
74 is elasto-plastic or visco-elastic etc. Many researchers have studied the GRC responses of  
75 different materials. For example, Brown et al. 1983, Alejano et al. 2009, Wang et al. 2010,  
76 Gonzales-Cao et al. 2013 have proposed analytical solutions for strain-softening rock masses  
77 based on different GRCs. Vrakas (2017) proposed a finite strain semi-analytical solution for the  
78 ground response problem of a circular tunnel in elasto-plastic medium with non-linear strength  
79 envelopes. Panet (1993) gives examples of GRCs of the most used visco-elastic models that are  
80 discussed in Section 2.2.

81 For elastic or moderately yielding rock masses approximately one third of the total displacement  
82 is observed at the tunnel face (Hoek et al. 2008) shown as  $x=0$  on the right hand axis of Figure 1.  
83 The deformation initiates in front of the face ( $x<0$ ), usually one to two tunnel diameters ahead of  
84 the face, and reaches its maximum magnitude at three to four tunnel diameters away from the  
85 face inside the tunnel ( $x>0$ ).

86 A Longitudinal Displacement Profile (LDP) of the tunnel closure is a graphical representation of  
87 the progression of the tunnel wall displacement (radial) at the reference section as the tunnel  
88 advances to and beyond this section. The reference datum ( $x=0$ ) indicates that the tunnel face is  
89 stationed at the reference section (Figure 1). LDPs are calibrated for a simplified unsupported  
90 tunnel and are then used in combination with the GRC to determine the support system required  
91 for the stability of the tunnel walls as well as the time of support installation.

92

93 Figure 1. The Ground Reaction Curve response of an elasto-plastic material and its relation to  
94 the LDP. Y-axis on the left refers to the internal pressure ( $p_i$ ) normalized to the in-situ pressure  
95 ( $p_0$ ), Y-axis on the right refers to the distance from the face ( $x$ ) normalized to the tunnel radius ( $R$ )  
96 and X-axis refers to the radial displacement at a location  $x$  normalized to the maximum radial  
97 displacement.

98 *It should be noted that in Figure 1 no time-dependent component is taken into consideration in*  
99 *this example.*

100 LDPs are initially calculated using analytical solutions or numerical analysis. In two-dimensional  
101 numerical analysis, LDPs are calculated through two-dimensional axisymmetric models for  
102 homogeneous and isotropic initial stress condition circular tunnels. Table 1 summarizes the  
103 various analytical solutions proposed by researchers (Panet and Guenet, 1982; Corbetta et al.  
104 1991; Panet, 1993, 1995; Chern et al. 1998; Unlu and Gercek, 2003; Vlachopoulos and  
105 Diederichs, 2009) to be used for LDP calculations according to the rock mass behaviour (i.e.  
106 elastic or elasto-plastic) where  $u_{\max}$  refers to the maximum radial displacement attained R and x  
107 denote the tunnel radius and x the under-investigation location,  $\nu$  is the Poisson's ratio.

108 Table 1. Analytical solutions for LDP calculation depending on the medium.

109 Panet (1993, 1995) and Corbetta et al. (1991) derived relationships for the LDP profiles of elastic  
110 material behaviours. Panet and Guento (1982) Chern et al (1998) proposed relationships for  
111 elato-plastic materials. Unlu and Gercek (2003) are the first who noted that the LDP curve in front  
112 of the face (in the non-excavated rock mass where  $x < 0$ ) is different than the LDP curve in behind  
113 the tunnel face (in the already-excavated rock mass where  $x > 0$ ). At the tunnel face (where  $x = 0$ )  
114 the radial displacement can be estimated using the Poisson's Ratio, as shown in Table 1. The  
115 same statement was used by Vlachopoulos and Diederichs (2009) who proposed three different  
116 equations to estimate the LDP for an elasto-plastic material in relation to the location x in terms  
117 of the tunnel face which is used for weak ground conditions at great depth assuming that a large  
118 ultimate plastic radius is created around the tunnel. It is important to note that none of the afore-  
119 ascribed LDP equations on Table 1 takes into consideration any deformation anticipated due to  
120 time-dependent squeezing (for instance). Additionally, any application of these LDPs equations  
121 to time-dependent rock masses will yield erroneous results leading to underestimation of the  
122 anticipated tunnel wall displacements and the support system requirements.

## 123 **2 TIME-DEPENDENT BEHAVIOUR**

124 The tendency of various rocks and rock masses to exhibit time-dependent shear deformation  
125 when subjected to a constant stress state (that it is less than the strength of the rock material) is  
126 known as creep. In tunnelling, creep behaviour emerges as the on-going increase of the radial  
127 displacements observed in the tunnel walls. This increase is related to the rheological properties  
128 and creep potential of the surrounding rock mass and can be considered to be in addition to the  
129 displacement resulting due to the incremental steps of tunnel advance - although the progress of  
130 the tunnel takes time and so this closure component is often but erroneously referred to as time-

131 dependent (Paraskevopoulou, 2016). For the design of tunnels in rock masses at depth it is often  
132 important to account for creep. This consideration extends through the initial construction period  
133 and beyond. The time effect can contribute up to 70% of the total deformation (Sulem et al. 1987).

134 In tunnelling, time-dependent behaviour is often observed in weak rocks and rock masses that  
135 exhibit severe squeezing (Barla 2001, Barla et al. 2010). Squeezing in this case, results from the  
136 plastic displacements due to shearing over a long period of time which leads to apparent visco-  
137 plastic creep. However, brittle rocks can experience creep when subjected to high in situ stresses  
138 (Malan, 1997; Damjanac and Fairhurst, 2010) and can also be subject to long-term strength  
139 degradation due to crack growth over time with or without observable creep. Creep behaviour  
140 (Goodman, 1980) is usually characterized by three stages (primary, secondary, tertiary) that  
141 follow the instantaneous response due to the change in the boundary conditions (constant stress)  
142 shown in Figure 2. As the stress or load is kept constant, the accumulated strains increase with  
143 a decreasing rate (primary stage). When this primary stage subsides and the strain increase  
144 approaches a constant strain-rate, the transition to the secondary (or steady state) can then be  
145 evident (although the processes of secondary creep may act coincidentally during the primary  
146 stage). At the end of the secondary state, the strain rate accelerates yielding or even failing the  
147 material in a brittle manner, a delayed yield process referred to as tertiary creep (although the use  
148 of the term creep may not be accurate in all cases). This failure is the result of weakening of the  
149 rock mass during creep deformation or excess deformations that create unstable conditions. It  
150 should be also noted that the magnitude and duration of each stage depends on the type of the  
151 rock material. Ductile materials such as rock salt may never reach tertiary creep (yield) as they  
152 are more prone to deforming without yielding (creep processes do not create damage) whereas  
153 in brittle materials like granite the secondary stage of creep is not always observed as Lockner  
154 (1993) also reported. In these materials, the tertiary stage manifests as delayed yield under  
155 sustained loading between a lower bound crack initiation threshold and maximum strength.

156 **Figure 2. Characteristic curve of creep behaviour.**

## 157 **2.1 Time-dependent Formulation and Rheological Models**

158 **Many researchers have developed and proposed various formulations and constitutive laws to**  
159 **capture the time-dependent behaviour of rock materials. Most formulations of time-dependent**  
160 **behaviour, suggested in the literature, can be separated into three main categories: a) empirical**  
161 **functions based upon curve fitting of experimental data (Mirza, 1978; Aydan et al. 1996; Sign et**  
162 **al. 1997; etc.), b) rheological functions based upon time-dependent behaviour models (Lo and**  
163 **Yuen, 1981; Aristorenas, 1992; Malan, 1997; Chin and Rogers, 1998; etc.), and, c) general**

164 theories (Perzyna, 1996; Debernardi, 2008; Sterpi and Gioda, 2009; Kalos, 2014; etc.) that are  
165 considered to be the most advanced aspects of numerical analysis codes (i.e. Finite Element and  
166 Finite Difference codes). The most commonly used of the three are the rheological models. They  
167 are based on constitutive relationships between stress and strain. In order to simulate the time-  
168 dependent viscous behaviour, usually elastic springs, viscous dashpots and plastic sliders are  
169 coupled in series or parallel. It is then possible to reproduce elasto-plastic, visco-elastic, visco-  
170 plastic, elasto-visco-plastic etc. mechanical behaviours. For simplicity here, it should be noted  
171 that at this paper focuses on the visco-elastic behaviour and no plastic yield is considered.

172 Table 2 summarizes the most common visco-elastic models used to simulate creep behaviour,  
173 where:  $\sigma$ =stress,  $\epsilon$ =strain,  $E$ =Young's modulus,  $K$ =bulk modulus,  $G$  =shear modulus,  $\eta$ =viscosity,  
174  $t$ =time, subscript K denotes Kelvin model, subscript M denotes Maxwell model,  $p$  is the mean  
175 stress and  $q$  is the deviatoric stress. Kelvin and most commonly its extension to the generalized  
176 Kelvin (Kelvin-Voigt) model comprised of a spring coupled in parallel with a dashpot is used to  
177 simulate the instantaneous response and primary stage of creep. Maxwell model or its extension  
178 (generalized Maxwell), a spring in series with a dashpot is used to capture the secondary creep  
179 stage. Coupling of these two models in series gives the Burgers model that is used to simulate  
180 the first two stages of creep behaviour. These models in order to be utilized, require the  
181 knowledge of creep parameters (i.e. viscosities ( $\eta$ ) and shear moduli ( $G$ ) of the mechanical  
182 analogues) that can be derived from creep tests in the laboratory (Lama and Vutukuri, 1978;  
183 Goodman, 1980) or in situ conditions (Goodman, 1980; Chen and Chung, 1996). According to  
184 Goodman, the visco-elastic parameters ( $\eta_K$ ,  $\eta_M$ ,  $G_K$ ,  $G_M$ ) can be estimated by fitting the  
185 experimental results of static load (creep) tests to the mathematical curve of the strain response  
186 of the Burgers model at different time increments and the corresponding strain intercepts.

187 Burgers-creep viscous (CVISC) model (Table 2) is a visco-elastic-plastic model introduced by  
188 Itasca (2011) and consists of the Burgers visco-elastic model in series with a plastic slider (Table  
189 2). The plastic component is based on the Mohr-Coulomb failure criterion and it is used to pseudo-  
190 simulate the tertiary stage of creep. However, since the plastic slider is not coupled with a viscous  
191 dashpot plastic-yielding is independent of time and depends only on the stress (Paraskevopoulou  
192 and Diederichs, 2013). If the model is subjected to a stress above the yielding stress of the slider  
193 the model behaves as an elasto-plastic material whereas if it is stressed below the yielding  
194 threshold the model behaves similar to a Burgers body.



195 Commonly, Burgers model is preferable for practical applications (Goodman, 1980). It should be  
196 stated, however, that there is not a simple model that can describe all the creep stages  
197 satisfactorily and can be used for all rock types and all in situ conditions without limitations. For  
198 instance, heavily sheared rock masses can exhibit primary creep in normal stress conditions  
199 whereas high strength materials will not (Paraskevopoulou and Diederichs, 2013).

200 **Table 2. Visco-elastic rheological models, their associated mechanical analogues, stress-strain**  
201 **and time-relationships.**

202 *(It should be noted that for incompressible materials  $E=3G$ ).*

## 203 **2.2 Time-dependent Deformation in Tunnelling**

204 The time-dependent response around the tunnel in a visco-elastic material has also been  
205 discussed in the literature. **Analytical and closed form solutions that take into account the time-**  
206 **dependent convergence have been proposed in viscous medium for supported (i.e. Sakurai,**  
207 **1978; Pan and Dong, 1991) and unsupported (i.e Panet, 1979; Sulem et al., 1987; Fahimifar, et**  
208 **al. 2010;) circular tunnels. Gnirk and Jonson (1964) analyzed the deformational behaviour of a**  
209 **circular mine shaft in a visco-elastic medium under hydrostatic stress. Goodman (1980) described**  
210 **a methodology on estimating visco-elastic creep parameters based on curve-fitting of tunnel data**  
211 **that experienced creep defromation. Yiouta-Mitra et al. (2010) investigated the LDP of a circular**  
212 **tunnel in a visco-elastic medium, neglecting however the effect on the cumulative tunnel wall**  
213 **displacement due to the tunnel advancement. Nomikos et al. (2011) performed axisymmetric**  
214 **analyses on supported tunnel within linear visoc-elastic rock masses. Although some of these**  
215 **formulations do consider the tunnel advance in the estimated total deformation, yet are found to**  
216 **be impractical due to the complex calculations required.**

217 In this paper, the linear visco-elastic analytical solutions developed by Panet (1979) and proposed  
218 for the Kelvin-Voigt and Maxwell models, are utilized for the calculation of the time-dependent  
219 radial displacements of an unsupported circular tunnel. Fahimifar et al. (2010) developed a  
220 closed-form solution considering the time-effect when tunnelling within a Burgers material, this  
221 formulation is also adopted in the presented analysis. Table 3 summarizes the mathematical  
222 representations and expected material response due to time and more specifically creep  
223 behaviour; the visco-elastic models are presented as well as their analytical solutions and the  
224 radial displacement – time relationships, where:  $\sigma_0$  is the in situ stress,  $\sigma_r$  is the radial stress,  $u_r$   
225 refers to the radial tunnel wall displacement,  $r$  is the tunnel radius,  $t$  describes the time,  $T$  denotes  
226 the retardation – relaxation time of each model,  $G$  is the shear modulus,  $\eta$  is the viscosity,  $t$ =time,



227 subscripts K, M and  $\infty$  refer to Kelvin-Voigt model, Maxwell model and the harmonic average,  
228 respectively.

229 **Table 3. Visco-elastic models and analytical solutions for a circular unsupported tunnel. The**  
230 **analytical solutions for Kelvin-Voigt and Maxwell model are adopted from Panet (1979) and for**  
231 **Burgers from Fahimifar et al. (2010).**

232 It should be noted that when time is assumed to be infinite the shear modulus used in the Kelvin  
233 model is estimated with the harmonic average  $G_\infty$  and is not equal with the initial shear modulus  
234 of the rock mass  $G_0$ .

### 235 **2.3 Combining the two effects in a Longitudinal Displacement Profile (LDP)**

236 The effects of tunnel advancement and time in the total radial displacements observed in the  
237 tunnel walls are shown in Figures 5 and 6 and expressed in the form of the LDP of an unsupported  
238 circular tunnel in an elasto visco-elastic-plastic and an elasto-visco-elastic medium respectively.  
239 In Figures 3 and 4,  $r$  is the tunnel radius,  $D$  is the tunnel diameter,  $t$  denotes the time,  $x$  denotes  
240 the distance from the tunnel face which is a function of time,  $u_r$  refers to the radial tunnel wall  
241 displacement which is the function of time and distance from the tunnel face,  $G$  is the shear  
242 modulus,  $\eta$  is the viscosity,  $q$  is the deviatoric stress,  $\sigma$  is the applied stress, subscripts M, K,  $y$   
243 refer to Kelvin and Maxwell models and yielding threshold respectively; superscripts el, p, s and  
244 tet denotes the elastic response and primary, secondary and tertiary components of the creep  
245 behaviour, respectively. The former case (Figure 3) represents the case (elasto-visco-elastic-  
246 plastic) where the material undergoes all three stages of creep until ultimate failure. This response  
247 is expected in severe squeezing rock masses where the induced-creep behaviour leads the  
248 material to fracture and failure after exhibiting large deformations and noticeable convergence.

249 **Figure 3. Longitudinal Displacement Profile (LDP) in an elasto-visco-elastic-plastic medium (see**  
250 **text for details).**

251 Figure 4 illustrates the anticipated LDP of the tunnel displacement in an elasto-visco-elastic  
252 medium where no tertiary creep takes place. More ductile materials as in the case of rock salt can  
253 behave in such manner.

254 **Figure 4. Schematic representation of the Longitudinal Displacement Profile (LDP) in an elasto-**  
255 **visco-elastic medium (see text for details).**

256 In both Figures 3 and 4, it is shown that when no time-effect is considered, the total displacements  
257 are underestimated which can lead to erroneous calculations at the initial stages of the design

258 process. Detailed investigation is recommended when dealing with rocks and rock masses that  
259 show time-dependent potential. The following discussion serves as an attempt to highlight the  
260 importance of time-dependent behaviour during tunnelling through a series of axisymmetric  
261 numerical analyses.

### 262 3 NUMERICAL ANALYSIS

263 An axisymmetric parametric analysis was performed within FLAC software (Itasca, 2011). The  
264 geometry of the model and the excavation sequence characteristics are shown in Figure 5. A  
265 circular tunnel of 6 m diameter and 400 m length was excavated in isotropic conditions. Full-face  
266 excavation was adopted. Two cases were assumed depending on the excavation step in each  
267 excavation cycle. In the first case (Case 1: D&B), the excavation step per cycle was 3 m as such  
268 conditions are considered to be typically representative of drill and blast excavation method on a  
269 fairly good quality rock mass. In the second case (Case 2: TBM), the excavation step per cycle  
270 was simulated to 1 m to represent the excavation sequence of a 6 m diameter mechanized tunnel  
271 using a TBM. The rock mass for both cases was assumed to behave as an elasto-visco-elastic  
272 material and CVISC model within FLAC software (Itasca, 2011) was employed. As previously  
273 discussed, the CVISC model is a visco-elastic-plastic model although for this purpose, the  
274 cohesion and tension on the model were given very high values to prevent any yielding from  
275 taking place in the model. No support measures were assumed on the study presented-herein.

276 **Figure 5. Case 1 refers to drill and blast method with 3 m excavation step per cycle (Drill jumbo**  
277 **graphic courtesy of Fletcher & Co.), Case 2 refers to TBM (Tunnelling Boring Machine) method**  
278 **with 1 m excavation per cycle (TBM graphic courtesy of Herrenknecht AG).**

279 In order to investigate further the time-dependent component of the total radial displacements it  
280 was decided to perform two main different analyses for both cases (D&B and TBM). The first  
281 analysis aimed to examine the contribution of primary creep using the Kelvin-Voigt model. In this  
282 regard, the viscous dashpots of the Maxwell body within the CVISC model was deactivated. On  
283 the second analysis, the contribution of the Burgers model was investigated in order to capture  
284 both primary and secondary stages of creep. In this case, both the Kelvin and the Maxwell bodies  
285 were activated.

286 In addition, three different sets of parameters were used for the three analyses on both cases  
287 shown in Table 4. However, for the scope of this study only the visco-elastic parameters varied  
288 between the three sets.

289 Table 4. Parameters used for CVISC model.

290 It should be stated that the visco-elastic parameters were chosen according to the analytical  
291 solution (Eq. 1) of the Kelvin-Voigt model developed by Panet (1979).

292 
$$u_r = \frac{\sigma_0 r}{2G_0} + \frac{\sigma_0 r}{2G_K} \left[ 1 - \exp\left(-\frac{t}{T_K}\right) \right] \quad (\text{Eq. 1})$$

293 where:  $\sigma_0$  is the in-situ stress conditions,  $r$  is the tunnel radius,  $G_0$  the elastic shear modulus,  $G_K$   
294 is the Kelvin shear Modulus,  $\eta_K$  is Kelvin's viscosity and  $T_K$  is known as retardation time and it is  
295 the ratio of Kelvin's viscosity over the Kelvin shear Modulus.

296 It was observed that the relaxation (retardation) time of the Kelvin-Voigt model plays a key role  
297 as this parameter controls the curvature of Kelvin's behaviour. In other words, the retardation time  
298 of Kelvin shows how fast the model will converge and reach a constant value. In this regard, the  
299 visco-elastic parameters were chosen so the retardation time ( $T_K$ ), found in the literature (Barla  
300 et al. 2010; Zhang et al. 2012; Feng et al. 2006) varies one order of magnitude between the three  
301 sets.

302 Furthermore, in order to take into consideration both the time-dependent component and the  
303 tunnel advance and examine their contribution to the total displacement recorded, the time of the  
304 excavation cycle was also captured in each set of parameters for both cases in the two analyses.  
305 The time of each excavation model varied from 2 to 8 hours. Additionally, two supplementary  
306 analyses were performed, one involved a set of runs with the Kelvin-Voigt model and the other a  
307 set of runs with the elastic models. These two analyses were used to validate the numerical  
308 models and were compared with analytical solutions. In total 62 models were simulated and their  
309 LDPs were analyzed and compared. Table 5 summarizes all the model runs performed in the  
310 presented parametric study.

311 Table 5. Nomenclature and model runs in this study.

## 312 **4 NUMERICAL RESULTS**

### 313 **4.1 Comparison of Numerical Analysis with Analytical Solutions**

314 The first step in this analysis was to compare the numerical results to the analytical solutions of  
315 the elastic (instantaneous deformation at each excavation step) and the Kelvin-Voigt model  
316 (hypothetically infinite time delay between each excavation step to allow full convergence of  
317 primary creep stage). Figure 6 shows that the numerical results are in agreement with the  
318 analytical solutions. It should be added that the elastic numerical case was compared to the elastic

319 solution of Vlachopoulos and Diederichs (2009) assuming that no plastic radius occurs at the  
320 tunnel walls (i.e.  $r_p/r_t=1$ ) The results from Kelvin-Voigt case were compared to Eq. 1.

321 **Figure 6. (Left) Numerical results (solid lines) related to the analytical solutions (as referenced)**  
322 **for the elastic and the Kelvin Voigt model, (Right) closer representation of the data for  $x$  values of**  
323  **$-15 < x < 25$ .**

324 These results serve to validate the numerical model. The real question, however, is how the  
325 viscous behaviour impacts the LDP between the two extremes in Figure 6 as the elastic case  
326 represents instantaneous excavation (cycle time is effectively zero) while the fully converged  
327 Kelvin-Voigt model (zero viscosity) represents an infinite cycle time between excavation steps.  
328 It is important, then, to consider the impact of the excavation rate (cycle time).

329 In order to examine the time-dependent potential during the construction, the tunnel excavation  
330 stages should be also considered. The bounding case numerical results (i.e. elastic and Kelvin-  
331 Voigt reference models) in the following sections were used as reference guides as they were  
332 considered to be the two extremes, the elastic is representative for the short-term LDP where no  
333 time-effect is considered whereas the Kelvin-Voigt is considered the long-term LDP during the  
334 primary stage of creep. From then on all of the results in the graphs refer to the numerical analyses  
335 unless otherwise stated.

336 The results are presented in two different ways shown in Figures 7 to 10. First, since the total  
337 displacement is much higher when the time component manifests, it was decided to normalize  
338 the total displacement to the maximum displacement of the Kelvin-Voigt reference model ( $u_{r\infty\max}$ ),  
339 shown in the Figures on the left vertical axes. Second, the numerically computed displacement  
340 against the tunnel face location is also plotted (right vertical axes). It should be noted that in the  
341 following Figures  $x$  is the distance from the tunnel face,  $R$  is the tunnel radius,  $u_r$  is the absolute  
342 radial tunnel wall displacement,  $u_{re\max}$  is the maximum elastic displacement and  $u_{r\infty\max}$  is the  
343 maximum visco-elastic displacement of the Kelvin-Voigt model. Grey and black lines are the  
344 elastic and the zero-viscosity KV models respectively.

#### 345 **4.2 KELVIN-VOIGT (KV), Investigating Primary Stage of Creep**

346 The first main analysis involved the investigation due to the time-effect on the overall total tunnel  
347 wall displacement assuming that only primary creep is observed in addition to the effect of tunnel  
348 advancement. For this purpose, the Kelvin-Voigt model (with non-zero viscosity) was assumed to  
349 represent the primary stage of creep and was used to simulate the mechanical behaviour of an

350 elasto-visco-elastic rock mass. The results for the drill and blast case and the TBM are presented  
351 in Figures 7 and 8, respectively.

352 **Figure 7. (Left) Numerical results of LDPs for the drill and blast (DB) case of the KELVIN-VOIGT**  
353 **(KV) analysis (the hours on the legend denote hours per excavation cycle), (Right) closer**  
354 **representation of the data for x values of  $-6 < X < 12$ .**

355 **Figure 8. (Left) Numerical results of LDPs for the TBM case of the KELVIN-VOIGT (KV) analysis**  
356 **(the hours on the legend denote hours per excavation cycle), (Right) closer representation of the**  
357 **data for x values of  $-2 < X < 4$ .**

358 Figures 7 and 8 show similar trends for the three sets of parameters. The results imply that  
359 increased cycle time or excavation delay exacerbates the mechanical behaviour of the rock mass,  
360 as in all models an increase of the ultimate total displacement was observed. This increase  
361 depends on the visco-elastic parameters of the Kelvin-Voigt model. Furthermore, it is shown that  
362 the models employed using the parameters of SET #2 and #3 which have a lower retardation time  
363 ( $T_K$ ) reached a constant value sooner than the models of SET#1. As expected, an increase of the  
364 retardation time parameter will result in an increase of the time required by the model to reach a  
365 constant value and become time-independent.

366 The excavation method used and thus the step advancement (m/excavation cycle) influences the  
367 results. It was observed that the models simulated employing the TBM sequence (1 m advance)  
368 reached a constant displacement value closer to the excavation face than the ones observed in  
369 the Drill and Blast Case (3 m advance). This was expected as in these analyses the time in each  
370 excavation cycle is considered; consequently, the 1-m excavation per cycle completes less tunnel  
371 meters during the same period than the 3-m excavation step.

372 Finally, the duration of each excavation cycle is important. It is shown that the displacement during  
373 the 8-hour shifts reached a constant value closer to the tunnel face than the 2-hours shift. This is  
374 also reasonable as the elapsed-time during excavation cycles contributes in allowing the rock  
375 mass to deform and reach its maximum displacement value.

### 376 **4.3 BURGERS (B), Investigating Primary and Secondary Stage of Creep**

377 The second stage of this analysis was to investigate the influence of both primary and secondary  
378 stages of creep behaviour using the Burgers model. The results are presented in Figures 9 and  
379 10 for the drill and blast and TBM case, respectively. Similar observations with the previous case  
380 of KELVIN-VOIGT analysis can be made.

381 The Burgers model simulates the idealized behaviour of the first two stages of creep. The  
382 maximum strains (deformation) due to the secondary stage (Maxwell model) are effectively  
383 infinite. This is also observed on Figures 9 and 10. In reality, ductile materials could keep  
384 deforming without yielding for a very long period of time or up to full closure of the tunnel.

385 Figure 9. (Left) Numerical results of LDPs for the drill and blast (DB) case of the BURGERS (B)  
386 analysis (the hours on the legend denote hours per excavation cycle), (Right) closer  
387 representation of the data for x values of  $-10 < X < 50$ .

388 Figure 10. (Left) Numerical results of LDPs for the TBM case of the BURGERS (B) analysis (the  
389 hours on the legend denote hours per excavation cycle), (Right) closer representation of the data  
390 for x values of  $-10 < X < 50$ .

391 In this part, it was noticed that the magnitude of the total displacements between the two cases  
392 varied significantly. The excavation method influences the accumulated displacements. In the drill  
393 and blast case, all three sets of models (parameters) exhibited less displacement than the TBM  
394 case for the same duration of the excavation cycles. During a tunnel excavation by a TBM, the  
395 tunnel excavation requires more time than a drill and blast excavation for the same excavation  
396 cycle. For instance, a TBM that excavates 1 m every 6 hours the elapsed time is three times  
397 longer than the drill and blast case of 3 m excavation per cycle. As a result, the time for the  
398 excavation of the same length tunnel will result in accumulation of displacement increase in the  
399 case of the TBM. However, in reality this may not always represent real conditions as TBMs are  
400 commonly preferable since they tend to achieve better excavation rates; if the rock mass  
401 conditions and the tunnel length make TBMs affordable. If the latter is the case, then a TBM  
402 excavation (Figure 10) of a two-hour excavation cycle, it is shown that the surrounding rock mass  
403 represented by SET#1 exhibits less displacement than of an eight-hour excavation cycle using  
404 drill and blast (Figure 9).

## 405 5 DISCUSSION

406 Another aspect of this study was to analyze the boundary and model conditions when creep  
407 behaviour manifests. Figures 11 and 12 show the stress-paths related to the numerical analyses  
408 presented herein for both cases drill and blast and TBM, where  $\sigma_{zz}$  and  $\sigma_{xx}$  are the major and  
409 minor stresses in the model, p is the mean stress and q the deviatoric, x refers to the location in  
410 the tunnel and R is the tunnel radius. Creep in these models is in response to differential stress  
411 (represented by q in the following figures) while the confining pressure (p) acts to resist yield but  
412 not creep in the visco-elastic case modelled here.

413 It is shown that the excavation step influences the stress regime in the tunnel. In the TBM case,  
414 where the excavation step is 1 m per excavation cycle, the stresses redistribute in a different  
415 manner than with the Drill and Blast case (3 m per cycle). In theory, the deviatoric stress ( $q$ ) in  
416 both cases should reach the in situ pressure,  $p$  (as the radial stresses are zero and tangential  
417 stresses are  $2p$  at the boundary). This does not occur in the model as the stresses are averaged  
418 in the grid zones. The deviatoric stress would approach the value of in situ stress if the elements  
419 in the numerical mesh were very small.

420 **Figure 11. Stress paths for the drill and blast case.**

421 **Figure 12. Stress paths for the TBM case.**

422 For a better understanding of the results the deviatoric stress was related to the displacement  
423 data normalized to the maximum displacement of the Kelvin-Voigt model ( $u_{r\infty\max}$ ). Only the results  
424 from the KELVIN-VOIGT analysis are presented and related to the deviatoric stress as it was  
425 noticed that time-dependent behaviour initiates at the same stress level and from the same  
426 location for all three sets and are shown in Figures 13 and 14 for the drill and blast case and the  
427 TBM, respectively; where:  $x$  is the distance from the tunnel face,  $R$  is the tunnel radius,  $u_r$  is the  
428 radial tunnel wall displacement,  $u_{re\max}$ ,  $q_{cr}$  denotes the deviatoric stress at which creep initiates.

429 **Figure 13. (Left) Relating the deviatoric stress ( $q$ ) to the tunnel wall displacement normalized to**  
430 **the maximum displacement of the KELVIN-VOIGT model ( $u_{r\infty\max}$ ) for the drill and blast case**  
431 **(D&B), (Right) closer representation of the data for  $x$  values of  $-6 < X < 12$ .**

432 **Figure 14. (Left) Relating the deviatoric stress ( $q$ ) to the tunnel wall displacement normalized to**  
433 **the maximum displacement of the KELVIN-VOIGT model ( $u_{r\infty\max}$ ) for the TBM case, (Right) closer**  
434 **representation of the data for  $x$  values of  $-2 < X < 4$ .**

435 Time-dependent behaviour starts for both cases and all data sets when the deviatoric stress  
436 reaches a critical value ( $q_{cr}$ ) shown in Figures 13 and 14. This critical value is attained after one  
437 excavation step. In the drill and blast case, this is 3 m away from the tunnel whereas for the TBM  
438 case it is 1 m. It is at the point at which the time-dependent LDPs deviate from the elastic LDP.  
439 Until this critical point, the rock mass behaves elastically.

440 Implications during the tunnel construction may arise due to time-dependent deformation. Figure  
441 15 shows the radial displacement of chainage at 1444 m of Saint Martin La Porte tunnel that  
442 exhibited severe squeezing and creep behaviour (Barla, 2016). It is illustrated that the rock mass  
443 deformed 60 cm during a period of 166 days. A schematic representation of the possible LDPs is  
444 also presented herein.

445 **Figure 15. Predicted LDPs according to the tunnel data of radial displacement against distance**  
446 **(modified after Barla, 2016).**



447 **6 CONCLUSIONS**

448 Analytical solutions often utilized in Convergence-Confinement analyses usually examine either  
449 the effect of tunnel advancement or the time-effect. Even in the latter case where time is  
450 considered, as shown in Figure 16 (i.e. Panet, 1979 curves), the overall displacement can be  
451 estimated. As this could be partially used for the selection of the final support, one may wonder if  
452 it could also be possible to simulate and replicate the complete problem. In this regard, an  
453 overview of the conventional methods used to predict the Longitudinal Displacement Profile of  
454 the radial displacements was presented and the limitations were highlighted. For this purpose,  
455 numerical analyses were performed where the displacement is both a function of time and the  
456 excavation advancement. More specifically, a parametric axisymmetric study was employed  
457 taking into consideration both effects (tunnel advancement and time) where three sets of models  
458 with different visco-elastic parameters were investigated under different conditions. It was shown  
459 that the effect of only the primary creep can lead to even 50% increase of the initial displacement  
460 and that the creep-parameters control the time the displacement will reach a constant value.  
461 There is no theoretical bound (other than full closure) when considering secondary creep. This  
462 could be the case of ductile rocks and rock masses like salt. The excavation method also controls  
463 the overall displacement as discussed. Different results may assist the selection of utilizing drill  
464 and blast over a TBM excavation if it is proven to be financially affordable. Finally, tunnel data  
465 were presented where time-dependent deformations were exhibited, relative findings to this study  
466 were derived.

467 **Figure 16. (Left) LDPs for the drill and blast (DB) and TBM case of the KELVIN-VOIGT (KV)**  
468 **analysis related to the analytical solutions (continued lines related to hours on the legend denote**  
469 **hours per excavation cycle), (Right) closer representation of the data for  $x$  values of  $-5 < X < 15$ .**

470 **In regards to time-dependent deformation taking place in an underground environment it would**  
471 **contribute to both science and practice if a complete tunnel dataset was utilized with monitoring**  
472 **data and laboratory data in a numerical back-analysis. Especially in some cases, it is valuable to**  
473 **attain data acquired over years of monitoring to be able to capture the full rock mass response as**  
474 **for example, in the case of creep behaviour where also the contribution of the support system**  
475 **could be further analyzed.**

476 Being able to predict and estimate the rock mass response due to one excavation method versus  
477 another can lead to project optimization. Optimization of the design usually involves the  
478 appropriate selection of the excavation method and the support system that would allow the rock  
479 mass to further deform over time avoiding overstressing that could otherwise lead to support

480 yielding and abrupt rock mass instabilities, safety issues and cost overruns (Paraskevopoulou  
481 and Benardos). It is encouraged thus, to further examine the geological model, its rheological  
482 behaviour potential and utilizing all data and information available that will improve the design of  
483 the overall project.

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## TABLE OF FIGURES

Figure 1. The Ground Reaction Curve response of an elasto-plastic material and its relation to the LDP. Y-axis on the left refers to the internal pressure ( $p_i$ ) normalized to the in-situ pressure ( $p_0$ ), Y-axis on the right refers to the distance from the face ( $x$ ) normalized to the tunnel radius ( $R$ ) and X-axis refers to the radial displacement at a location  $x$  normalized to the maximum radial displacement.

Figure 2. Characteristic curve of creep behaviour.

Figure 3. Longitudinal Displacement Profile (LDP) in an elasto-visco-elastic-plastic medium (see text for details).

Figure 4. Longitudinal Displacement Profile (LDP) in an elasto-visco-elastic medium (see text for details).

Figure 5. Case 1 refers to drill and blast method with 3 m excavation step per cycle (Drill jumbo graphic courtesy of Fletcher & Co.), Case 2 refers to TBM (Tunnelling Boring Machine) method with 1 m excavation per cycle (TBM graphic courtesy of Herrenknecht AG).

Figure 6. (Left) Numerical results (solid lines) related to the analytical solutions (as referenced) for the elastic and the Kelvin Voigt model, (Right) closer representation of the data for  $x$  values of  $-15 < x < 25$ .

Figure 7. (Left) Numerical results of LDPs for the drill and blast (DB) case of the KELVIN-VOIGT (KV) analysis (the hours on the legend denote hours per excavation cycle), (Right) closer representation of the data for  $x$  values of  $-6 < X < 12$ .

Figure 8. (Left) Numerical results of LDPs for the TBM case of the KELVIN-VOIGT (KV) analysis (the hours on the legend denote hours per excavation cycle), (Right) closer representation of the data for  $x$  values of  $-2 < X < 4$ .

Figure 9. (Left) Numerical results of LDPs for the drill and blast (DB) case of the BURGERS (B) analysis (the hours on the legend denote hours per excavation cycle), (Right) closer representation of the data for  $x$  values of  $-10 < X < 50$ .

Figure 10. (Left) Numerical results of LDPs for the TBM case of the BURGERS (B) analysis (the hours on the legend denote hours per excavation cycle), (Right) closer representation of the data for  $x$  values of  $-10 < X < 50$ .

Figure 11. Stress paths for the drill and blast case.

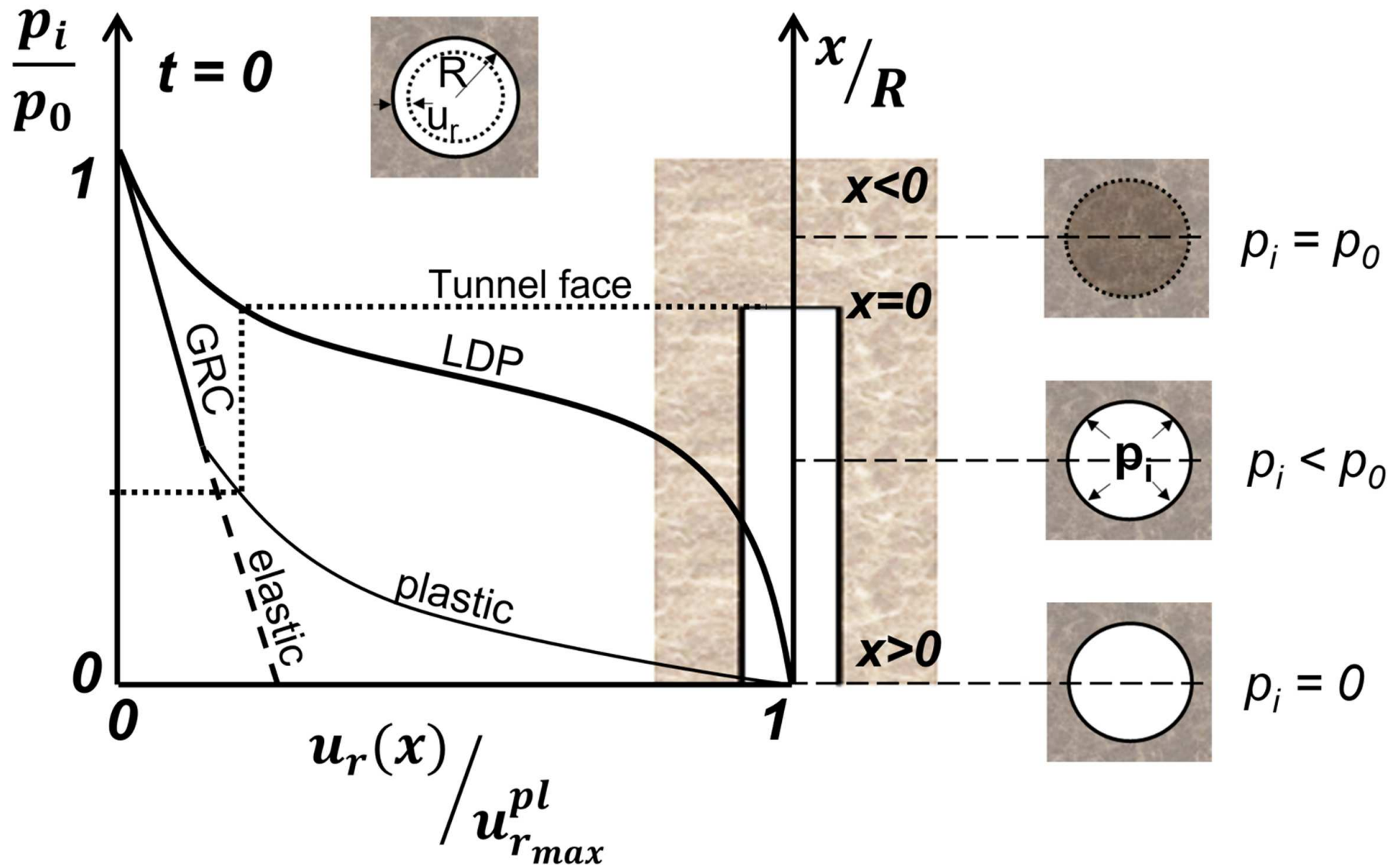
Figure 12. Stress paths for the TBM case.

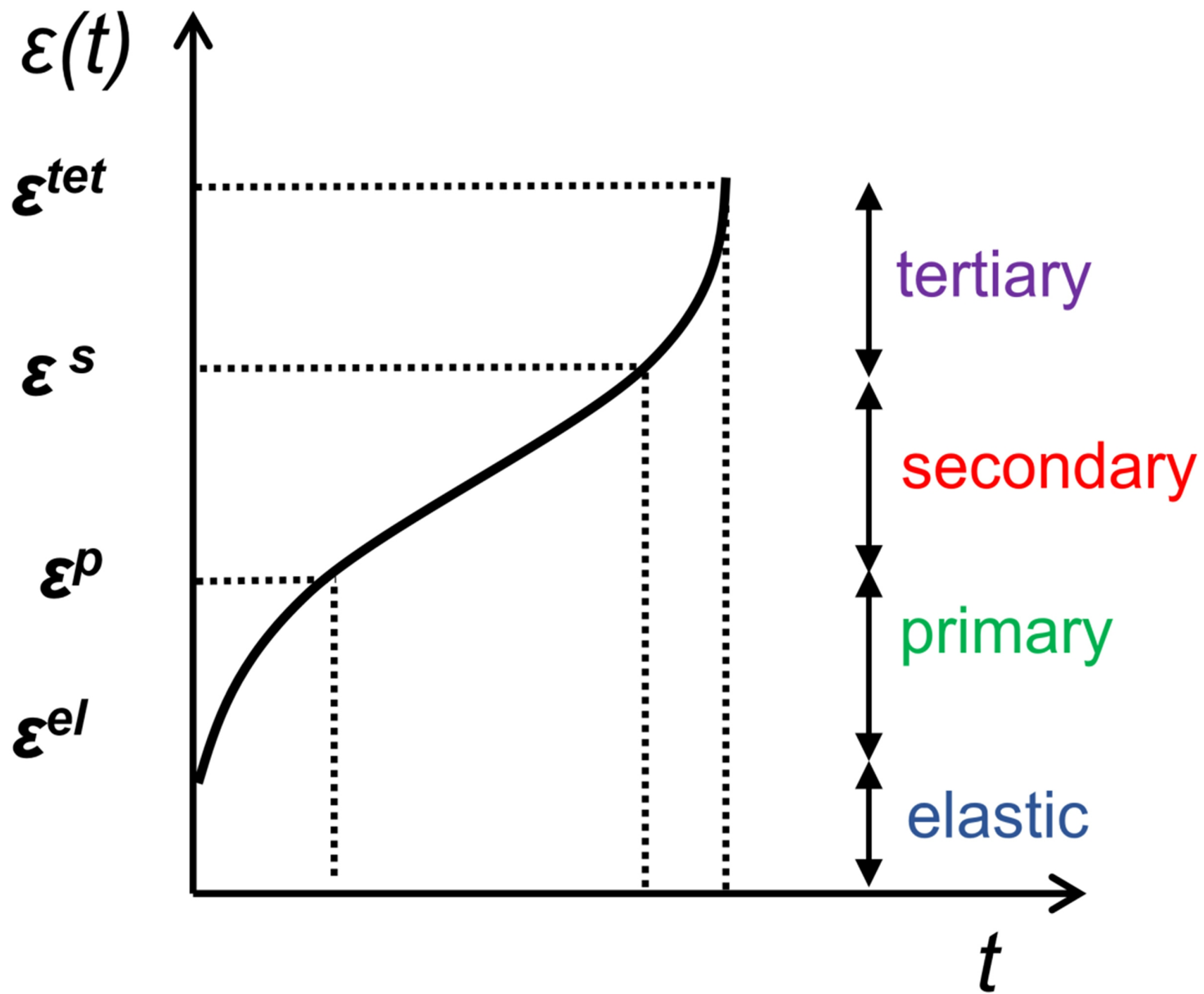
Figure 13. (Left) Relating the deviatoric stress ( $q$ ) to the tunnel wall displacement normalized to the maximum displacement of the KELVIN-VOIGT model ( $u_{r\infty_{\max}}$ ) for the drill and blast case (D&B), (Right) closer representation of the data for  $x$  values of  $-6 < X < 12$ .

Figure 14. (Left) Relating the deviatoric stress ( $q$ ) to the tunnel wall displacement normalized to the maximum displacement of the KELVIN-VOIGT model ( $u_{r\infty_{\max}}$ ) for the TBM case, (Right) closer representation of the data for  $x$  values of  $-2 < X < 4$ .

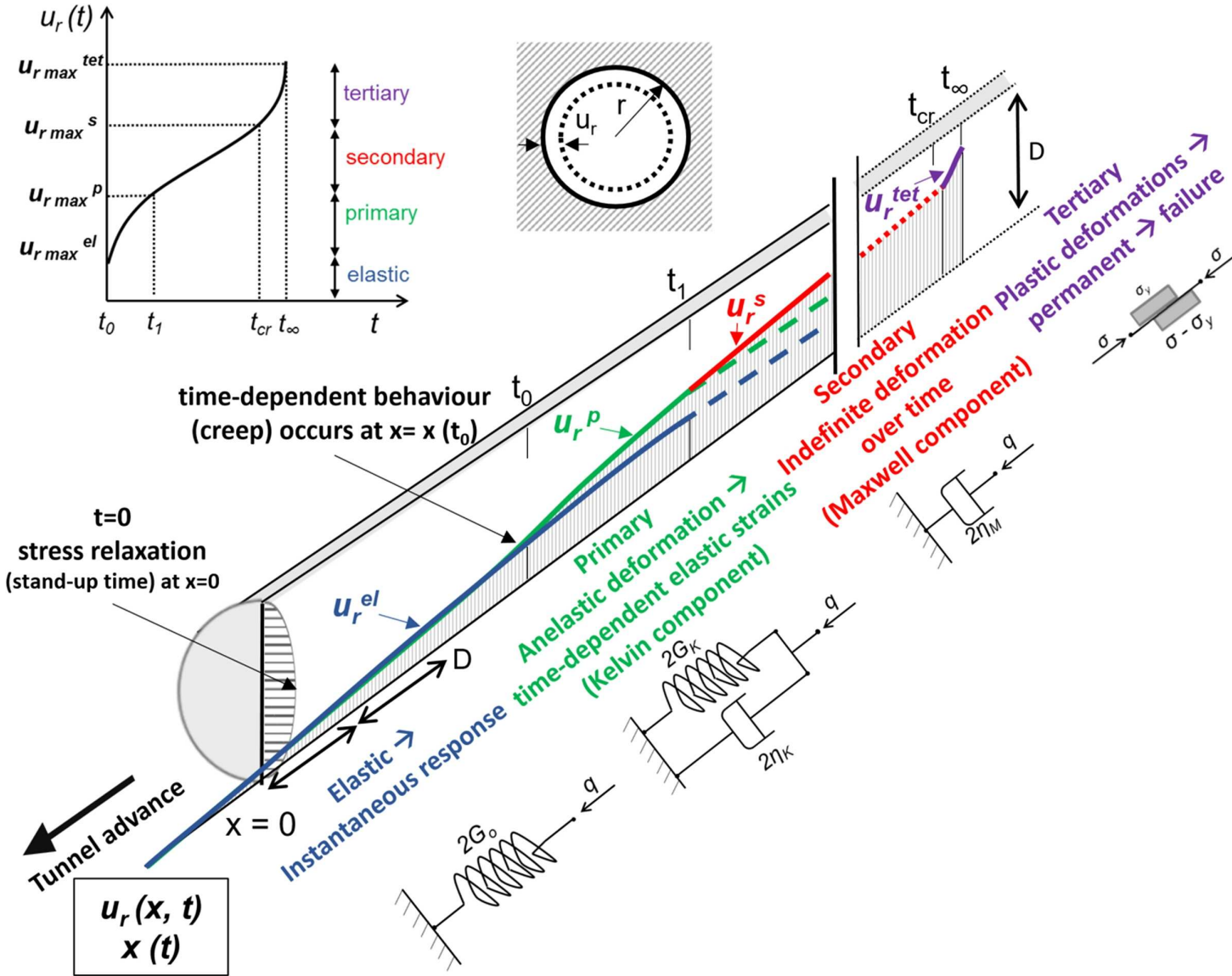
Figure 15. Predicted LDPs according to the tunnel data of radial displacement against distance (modified after Barla, 2016).

Figure 16. (Left) LDPs for the drill and blast (DB) and TBM case of the KELVIN-VOIGT (KV) analysis related to the analytical solutions (continued lines related to hours on the legend denote hours per excavation cycle), (Right) closer representation of the data for  $x$  values of  $-5 < X < 15$ .

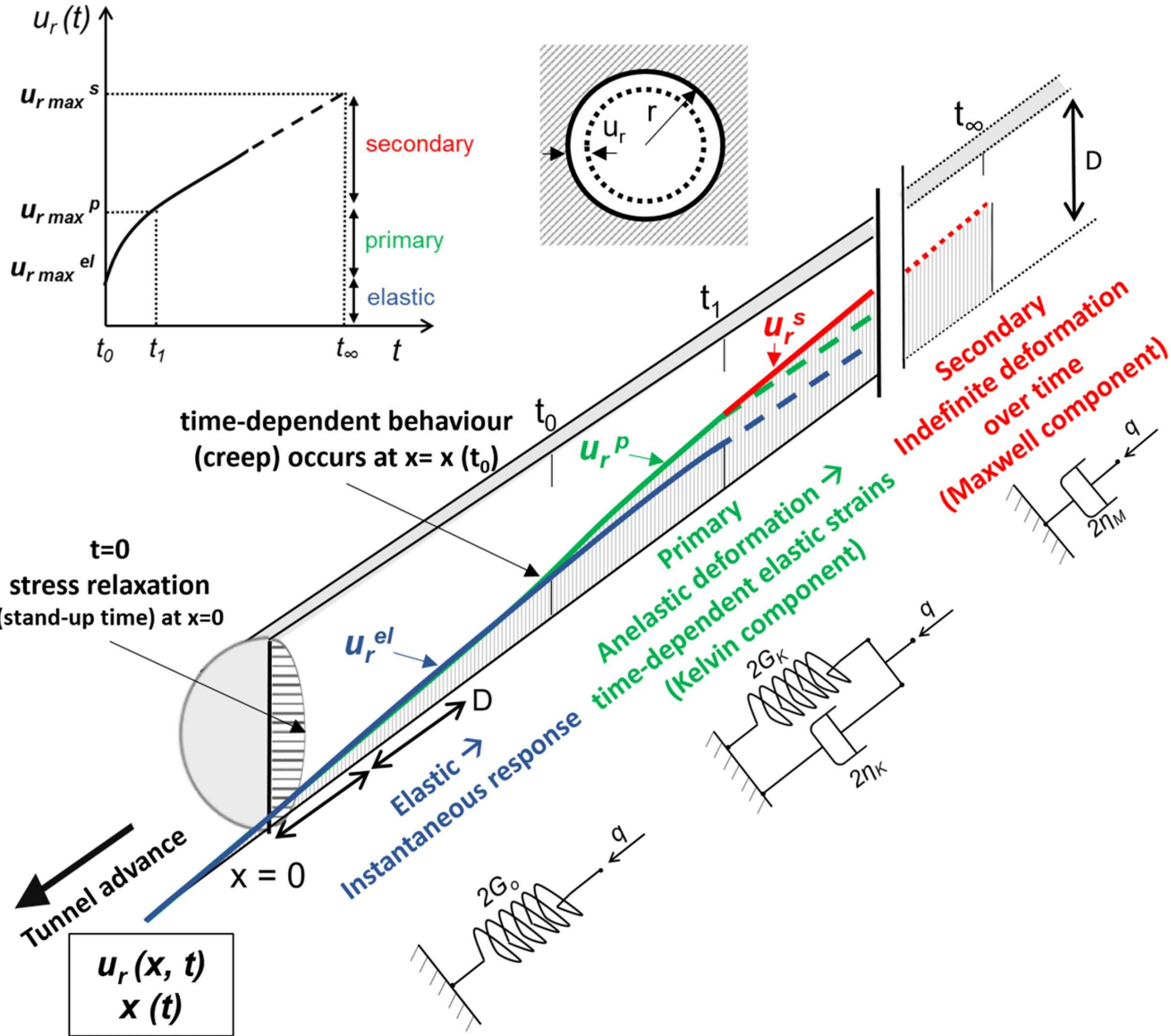


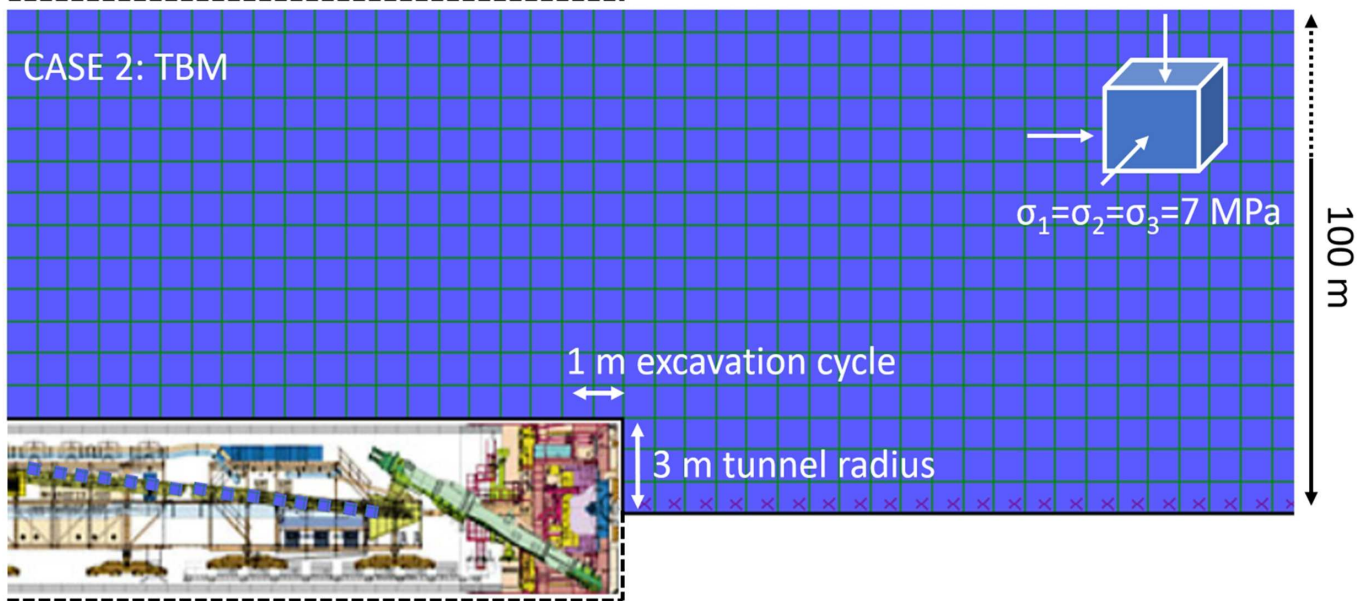
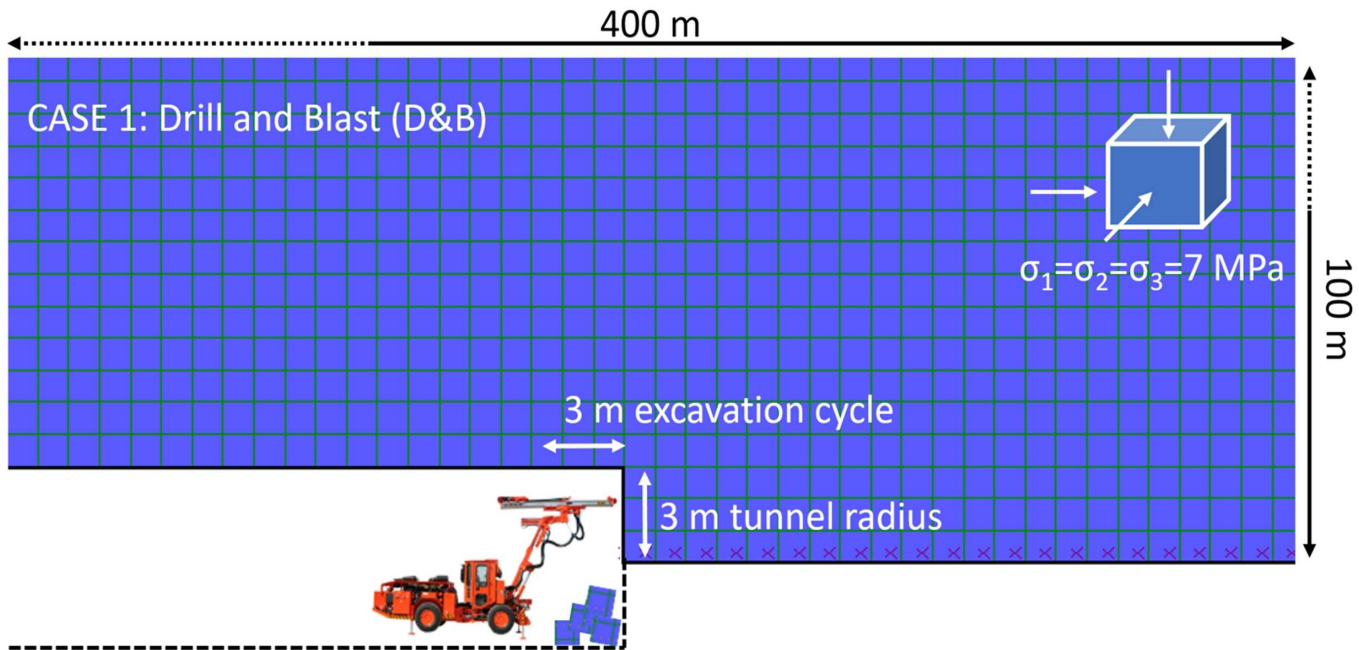


# Elasto-visco-elastic-plastic medium

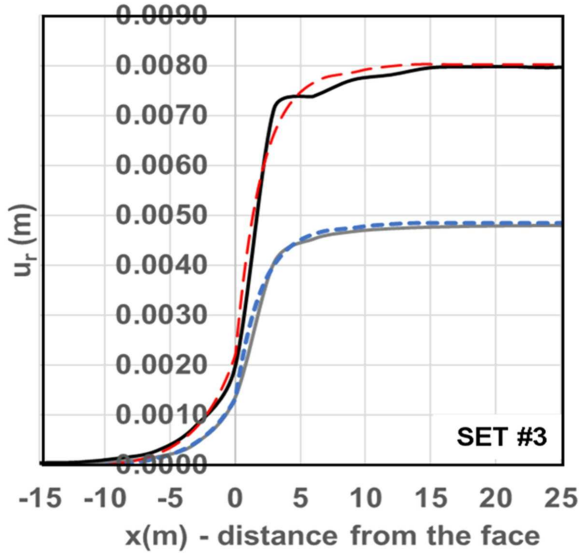
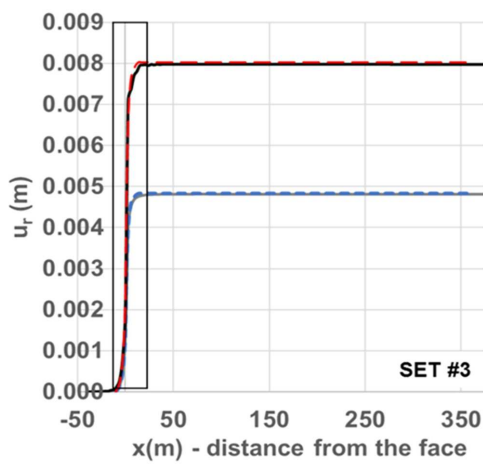
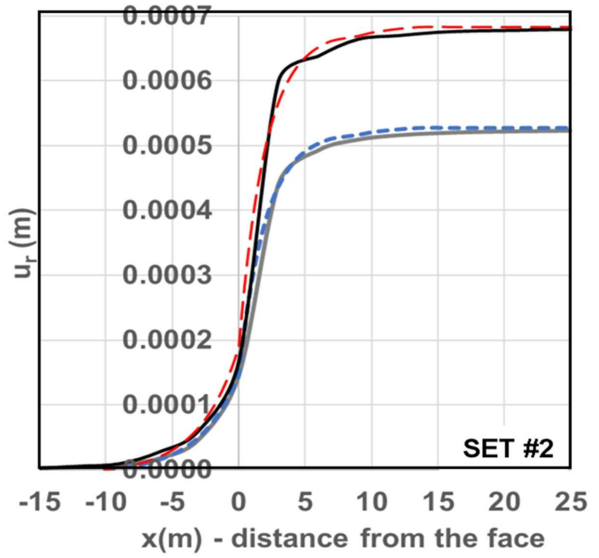
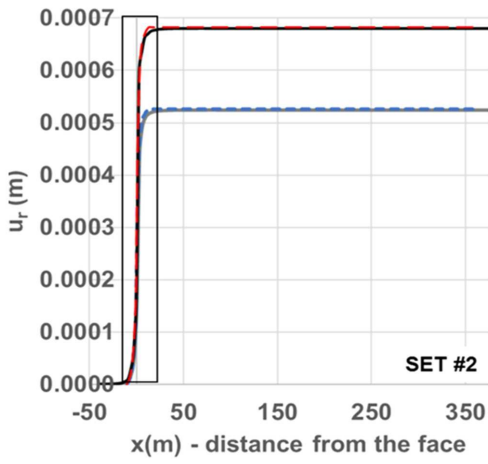
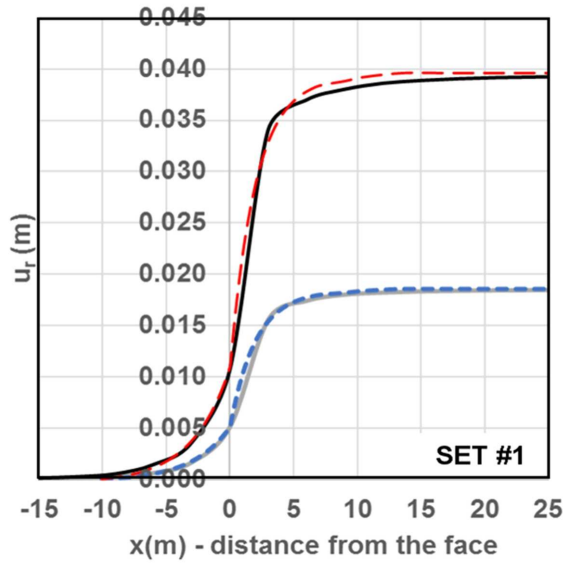
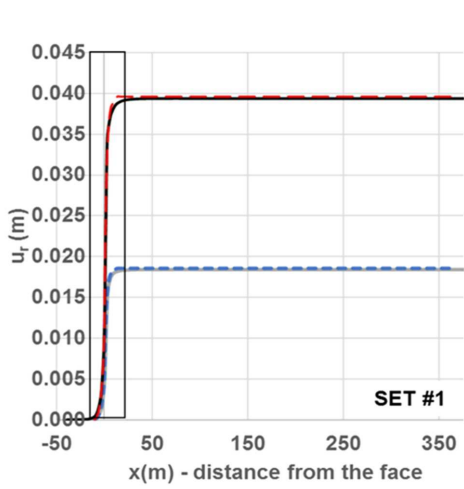


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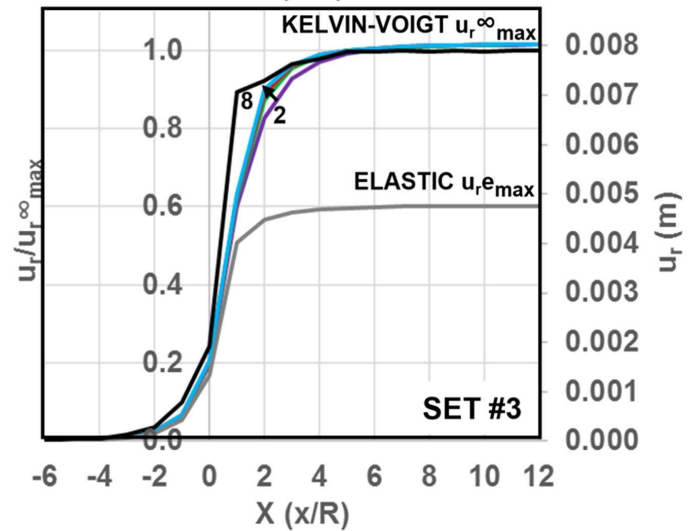
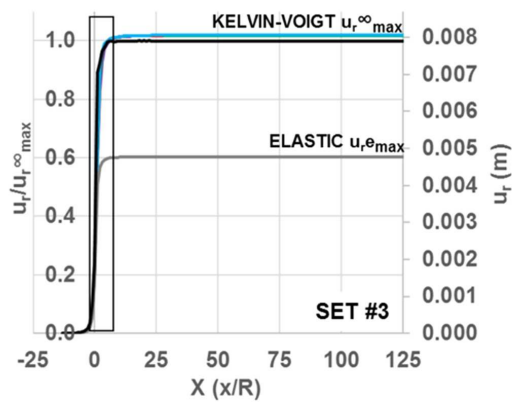
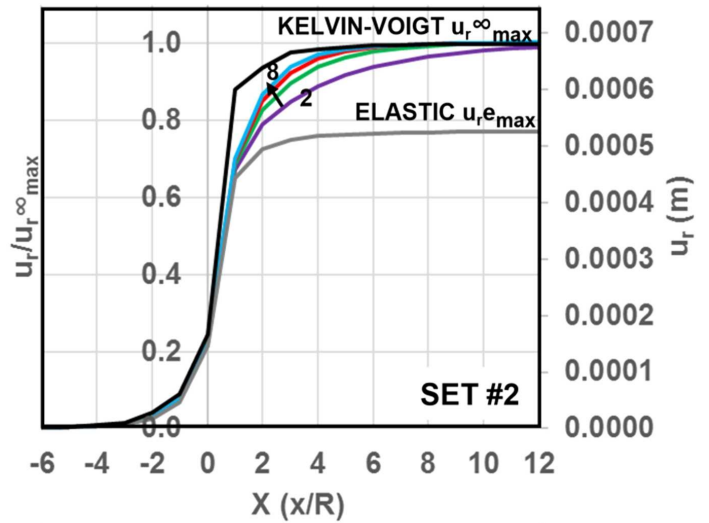
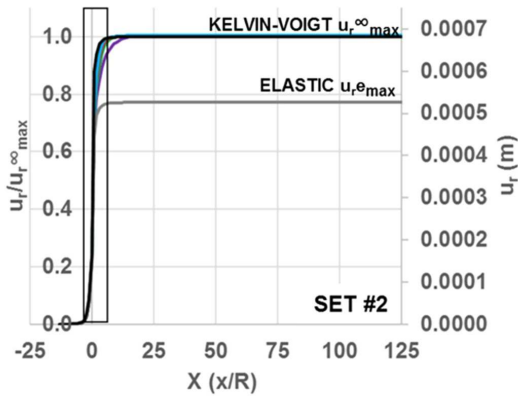
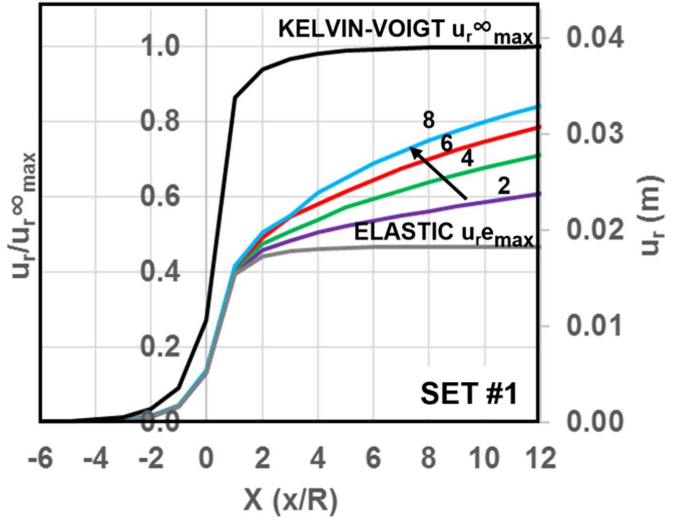
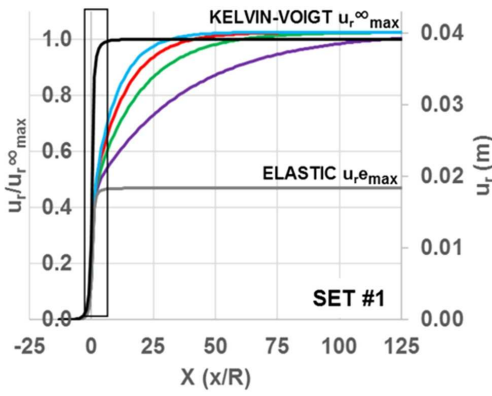






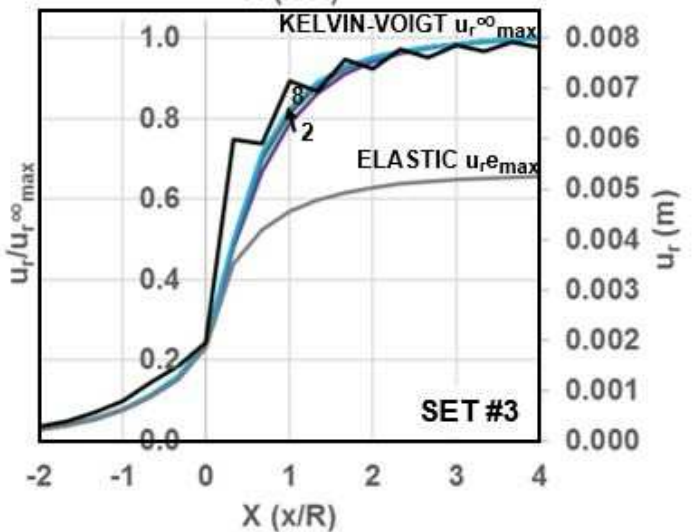
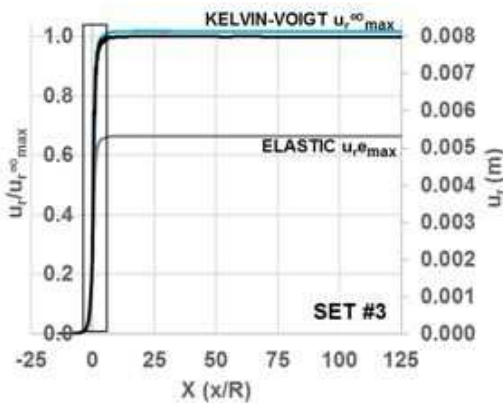
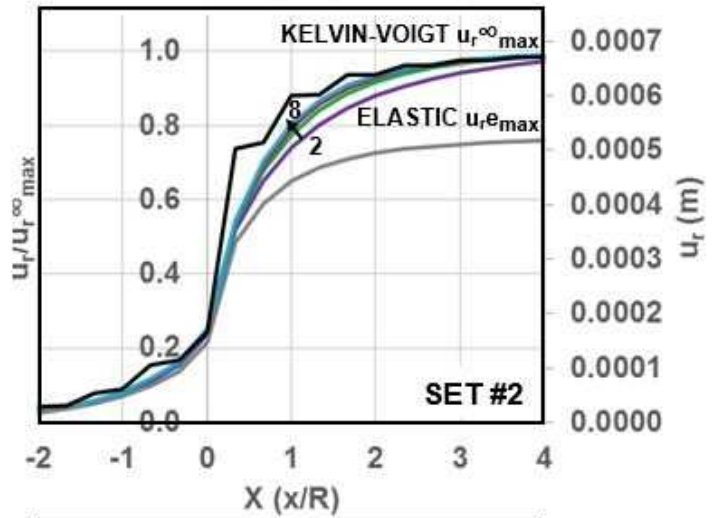
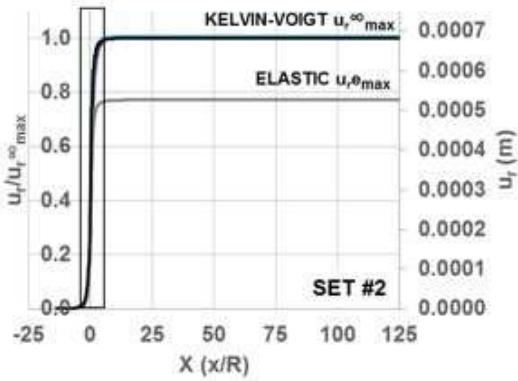
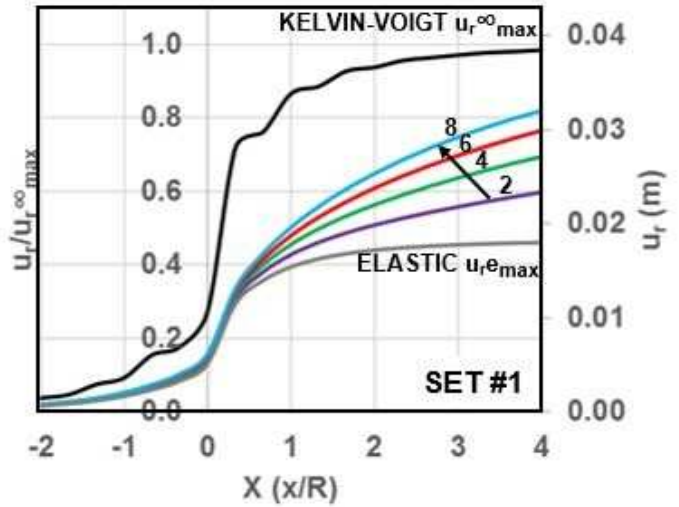
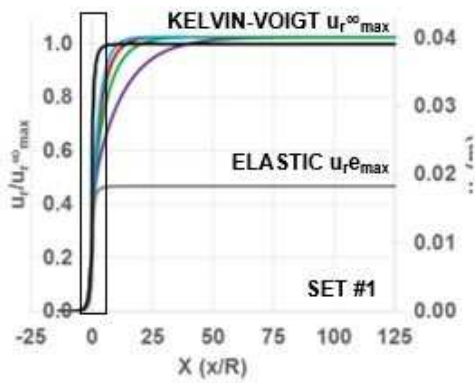


- ELASTIC
- - - ELASTIC (Vlachopoulos and Diederichs 2009)
- KELVIN-VOIGT
- - - KELVIN-VOIGT (Panet 1976)

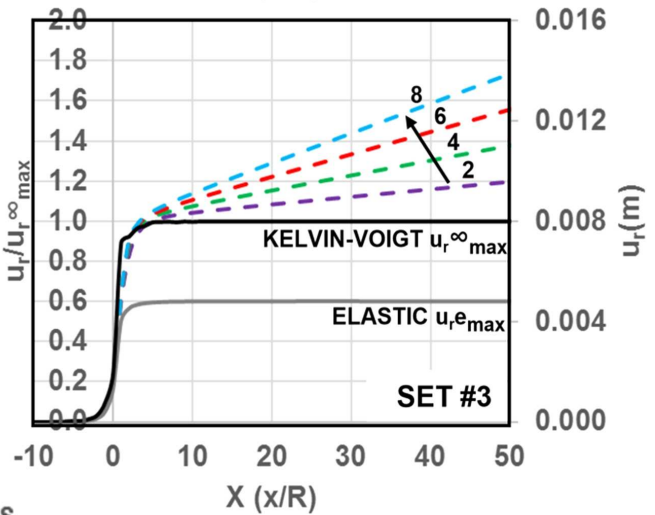
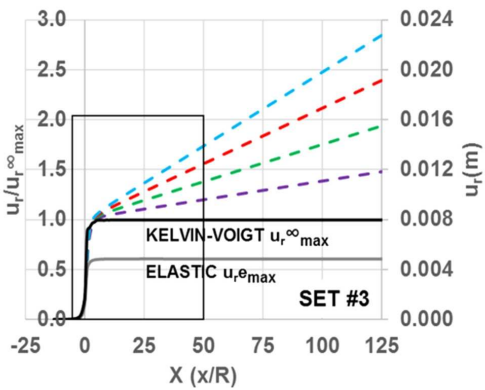
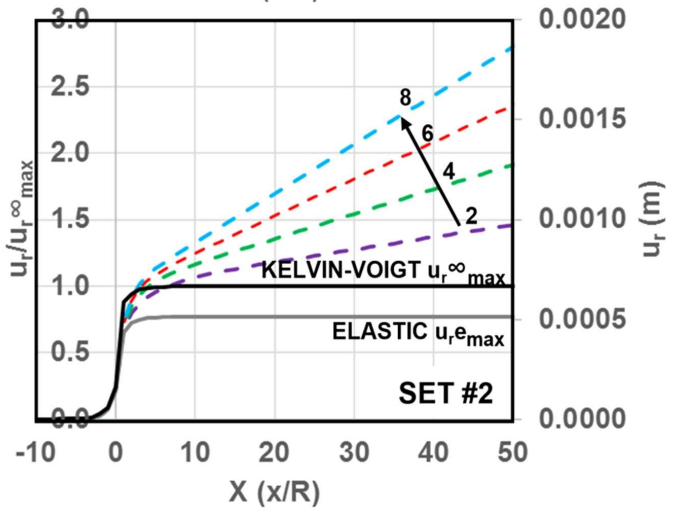
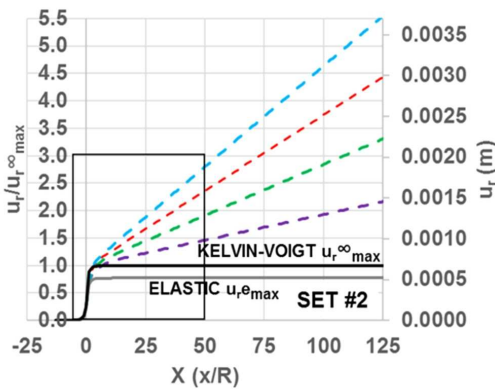
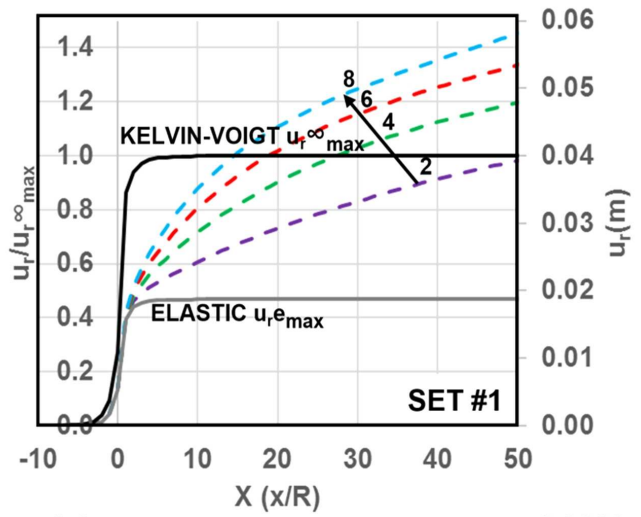
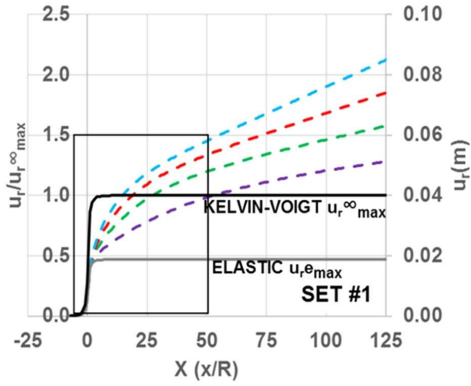


- 2 hours\_KV
- 4 hours\_KV
- 6 hours\_KV
- 8 hours\_KV
- ELASTIC
- KELVIN-VOIGT

# TBM

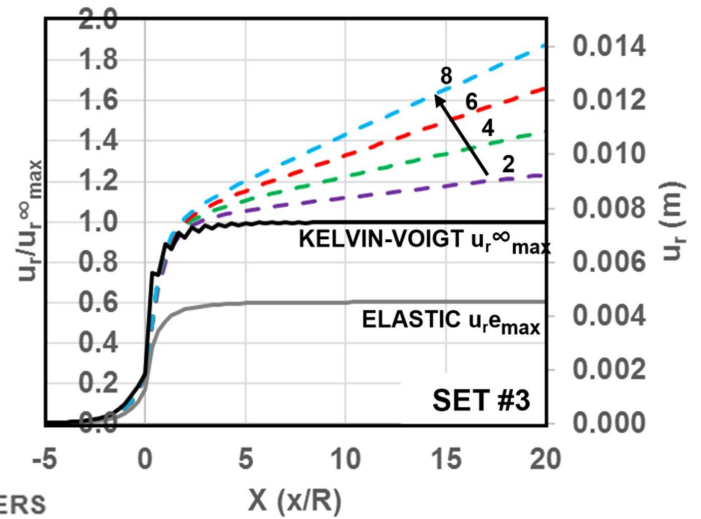
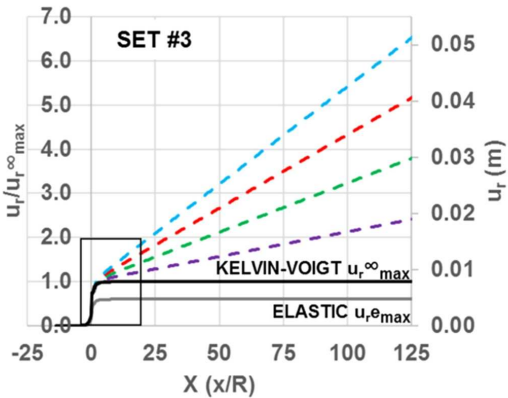
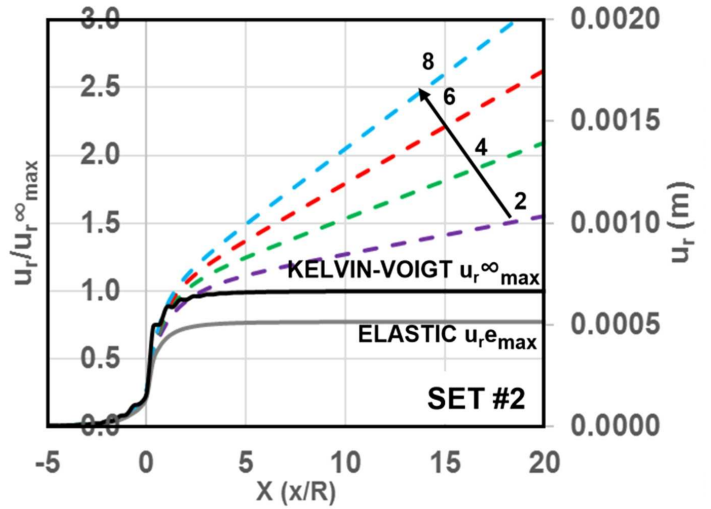
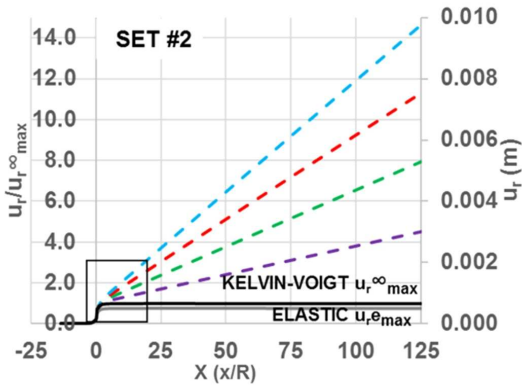
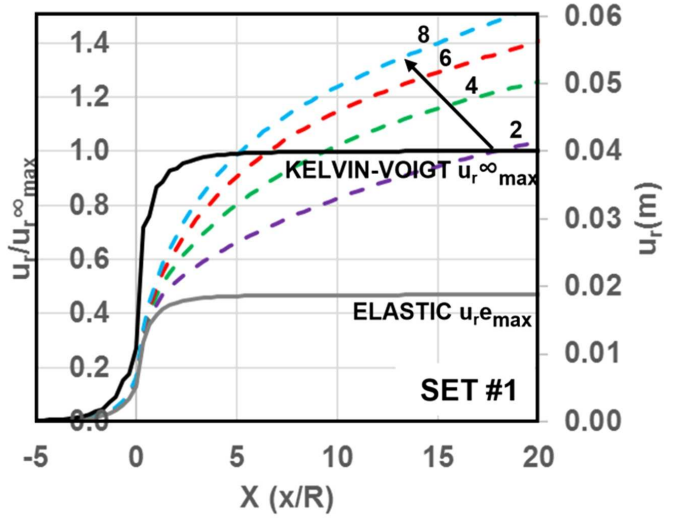
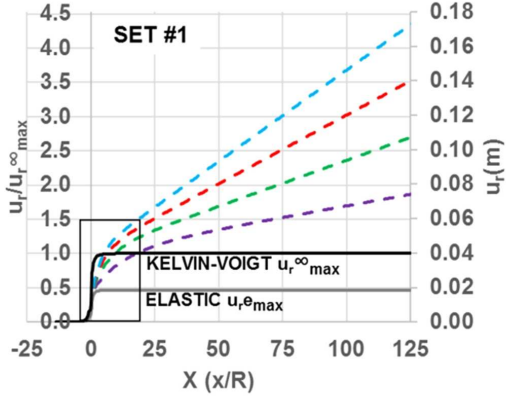


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- 6 hours\_KV    —8 hours\_KV
- ELASTIC        —KELVIN-VOIGT



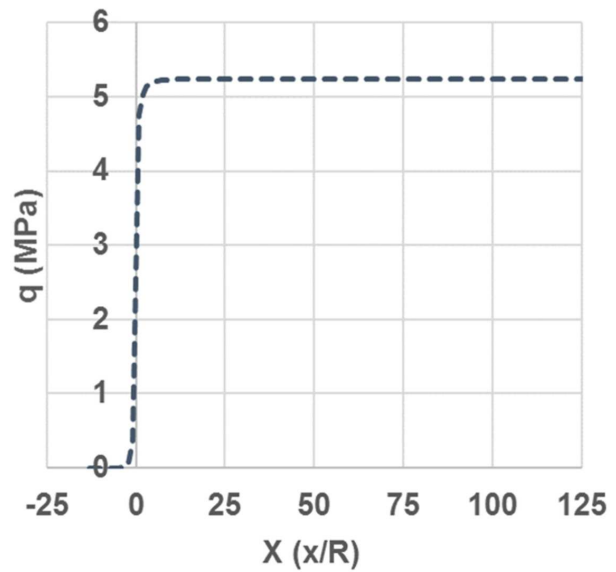
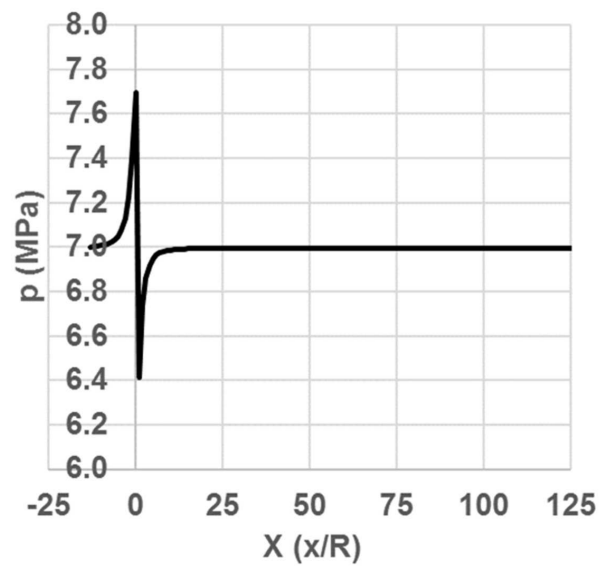
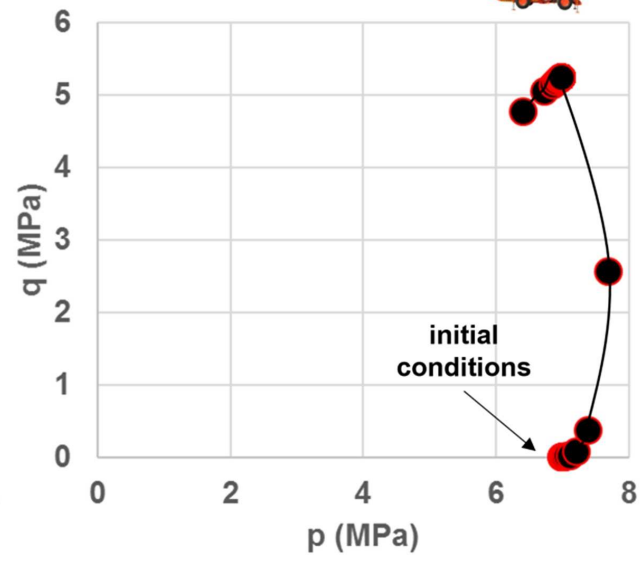
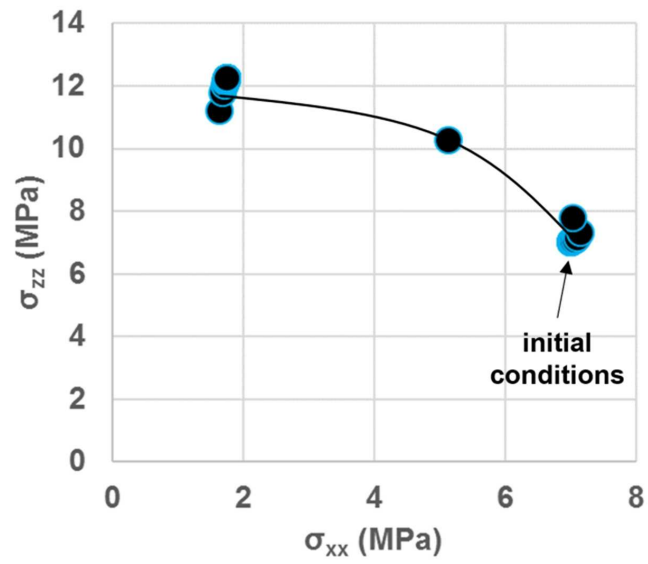
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- ELASTIC                    — KELVIN-VOIGT

# TBM

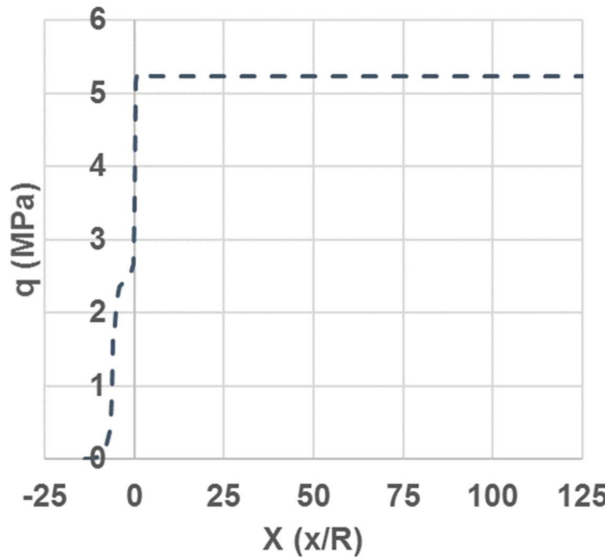
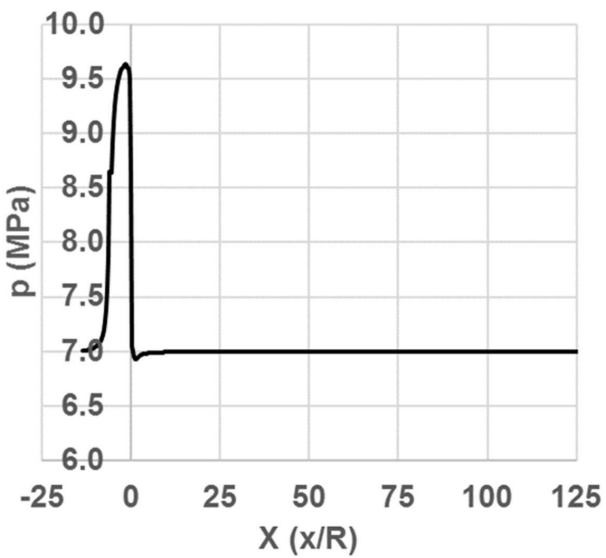
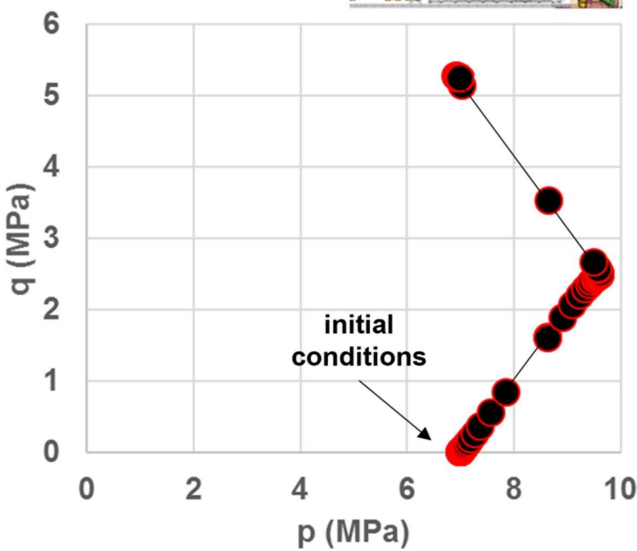
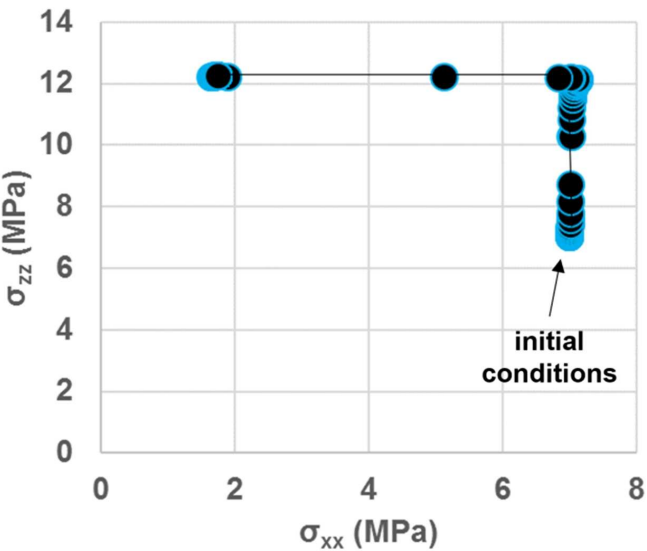


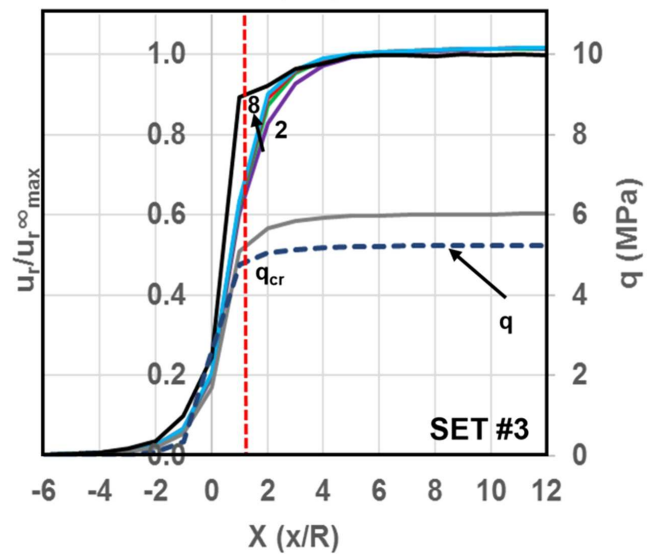
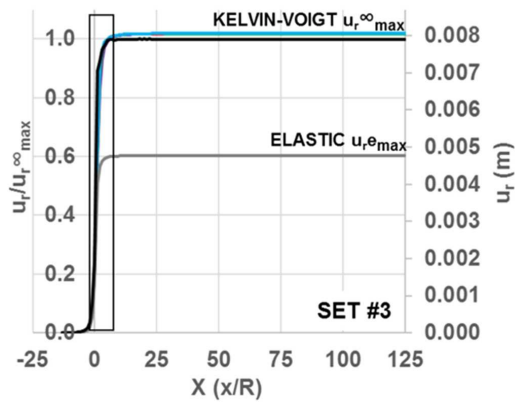
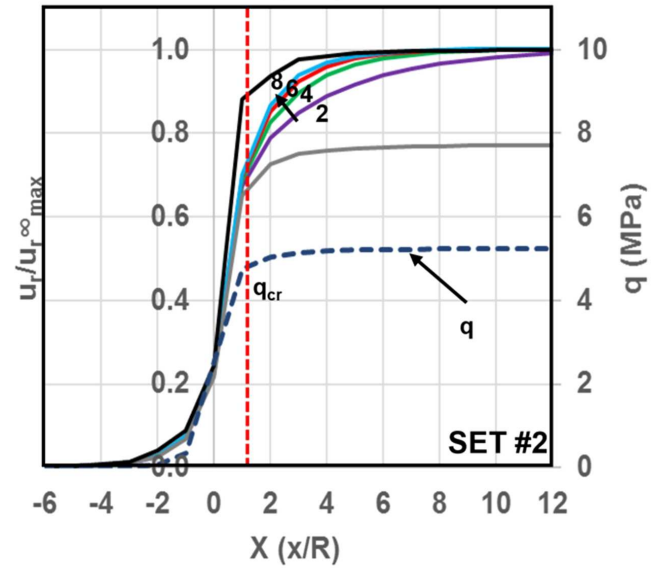
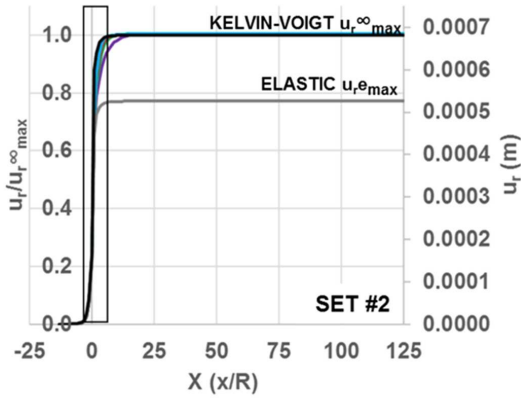
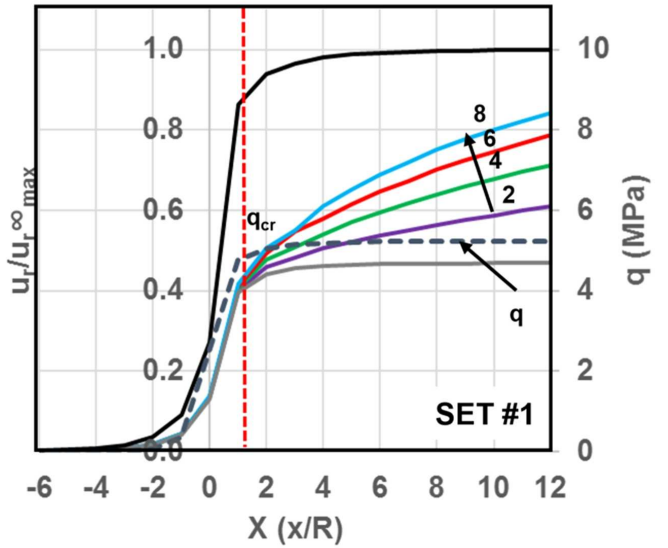
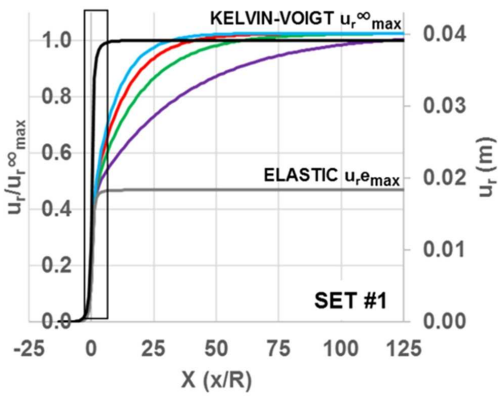
- - 2 hours\_BURGERS    - - 4 hours\_BURGERS
- - 6 hours\_BURGERS    - - 8 hours\_BURGERS
- ELASTIC                    — KELVIN-VOIGT





**TBM**

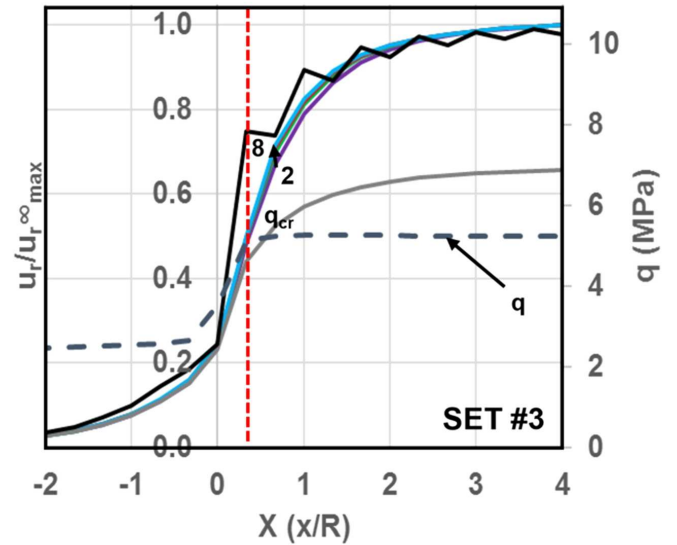
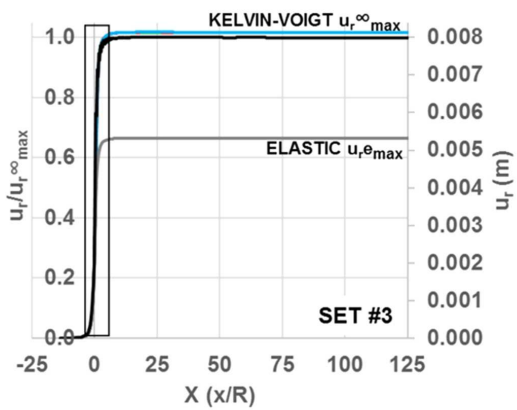
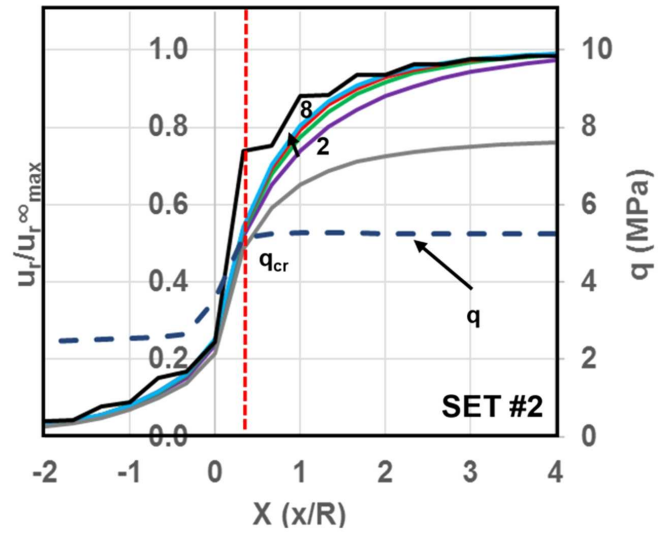
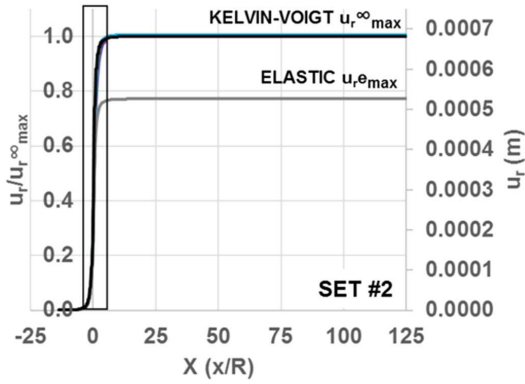
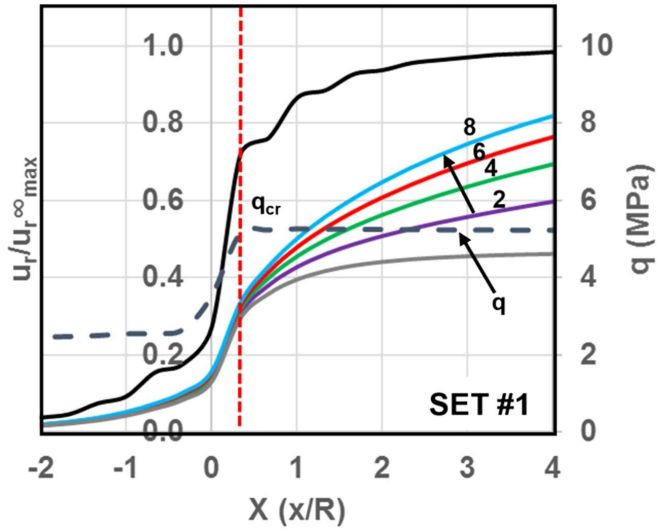
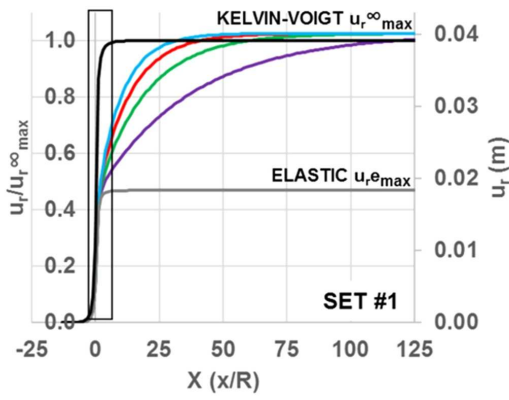




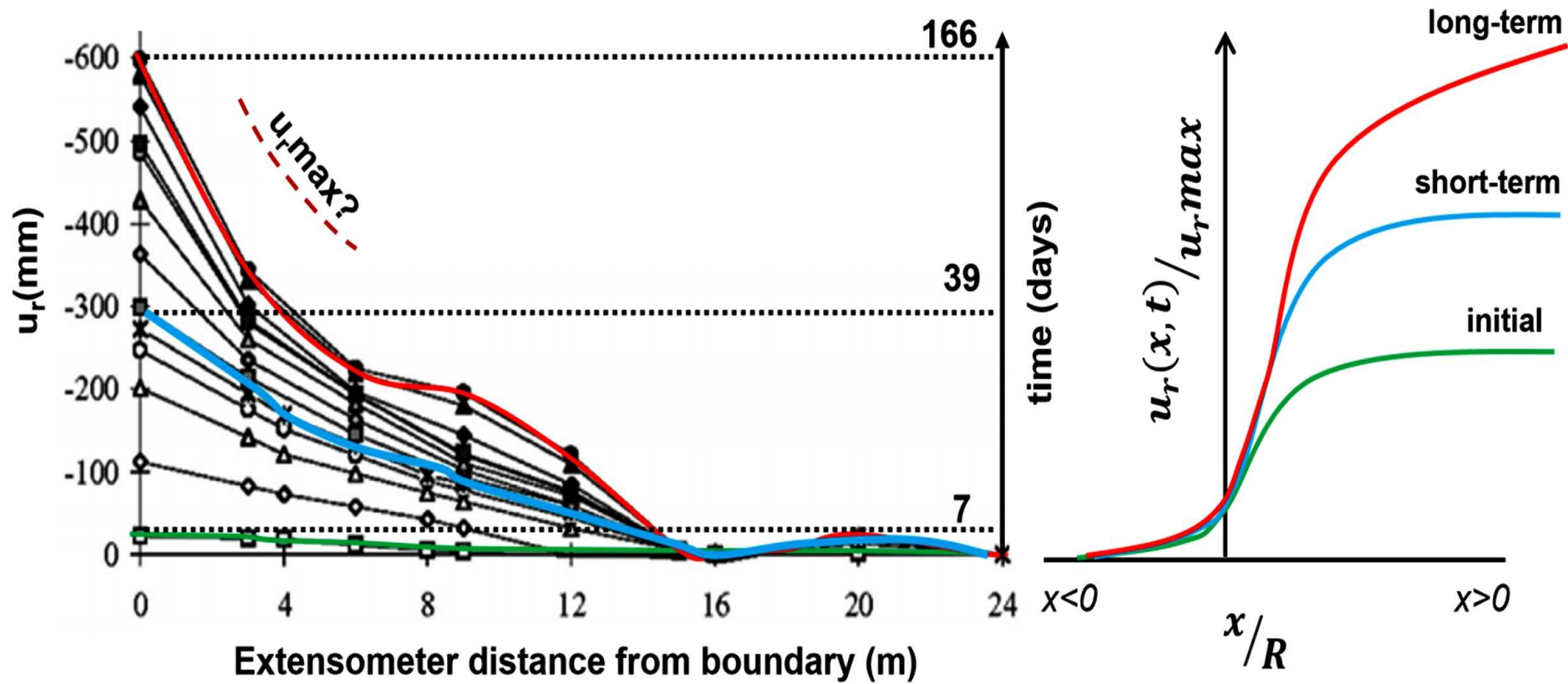
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- ELASTIC        — KELVIN-VOIGT

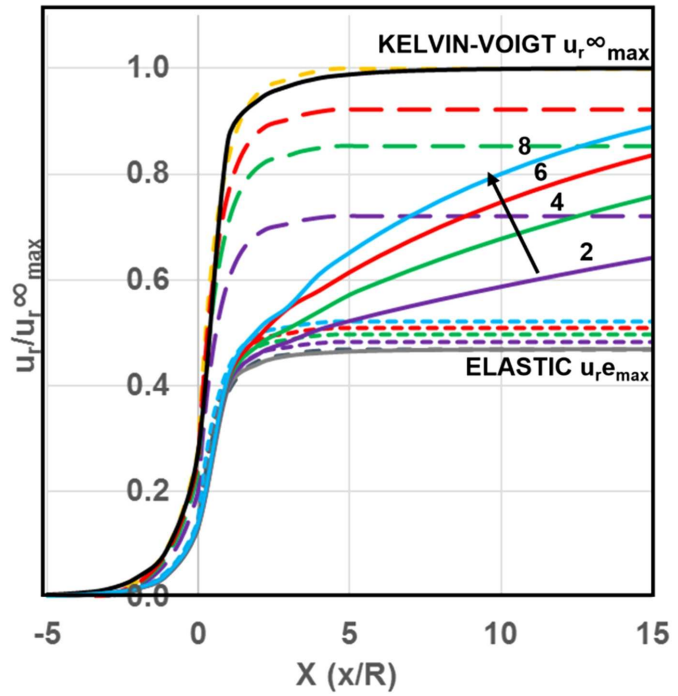
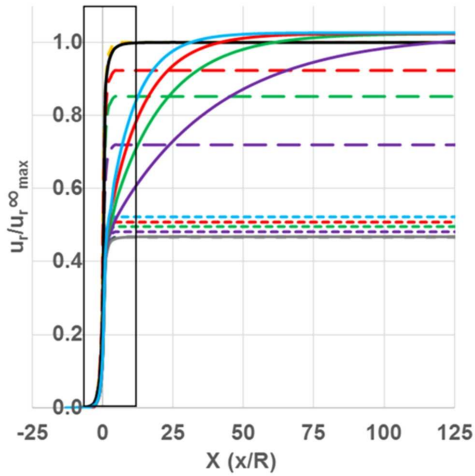


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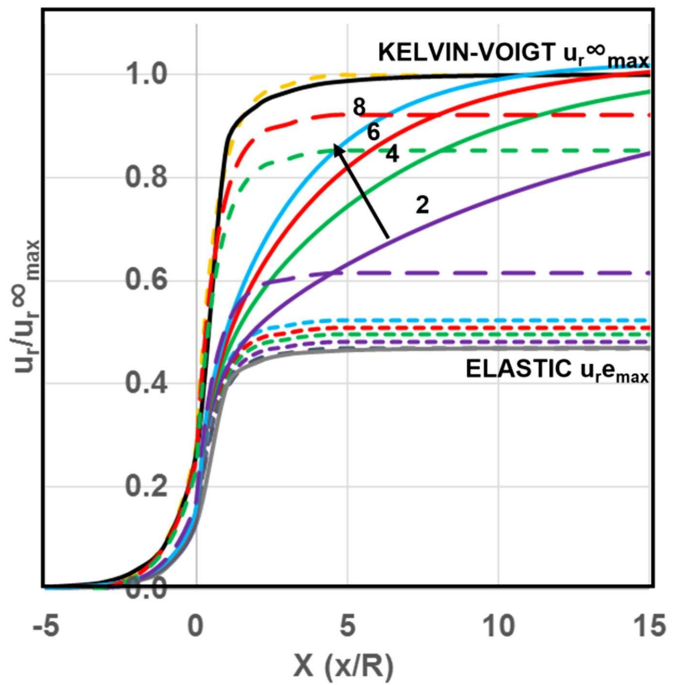
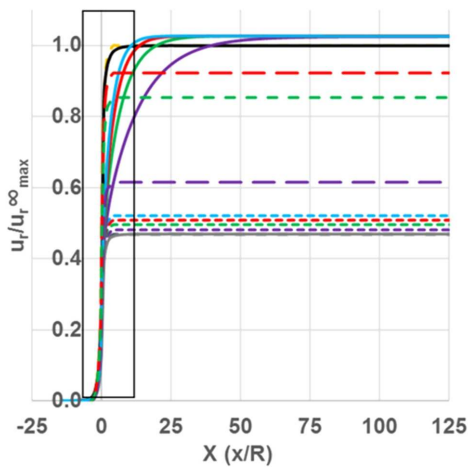


- 2 hours\_KV      — 4 hours\_KV
- 6 hours\_KV    — 8 hours\_KV
- ELASTIC        — KELVIN-VOIGT





### TBM



- ELASTIC (Vlachopoulos and Diederichs 2009)
- 2 hours (Panet 1979)
- 6 hours (Panet 1979)
- 2 days (Panet 1979)
- 6 days (Panet 1979)
- KELVIN-VOIGT
- 4 hours
- 8 hours
- KELVIN-VOIGT (Panet 1976)
- 4 hours (Panet 1979)
- 8 hours (Panet 1979)
- 4 days (Panet 1979)
- ELASTIC
- 2 hours
- 6 hours

## TABLES

Table 1. Analytical solutions for LDP calculation depending on the medium.

Table 2. Visco-elastic rheological models, their associated mechanical analogues, stress-strain and time-relationships.

Table 3. Visco-elastic models and analytical solutions for a circular unsupported tunnel. The analytical solutions for Kelvin-Voigt and Maxwell model are adopted from Panet (1979) and for Burgers from Fahimifar et al. (2010).

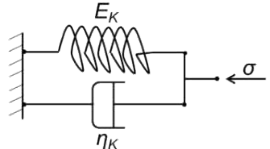
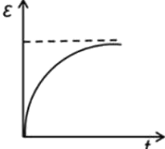
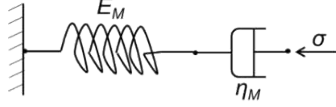
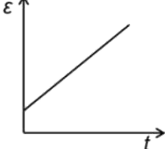
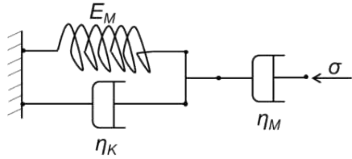
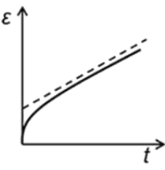
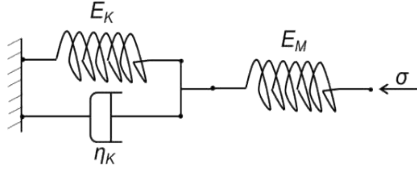
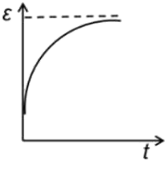
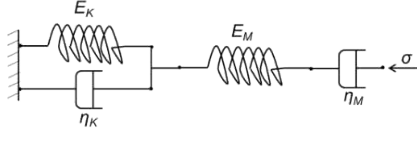
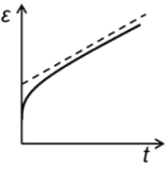
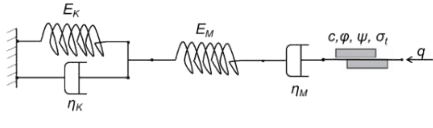
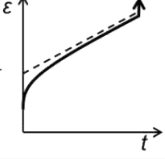
Table 4. Parameters used for CVISC model.

Table 5. Nomenclature and model runs in this study.

Table 1. Analytical solutions for LDP calculation depending on the medium.

Reference	Analytical Solution	Medium Behaviour
Panet and Guenot (1982)	$\frac{u_r}{u_{max}} = 0.28 + 0.72 \left[ 1 - \left( \frac{0.84}{0.84 + x/R} \right)^2 \right]$	Elasto-Plastic
Panet (1993, 1995)	$\frac{u_r}{u_{max}} = 0.25 + 0.75 \left[ 1 - \left( \frac{0.75}{0.25 + x/R} \right)^2 \right]$	Elastic
Corbetta et al. (1991)	$\frac{u_r}{u_{max}} = 0.29 + 0.71 \left[ 1 - \left( -1.5(x/R)^{0.7} \right) \right]$	Elastic
Chern et al. (1998)	$\frac{u_r}{u_{max}} = \left[ 1 + \exp \left( \frac{-x/R}{1.1} \right)^{-1.7} \right]$	Elasto-plastic
Unlu and Gercek (2003)	$\frac{u_r}{u_{max}} = \frac{u_o}{u_{max}} + A_a (1 - e^{B_a(x/R)}), \quad x/R \leq 0$ $\frac{u_r}{u_{max}} = \frac{u_o}{u_{max}} + A_b [1 - ((B_b + (x/R))^2)], \quad x/R \geq 0$ $\frac{u_o}{u_{max}} = 0.22\nu + 0.19, \quad x/R = 0$ $A_a = -0.22\nu + 0.19 \quad B_a = 0.73\nu + 0.81$ $A_b = -0.22\nu + 0.81 \quad B_b = 0.39\nu + 0.65$	Elastic
Vlachopoulos and Diederichs (2009)	$\frac{u_r}{u_{max}} = \frac{u_o}{u_{max}} e^{x/R}, \quad x/R \leq 0$ $\frac{u_r}{u_{max}} = 1 - \left( 1 - \frac{u_o}{u_{max}} \right) e^{(-3x/R)/(2r_p/R)}, \quad x/R \geq 0$ $\frac{u_o}{u_{max}} = \frac{1}{3} e^{-0.15(r_p/R)}, \quad x/R = 0$ <p style="text-align: center;"><math>r_p</math> - plastic radius</p>	Elasto-plastic

Table 2. Visco-elastic rheological models, their associated mechanical analogues, stress-strain and time-relationships.

Model	Mechanical Analogue	Stress-Strain – Time Relationships
<b>Kelvin</b>		 $\varepsilon(t) = \frac{\sigma}{E_K} \left[ 1 - \exp\left(-\frac{E_K t}{3\eta_K}\right) \right]$
<b>Maxwell</b>		 $\varepsilon(t) = \frac{\sigma}{E_M} + \frac{\sigma t}{3\eta_M}$
<b>Generalized Maxwell</b>		 $\varepsilon(t) = \frac{\sigma}{E_K} \left[ 1 - \exp\left(-\frac{E_K t}{3\eta_K}\right) \right] + \frac{\sigma t}{3\eta_M}$
<b>Generalized Kelvin (Kelvin-Voigt)</b>		 $\varepsilon(t) = \frac{\sigma}{E_M} + \left[ 1 - \exp\left(-\frac{E_K t}{3\eta_K}\right) \right]$
<b>Burgers</b>		 $\varepsilon(t) = \frac{\sigma}{E_M} + \left[ 1 - \exp\left(-\frac{E_K t}{3\eta_K}\right) \right] + \frac{\sigma t}{3\eta_M}$
<b>CVISC</b>		 $\varepsilon(t) = \frac{p}{3K} + \frac{q}{3G_M} + \frac{q}{3\eta_M} t + \frac{q}{3G_K} + \left[ 1 - \exp\left(-\frac{G_K}{\eta_K} t\right) \right]$

(It should be noted that for incompressible materials  $E=3G$ ).

Table 3. Visco-elastic models and analytical solutions for a circular unsupported tunnel (the analytical solutions for Kelvin-Voigt and Maxwell model are adopted from Panet (1979) and for Burgers from Fahimifar et al. (2010)).

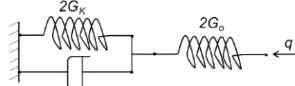
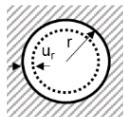
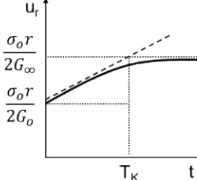
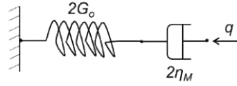
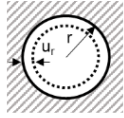
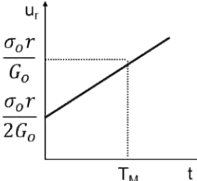
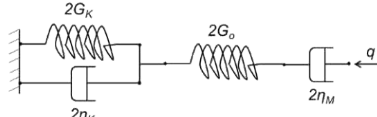
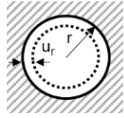
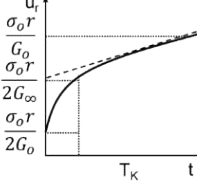
Model	Spring-Dashpot Analogues and Radial displacement – Time Analytical Solutions			
Kelvin-Voigt (Generalized Kelvin) <i>(primary)</i>	 $u_r = \frac{\sigma_o r}{2G_o} + \frac{\sigma_o r}{2G_K} \left[ 1 - \exp\left(-\frac{t}{T_K}\right) \right]$	$\frac{1}{G_\infty} = \frac{1}{G_o} + \frac{1}{G_K}$ $T_K = \frac{\eta_K}{G_K}$	 $\sigma_r = 0 \text{ for } t > 0$	
Maxwell <i>(secondary)</i>	 $u_r = \frac{\sigma_o r}{2G_o} \left[ 1 + \left( \frac{t}{T_M} \right) \right]$	$T_M = \frac{\eta_M}{G_o}$	 $\sigma_r = 0 \text{ for } t > 0$	
Burgers <i>(primary &amp; secondary)</i>	 $u_r = \frac{\sigma_o r}{2} \left\{ \frac{1}{G_o} + \frac{t}{\eta_M} + \frac{1}{G_K} \left[ 1 - \exp\left(-\frac{t}{T_K}\right) \right] \right\}$	$\frac{1}{G_\infty} = \frac{1}{G_o} + \frac{1}{G_K}$ $T_K = \frac{\eta_K}{G_K}$	 $\sigma_r = 0 \text{ for } t > 0$	

Table 4. Parameters used for CVISC model.

<b>Parameter</b>	<b>SET #1</b>	<b>SET #2</b>	<b>SET #3</b>
<b><i>Rockmass conditions</i></b>			
$\gamma$ (KN/m <sup>3</sup> )	20	20	20
$\varphi$ (°)	23	23	23
c (MPa)	1.00E+20	1.00E+20	1.00E+20
t (MPa)	1.00E+20	1.00E+20	1.00E+20
K (MPa)	1.23E+03	4.32E+04	4.70E+03
<b><i>Stress Conditions</i></b>			
$k_0$	1	1	1
$p_0$ (or $\sigma_0$ ) (MPa)	7	7	7
<b><i>Visco-elastic Parameters*</i></b>			
$G_K$ (MPa)	4.98E+02	6.73E+04	3.29E+03
$\eta_K$ (MPa*s)	1.34E+08	1.72E+09	1.49E+07
$G_0$ or $G_M$ (MPa)	5.66E+02	1.99E+04	2.17E+03
$\eta_M$ (MPa*s)	8.82E+08	1.20E+10	3.60E+09
$T_K = \eta_K/G_K$ (s)	2.69E+05	2.56E+04	4.52E+03
<b><i>Reference*</i></b>	Barla et al. 2010	Zhang et al. 2012	Feng et al. 2006



Table 5. Nomenclature and model runs in this study.

Model	Time per excavation cycle	CASE 1 - D&B (3m/exc.)			CASE 2 - TBM (3m/exc.)		
		SET#1	SET#2	SET#3	SET#1	SET#2	SET#3
<i>KELVIN-VOIGT (KV)</i>	2 hours	X	X	X	X	X	X
	4 hours	X	X	X	X	X	X
	6 hours	X	X	X	X	X	X
	8 hours	X	X	X	X	X	X
<i>BURGERS (B)</i>	2 hours	X	X	X	X	X	X
	4 hours	X	X	X	X	X	X
	6 hours	X	X	X	X	X	X
	8 hours	X	X	X	X	X	X
<i>KELVIN-VOIGT*</i>	infinite excavation delay	X	X	X	X	X	X
<i>ELASTIC*</i>	instantaneous excavation	X	X	X	X	X	X

*\*no time between excavation stages was considered in these models although in the KV model, both springs in series were considered active (zero viscosity in the Kelvin dashpot)*

## LIST OF SYMBOLS - GLOSSARY

CCM	Convergence Confinement Method
CVISC	Burgers visco-plastic Model
LDP	Longitudinal Displacement Profile
GRC	Ground Reaction Curve
SCC	Support Characteristic Curve
E	Young's modulus
el	elastic
G or $G_0$	shear modulus
$G_K$	Kelvin shear modulus
$G_M$	Maxwell shear modulus
$1/G_\infty$	harmonic average
K	bulk modulus
$p_0$	in situ stress
$p_i$	internal pressure
q	deviatoric stress
$q_{cr}$	critical deviatoric stress
r	radius
$r_p$	plastic radius
R	tunnel radius
t	time
$u_r$	radial displacement
$u_{r\max}$	maximum elastic displacement
$u_{r\max}^\infty$	maximum visco-elastic displacement
$\nu$	Poisson's ratio
$\nu_e$	visco-elastic
$\nu_p$	visco-plastic
x	distance from the tunnel face
y	yielding
$\eta$	viscosity
$\eta_K$	Kelvin viscosity
$\eta_M$	Maxwell viscosity
$\varepsilon$	strain
$\dot{\varepsilon}$	strain-rate
$\varepsilon^P$	axial strain due to primary stage of creep

$\epsilon^s$	axial strain due to secondary stage of creep
$\epsilon^{tet}$	axial strain due to tertiary stage of creep
$\sigma$	stress
$\sigma_0$	in situ stress
$\sigma_r$	radial stress
$\sigma_{xx}$	minor stresses
$\sigma_{zz}$	major stresses
T	denotes the retardation – relaxation time of each model