

Rapid Spatial Mapping of Focused Ultrasound Fields Using a Planar Fabry-Pérot Sensor

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Abstract—Measurement of high acoustic pressures is necessary in order to fully characterise clinical high-intensity focused ultrasound (HIFU) fields, and for accurate validation of computational models of ultrasound propagation. However, many existing measurement devices are unable to withstand the extreme pressures generated in these fields, and those that can often exhibit low sensitivity. Here, a planar Fabry-Pérot interferometer with hard dielectric mirrors and spacer was designed, fabricated, and characterised and its suitability for measurement of nonlinear focused ultrasound fields was investigated. The noise equivalent pressure of the scanning system scaled with the adjustable pressure detection range between 49 kPa for pressures up to 8 MPa and 152 kPa for measurements up to 25 MPa, over a 125 MHz measurement bandwidth. Measurements of the frequency response of the sensor showed that it varied by less than 3 dB in the range 1 - 62 MHz. The effective element size of the sensor was 65 μm and waveforms were acquired at a rate of 200 Hz. The device was used to measure the acoustic pressure in the field of a 1.1 MHz single element spherically focused bowl transducer. Measurements of the acoustic field at low pressures compared well with measurements made using a PVDF needle hydrophone. At high pressures, the measured peak focal pressures agreed well with the focal pressure modelled using the Khokhlov-Zabolotskaya-Kuznetsov equation. Maximum peak positive pressures of 25 MPa, and peak negative pressures of 12 MPa were measured, and planar field scans were acquired in scan times on the order of 1 minute. The properties of the sensor and scanning system are well suited to measurement of nonlinear focused ultrasound fields, in both the focal region and the low pressure peripheral regions. The fast acquisition speed of the system and its low noise equivalent pressure are advantageous, and with further development of the sensor, it has potential in application to HIFU metrology.

Keywords: HIFU, Field mapping, Fabry-Pérot, Acoustic pressure measurement

I. INTRODUCTION

THE measurement of high intensity focused ultrasound (HIFU) fields is critical in monitoring the stability of clinical ultrasound therapy systems, in validating models of ultrasound propagation, and in understanding these complex acoustic fields and their bioeffects. In order to fully characterise clinical therapeutic ultrasound fields, they must be measured at clinical levels where extremely high pressures of over 100 MPa are generated in the focal region [1, 2]. In the ideal case, a suitable sensor for these conditions must be robust enough to withstand high pressures, temperatures

and cavitation, and have a high dynamic range (≥ 60 dB) and low noise equivalent pressure ($\lesssim 100$ kPa) suitable for measuring the high-pressure focal region and low pressures elsewhere in the field. It must also have a wide bandwidth ($> 100 - 150$ MHz) to capture high frequency harmonics, and a small element size ($< \lambda/4$) to avoid spatial averaging in the narrow focal region and to provide an omnidirectional response. Ideally, measurements would also be acquired rapidly, to reduce uncertainty due to fluctuations in the experimental conditions. At present, there are no sensors that fulfil all of these criteria. In this paper, the usefulness of an optical sensor and scanning system in addressing these requirements is investigated and applied to the measurement of a nonlinear ultrasound field.

A. Existing sensors

Currently available acoustic pressure sensors used for the measurement of ultrasound fields fall into two categories: piezoelectric sensors and optical sensors. Conventional piezoelectric hydrophones can be easily damaged by cavitation, heating and direct mechanical effects. While purification and degassing of the test medium (usually water) can increase the threshold for cavitation, and use of a low duty cycle will reduce heating, damage is likely to occur eventually. One study has reported the use of a conventional PVDF membrane hydrophone for measurement of pressures up to peak positive and negative pressures of 27 MPa and 10 MPa before cavitation occurred, damaging the hydrophone [3]. However, exposing expensive hydrophones to pressures close to this level poses a significant risk, especially where water quality cannot be guaranteed. The pressure range of most piezoelectric sensors is also limited, often to 10 or 20 MPa, by the dynamic range of components such as preamplifiers. This limits them to the measurement of relatively low amplitude fields [4].

Small sensitive element sizes are desirable for measuring fields with high frequency content. Although piezoelectric probe hydrophones with element sizes as small as 40 μm are available, decreasing sensor size leads to a lower sensitivity and the frequency response of these types of hydrophone can be non-uniform [5]. Piezoelectric membrane hydrophones exhibit a more uniform frequency response but are only commercially available with 0.2 mm diameter elements at the smallest. Spatial averaging caused by relatively large element sizes can lead to significant underestimation of the peak positive focal pressure in highly nonlinear focused fields where the width of the focal peak may be less than 1 mm [1, 6].

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Some piezoelectric hydrophones with extra coatings or layers added to increase their robustness have been reported in the literature. For example, a metal coated piezoceramic needle hydrophone was reported capable of measuring up to 25 MPa peak positive and 9 MPa peak negative pressure before damage occurred [7, 8]. A PVDF membrane hydrophone with protective stainless steel and polymer coatings, designed for use in HIFU fields is also available. Its use has been demonstrated for measurement of pressures up to approximately 60 MPa [6]. By further adapting this design with a polyurethane backing layer, the measurement of pressures up to 75 MPa peak positive and 15 MPa peak negative was demonstrated, restricted by the operating limits of the transducer [3]. Both of these devices maintain low NEP of 45 kPa and 65 kPa for the two designs respectively. These hydrophones have relatively large element sizes (≥ 0.2 mm) and somewhat limited bandwidths of 10 MHz for the robust needle hydrophone and 40 MHz for the robust membranes. The usable bandwidth of the robust membrane hydrophone was extended in this work however, by deconvolution of the full frequency response of the hydrophone [3]. Limited measurement bandwidth can lead to underestimation of the peak positive focal pressure if all harmonics are not captured [6].

Optical sensors such as the fibre optic hydrophone (FOPH), provide an alternative to the piezoelectric hydrophone, in general with the advantage of small element size and broad bandwidth [4, 9]. The Eisenmenger type fibre optic hydrophone is based on pressure-induced refractive index changes at the tip of an optical fibre and has been used to measure upwards of 100 MPa peak positive pressure and 18 MPa peak negative pressure [2, 10]. This is a suitable candidate for the measurement of HIFU fields due to its small size (100 - 125 μm element size) and wide bandwidth (~ 100 MHz). It is also robust and has the advantage that the tip of the fibre can easily be re-cleaved to form a new fibre tip in the event of damage. However, its high noise equivalent pressure (NEP) of more than 0.5 MPa [9, 11] (up to 2-3 MPa [6]) renders it unsuitable for mapping regions of lower pressure.

Higher sensitivity has been achieved with Fabry-Pérot polymer film ultrasound sensors [12, 13]. These sensors comprise a polymer film spacer sandwiched between a pair of mirrors and can be deposited on to either a planar substrate or the tip of an optical fibre. The exact construction of the mirrors, spacer, and substrate can be adjusted to optimise the sensitivity and bandwidth for a given application. For example, as part of the photoacoustic scanner described in [13], a sensor with a 22 μm spacer had a noise equivalent pressure (NEP) of 0.31 kPa over a 20 MHz measurement bandwidth, and -3 dB bandwidth of 39 MHz. These NEP are extremely low compared to the 50 kPa NEP associated with a 75 μm PVDF needle hydrophone [14]. While ideally suited to use in photoacoustic imaging when high sensitivity is required for the detection of low amplitude signals, this polymer spacer construction is not robust to high pressures and the upper limit of linear detection is low, typically a few MPa.

To enable characterisation of HIFU fields at both low and high outputs, a sensor that combines the individual benefits of the existing sensors in terms of robustness, small size,

broad bandwidth, and low NEP is required. It may be possible to address these requirements using a Fabry-Pérot type sensor, by employing hard dielectric material to form the spacer rather than a polymer film. Previously, both fibre mounted and planar glass backed sensors of hard dielectric construction have been demonstrated [15, 16]. A planar sensor formed from SiO_2 and NbO_2 mirrors with a $\lambda/2$ SiO_2 spacer, 1.9 μm thick in total, was shown to have a flat frequency response from 1 - 75 MHz, with a linear range of 37 MPa [15]. The suitability of this type of sensor has been demonstrated for mapping nonlinear diagnostic ultrasound fields [17], and as a reference sensor for amplitude and phase calibration of hydrophones [18]. However, it has not previously been used for mapping HIFU fields.

B. Field scanning techniques

Currently, the most common method of acoustic field mapping is mechanical scanning of piezoelectric or fibre optic hydrophones, which are commonly used for scanning at high output levels [1, 2, 19]. Measurement requirements are specified in the standards IEC 62127-1 [20] and IEC TS 62556 [21]. In general, an automatic positioning system is used to move a hydrophone in small steps through the acoustic field generated by a transducer mounted in a large tank of degassed and deionised water. Typically, the hydrophone is moved and waveforms acquired with a frequency on the order of 1 scan point per second, with a spatial step size of less than half the acoustic wavelength. Consequently, it can take several hours to adequately sample the field of a typical HIFU transducer. Over these timescales, measurement errors are possible due to fluctuations in the source, hydrophone, and environmental conditions.

Other methods of acoustic field mapping have also been employed, which have some advantages in terms of acquisition speed and robustness. One approach to measuring high acoustic pressures, which removes the possibility of damaging sensors, is to use a noninvasive method. Historically, Schlieren imaging has been used to visualise ultrasound fields. Through projection images can be obtained in real time, but do not give quantitative information. More recently, a quantitative tomographic optical phase contrast measurement method has been described by Oyama et al. [24]. However, due to difficulties with optical phase unwrapping, the acoustic pressure amplitude that can currently be measured using this approach is reported to be less than 10 MPa.

Planar Fabry-Pérot sensors [13] can also be used to make fast measurements of acoustic pressure. The sensors are interrogated by a scanning laser beam rather than mechanically scanning the sensor itself, enabling rapid data acquisition. These sensors have been used extensively in photoacoustic imaging (e.g. [13]), for ultrasonic field mapping [17, 25, 26], and for measurement of temperature and acoustic pressure for characterisation of acoustic properties of materials [27].

C. Paper outline

In this paper, the design of a robust planar Fabry-Pérot sensor suitable for measurement of high acoustic pressures

is discussed. This builds on the work reported in [15], using a similar sensor formed from all hard dielectric materials, but which has instead been designed to operate at 1550 nm, coupled with a C-L (1516–1610 nm) band wavelength tuneable laser and rapid scanning system. A full characterisation of the sensor in terms of its frequency response, directivity and noise equivalent pressure is presented in addition to a set of measurements of a HIFU field made with the sensor. Section II discusses the transduction mechanisms of the Fabry-Pérot sensor, and the construction of the sensor and scanning system. In Section III, the measured on-axis and directional frequency response and the NEP of the sensor are reported. Measurements of the field of a spherically focused ultrasound transducer at a range of drive levels are presented in Section IV.

II. THE FABRY-PÉROT INTERFEROMETER

A. Transduction mechanisms

A Fabry-Pérot interferometer (FPI) consists of two plane parallel mirrors separated by a cavity or spacer. Incident light is multiply reflected from the mirrors and the multiple beams interfere at the first mirror (Fig. 1a). The variation in optical power reflected from the FPI as a function of interrogation laser wavelength is termed the interferometer transfer function (ITF) and is shown in Fig. 1b. The sensor is optimally biased by tuning the laser wavelength so that it corresponds to the maximum gradient of the ITF. Under these conditions, when the FPI is placed in an acoustic field, its optical thickness is modulated by the acoustic pressure causing a phase shift which results in a corresponding modulation of the optical power reflected from the sensor.

The overall sensitivity of a Fabry-Pérot sensor depends on both the optical phase sensitivity, which is the change in reflected optical power per unit phase shift and the acoustic phase sensitivity, which is the optical phase shift per unit acoustic pressure [28]. The optical phase sensitivity depends on the power of the interrogating light and the reflectivity of the interferometer mirrors. The acoustic phase sensitivity is governed mainly by the optical and mechanical properties of the sensor. The incident pressure field induces small changes in the refractive index and thickness of the layers forming the mirrors and spacer, which modulates the reflected optical power [16].

The reflectivity finesse of a sensor is defined as the ratio of the separation in wavelength of consecutive minima in the ITF to its full width half maximum. A very high finesse sensor has a steep ITF and is extremely sensitive to small optical phase changes generated by small changes in acoustic pressure, but as such has a very limited detection range.

As discussed in Sec. I-A, forming the interferometer from SiO₂ hard dielectric mirrors and spacer provides the necessary robustness. However, the acoustic phase sensitivity is dependent on the refractive index and Young's modulus and will be reduced compared to the polymer based sensors ($n = 1.444$ and $E = 73$ GPa for SiO₂ [30] cf. $n = 1.65$ [13] and $E \sim 3$ GPa for Parylene C [31]). However, for measurement of high acoustic pressures, an increase in the upper limit of pressure

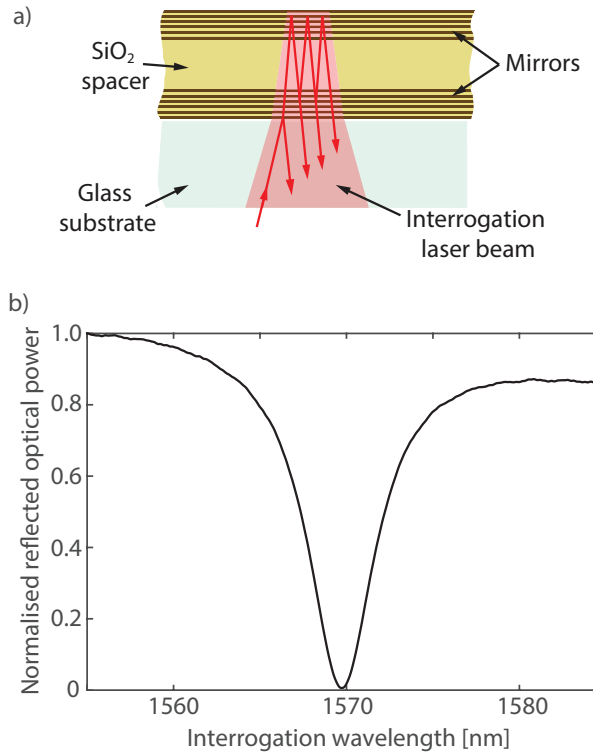


Fig. 1. a) Schematic diagram of the mirrors and spacer layers forming the Fabry-Pérot interferometer deposited on the glass substrate. The interferometer is interrogated by a scanned focused laser beam which is multiply reflected from the mirrors. b) The interferometer transfer function measured for the sensor.

detectable by the sensor is desirable and thus the decrease in acoustic phase sensitivity is acceptable. To offset the reduction in acoustic phase sensitivity, the optical phase sensitivity can be increased by increasing the reflectivity of the mirrors. The detection bandwidth of the sensor is related to the spatial variation of pressure across the interferometer and is therefore dependent on the thickness of the multilayer structure [32], with thinner sensors having a wider bandwidth.

B. Sensor construction

As discussed in Section II-A, to increase the linear range and robustness of the sensor and maintain optical phase sensitivity, the sensor used in this work was designed with an all hard dielectric construction. The mirrors were constructed from six sets of alternate layers of SiO₂ and ZrO₂ separated by a 3.9 μm SiO₂ spacer. In this proof of concept design, all layers were deposited by electron beam-gun evaporation onto a 3 mm thick glass substrate. A parylene barrier coating was then applied to the sensor. This substrate was glued to another 16 mm thick glass plate to increase the time of arrival of acoustic reflections from the back of the substrate. The pressure reflection coefficient of the boundary between the two glass plates was measured to be less than 0.1 at 20 MHz, and lower at lower frequencies. In future designs, the interferometer structure will be deposited onto a single thicker substrate to provide the necessary time delay between the incident field and its reflection. The bottom face of the glass

substrate was shaped into a wedge to eliminate parasitic optical reflections. The free spectral range of the sensor was 220 nm at an interrogation wavelength of 1569.5 nm, the reflectivity finesse was 48.9 and the visibility was 0.83.

C. Scanner system

The scanning system was as previously described in [13]. To interrogate the sensor, a focused laser beam tuneable in the range 1440 nm to 1640 nm (Tunics T100S-HP, Yenista Optics, France) was scanned across the sensor using a pair of orthogonal galvanometer mirrors (Edmund Optics, York, UK). The maximum scan area was 28 mm by 30 mm. The waveform acquisition rate was 200 Hz, limited by the movement of the galvanometer mirrors and the tuning of the interrogation laser wavelength. To maximise the sensitivity of the sensor, the wavelength of the incident light is tuned to the maximum gradient of the ITF at each point. For the hard dielectric sensor, the thickness of the interferometer is very uniform and so the bias wavelengths lie within a range of approximately 1 nm.

Fabry-Pérot sensors of both polymer and hard-dielectric construction have previously been shown to be temperature sensitive [12, 33]. Thermally induced changes in optical thickness cause changes in the reflectance of the sensor, resulting in a change in the DC voltage at the photodiode. In the current work, the sensor was not used to measure temperature. The low duty cycle and short pulse length employed in these measurements kept heating to a minimum and any temperature-induced shifts in the ITF were within the linear range of the ITF. No change in sensitivity was observed following measurements.

At each scan point, the reflected light was measured by an InGaS photodiode [13], and the resulting voltage signal digitised by a digital storage oscilloscope and downloaded to a PC to build up a 2D map of the time varying acoustic field distribution. The signals acquired at each scan point were corrected for the sensitivity of the interferometer by division by the maximum gradient of the ITF at that point on the sensor. The effective element size of the sensor is optically defined by the spot size of the incident laser light source ($65 \mu\text{m}$) [13] which minimises spatial averaging.

III. SENSOR CHARACTERISATION

A. Linearity and sensitivity

The linear range of the sensor was determined from the measured ITF shown in Fig. 1(b), and the pressure sensitivity of the system. The linear range of the sensor is defined as the range over which a straight line at a tangent to the point of maximum gradient (the bias point) of the measured ITF lies within 5% of the ITF. For the sensor used here, the linear range was 35 MPa to within 5% (allowing for the doubling in pressure at the sensor surface), and 56 MPa to within 10%. The dynamic range of the system was 49 dB.

The noise equivalent pressure (NEP) of the system was obtained as follows. First, the pressure sensitivity of the system in mV/MPa was determined from the sensor output relative to a calibrated hydrophone using an incident acoustic wave emitted by a plane-piston transducer. Then the noise voltage was calculated as 3 standard deviations of the signal measured

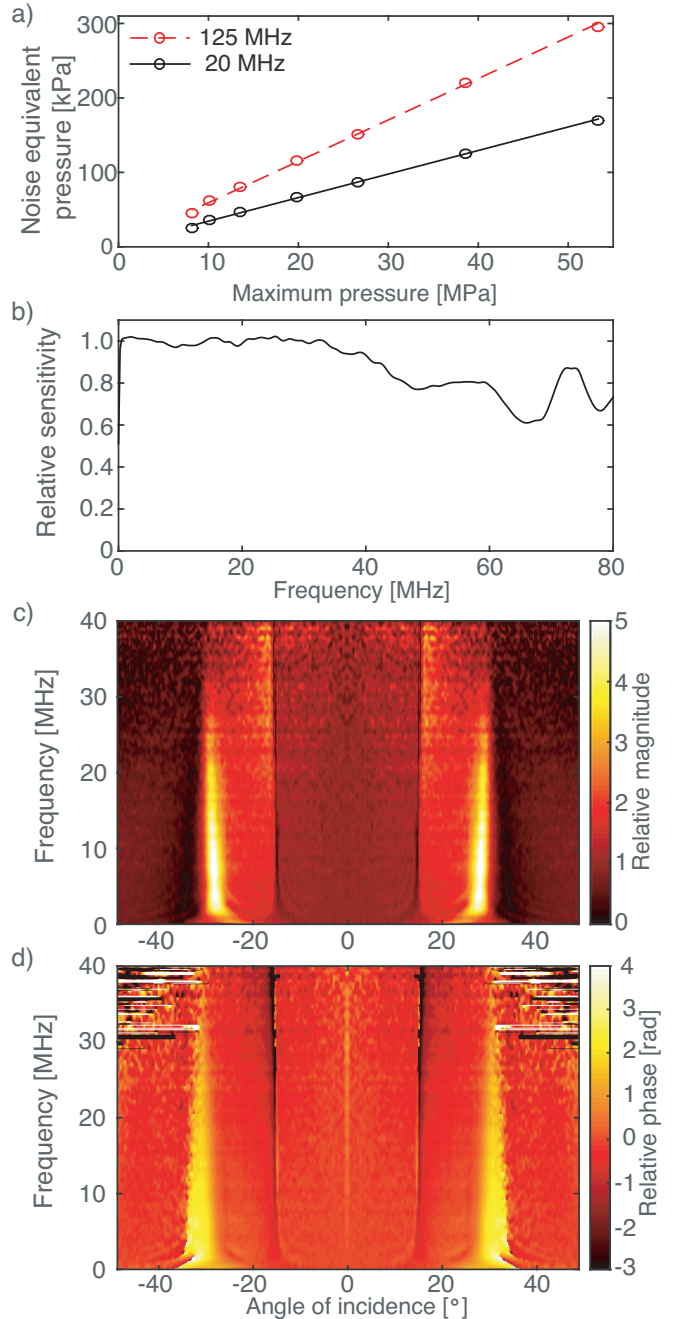


Fig. 2. (a) The noise equivalent pressure of the system as a function of the upper limit of detectable pressure of the system. (b) The relative normal incidence frequency response of the sensor. (c) Magnitude of the directional response normalised to 1 at $\theta = 0$. (d) Phase of the directional response referenced to 0 at $\theta = 0$.

over a segment of the detected waveform in a time window immediately before the arrival of the acoustic signal. The NEP was then given by the ratio of the noise to the sensitivity. This was calculated over the full 125 MHz measurement bandwidth used for measurements and over a 20 MHz bandwidth for comparison with other sensors.

During measurements, the reflected interrogation light was measured by a photodiode which has a peak-to-peak saturation voltage of 5 V. The measured voltage is proportional to the product of the sensitivity of the sensor, the interrogation laser

power, and the acoustic pressure. It is therefore possible to adjust the measurement range of the system by changing the power of the interrogation laser. A low interrogation laser power is used for measuring high pressures and a high laser power is used to increase the signal to noise ratio for measurement of low pressures. The NEP of the system scales with the interrogation laser power, as shown in Fig. 2a. At the lower end of the pressure range (up to 8 MPa), the NEP over a 20 MHz bandwidth is 26 kPa. This is lower than the 50 kPa NEP associated with a similar sized 75 μm PVDF needle hydrophone [14]. At the upper end of the linear range (56 MPa), the NEP is approximately 170 kPa over a 20 MHz bandwidth or 295 kPa over a 125 MHz bandwidth. This is lower than the NEP of the Eisenmenger type fibre optic hydrophone which has an NEP of 500 kPa or more [9, 11], but higher than the robust membrane hydrophones used to measure high amplitude acoustic fields [3].

B. Frequency response

The relative normal incidence frequency response of the sensor was obtained by substitution calibration against a Fabry-Pérot sensor with a 20 μm Parylene-C spacer and gold mirrors. The frequency response of this sensor was previously measured and modelled as described in [28] and had a -3dB bandwidth of 35 MHz; this will be herein referred to as the reference sensor. The sensor was mounted in the base of a water bath. An acoustic field was photoacoustically generated by laser light incident on a 2.5 cm diameter plane black absorber, which generated a planar monopolar acoustic pulse containing energy at frequencies up to approximately 80 MHz. The source was placed at a distance of 6 mm from the sensor and signals were acquired using the hard dielectric sensor from 9 points at the centre of the acoustic field distribution. At these positions in the acoustic field, the plane direct wave was temporally isolated from the edge waves, which were gated out, leaving only the plane wave. The sensor was then replaced by the reference sensor and the measurements were repeated. Signals were acquired with 2200 averages at each measurement point. The signals were then windowed using a 0.25 μs Tukey window centred on the pulse, and their Fourier transforms were obtained. The magnitudes of the FFTs were normalised and averaged. The frequency dependent relative sensitivity of the hard dielectric sensor was then calculated by

$$S_{HD}(f) = S_G(f) \frac{\mathcal{F}_{HD}(f)}{\mathcal{F}_G(f)}, \quad (1)$$

where $S_G(f)$ is the sensitivity of the reference sensor, \mathcal{F}_{HD} is the Fourier transform of the signal acquired from the hard dielectric sensor and \mathcal{F}_G is the Fourier transform of the signal acquired from the reference sensor. The relative frequency response of the sensor is shown in Fig. 2b. The measured response was constant to within 1 dB in the range 1 to 40 MHz and to within 3 dB up to 62 MHz. The fluctuations beyond this range may be due to the low SNR of the reference sensor signals due to its bandwidth (35 MHz -3 dB bandwidth, sensitivity decreasing to a minimum at approximately 90 MHz). Previously, a planar SiO_2 sensor of smaller thickness

(1.9 μm in total) was shown to have a frequency response that was constant to within the calibration uncertainty in the range 1 to 75 MHz [15]. It may be expected that the frequency response of the sensor measured here would be similar in terms of its flatness, although with a reduced bandwidth given its larger thickness.

C. Directional response

The directional response of the sensor was measured as described in [29], using the same broadband optically generated acoustic field as used to measure its frequency response. The source was mounted on a rotation stage to control the angle of incidence of the field on the sensor. The source was aligned such that its centre of rotation was coincident with the sensor surface and the beam axis was aligned with the centre of the sensor area. The source to sensor distance was approximately 30 mm to allow the lens tube holding the source to rotate within the walls of the tank. The angle of the source was stepped in 0.25° increments from -49° to +49°. At each angle the signal was acquired with 20 averages with the pulse centred in a 2 μs window. A Tukey window the same length as the acquired data was applied to the signals and their Fourier transforms were acquired. The magnitude of the spectra were normalised to the normal incidence values, and the unwrapped phase of the spectra was set to 0 at normal incidence for each frequency. The measured data was then smoothed by fitting splines.

The magnitude and phase of the directional response of the sensor are plotted as a function of angle and frequency in Fig. 2c and d, respectively. As the figure shows, the directional response of the sensor is not uniform with angle and several major features are observed. Below the critical angle for compressional waves at the water to glass interface ($\sim 15^\circ$ assuming a speed of sound in water at 21°C of 1488 ms^{-1} and a speed of sound in glass of 5640 ms^{-1} [30]), the magnitude and phase response are relatively flat. At the critical angle there is a sharp increase in the magnitude response accompanied by a minimum in the phase response. There is a second sharp increase in the magnitude response which coincides with the critical angle for shear waves at the water to glass interface ($\sim 27^\circ$ assuming a shear speed of 3280 ms^{-1} [30]). The maxima and minima in the magnitude response are accompanied by rapid changes in the phase response. When the second critical angle is reached, other wave modes begin to influence the response. The exact nature of all wave modes involved is not currently known, and is the subject of ongoing work.

The complexity of the directional response of this sensor could give rise to errors in measurements of acoustic pressure, especially in focused and geometrically complex fields, as has been previously reported [26]. For example, for the spherically focused transducer used in this work, in the focal region, waves will be incident at angles up to 30.4° (the angle subtended at the focus by the radius of the transducer) which exceeds both critical angles. A correction for the directional response is therefore necessary. This correction can be made

by deconvolving the directional response from the signals measured over a 2D plane:

$$P(x, y, t) = \mathcal{F}^{-1} \left(\frac{M_{\text{meas}}(k_x, k_y, \omega)}{D(k_x, k_y, \omega)} \right), \quad (2)$$

where \mathcal{F}^{-1} is the inverse Fourier transform, $M_{\text{meas}}(k_x, k_y, \omega)$ is the 3D Fourier transform of the measured time domain acoustic signals acquired over a planar area, k_x and k_y are the x and y wavenumber components, ω is the angular frequency and $D(k_x, k_y, \omega)$ is the directional response of the sensor.

In practice, this correction is implemented as follows. The measured data is zero padded to achieve sufficient sampling in k -space, as undersampling will result in an interpolation error when the correction is applied. The 3D Fourier transform of the measured data is then calculated, along with the corresponding k_x, k_y and ω values. Incidence angles for each wavenumber component are then calculated by

$$\theta = \tan^{-1} \left(\sqrt{\frac{k_x^2 + k_y^2}{\frac{\omega^2}{c^2} - k_x^2 - k_y^2}} \right). \quad (3)$$

Next, the directional response is interpolated onto the angle and frequency space occupied by the Fourier transform of the measured data. The correction is then applied by dividing the magnitude of the FFT of the data by the magnitude of the directional response and subtracting the phase of the directional response from the phase of the Fourier transform of the measured data. The magnitude and phase are then combined into a complex number, and the inverse Fourier transform is calculated.

In practice, deconvolution of the directional response from the measured signals introduces noise into the corrected time domain data. Just above the shear wave critical angle, the magnitude of the response is very low and so the SNR of the corresponding data will be very low. Applying the correction at these points is likely to introduce significant noise into the corrected data. To avoid this, the magnitude of the directional response correction ($1/|D(k_x, k_y, \omega)|$) was windowed to smooth these regions. A top hat window was applied, with a width determined by the angular position of the minimum in the correction at each frequency. For the correction at angles exceeding this, the correction was set to the value at the edge of the window.

IV. HIFU FIELD MEASUREMENTS

A. Ultrasound source and driving system

To demonstrate the suitability of the hard dielectric Fabry-Pérot sensor and rapid scanning system for ultrasonic field mapping, measurements of the field of a focused transducer were performed at a range of drive levels. The FP sensor, which had an area of 50 mm by 30 mm, was mounted in an aperture in the base of a specially designed water bath filled with deionised water, which was mounted above the optics necessary for interrogation of the sensor. The water was degassed by boiling to a dissolved oxygen concentration of approximately 2 mg/l. Temperature control was provided by a polythene tube heat exchanger through which water was circulated from a thermostatically controlled water bath

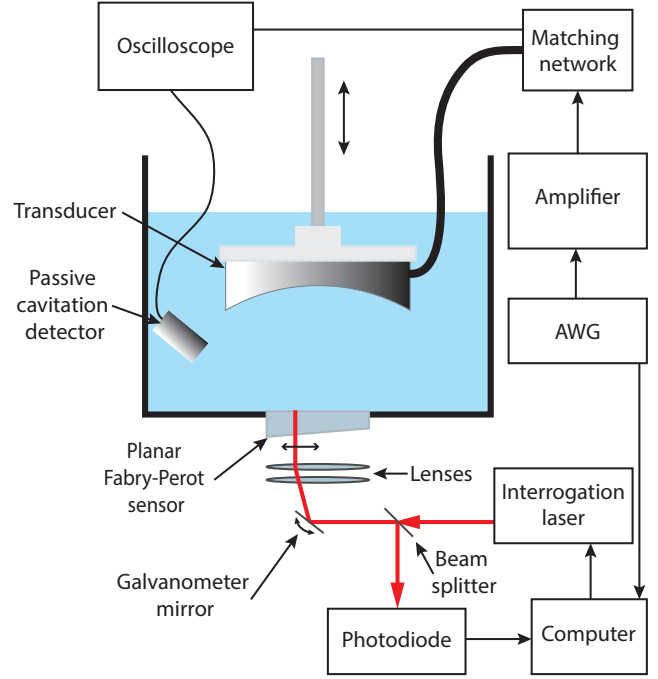


Fig. 3. Schematic of experimental configuration

(Eco Silver RE 415S, Lauda, Germany). A diagram of the experimental arrangement is shown in Fig. 3. An acoustic field was generated by a single element spherically focused bowl transducer (H101, Sonic Concepts, Bothell, WA, USA) mounted in the top of the water bath. The transducer had an active area diameter of 64 mm and focal length of 63.2 mm [22]. The transducer was driven with a 4 cycle burst at 1.1 MHz. Input signals were generated by an Agilent 33522A Arbitrary Waveform Generator (Agilent, Berkshire, UK) before amplification by an E&I A300 RF power amplifier (Electronics & Innovation Ltd., Rochester, NY). This was coupled to the transducer via an impedance matching network. The transducer drive signal was monitored using an Agilent oscilloscope probe and Agilent DSO-X3204 oscilloscope (Agilent, as above). A 10 mm diameter 4 MHz PVDF transducer was used for passive cavitation detection (the signal and spectrum were monitored using the oscilloscope).

B. Comparison with hydrophone measurements at low pressure

For comparison, measurements of the acoustic field were made at a low drive level with both the Fabry-Pérot sensor and a calibrated 0.2 mm PVDF needle hydrophone (Precision Acoustics Ltd., Dorchester, UK; hydrophone calibration provided by the National Physical Laboratory, Teddington, UK). Hydrophone measurements were performed in a tank of deionised water, with the hydrophone positioned using a scanning tank with 5 computer controlled translation stages (Precision Acoustics, as above). The transducer was driven as described in Sec. IV-A with a peak to peak drive voltage of 36 V. For the hydrophone measurements, the drive voltage was monitored using a Tektronix TPP0850 oscilloscope probe and

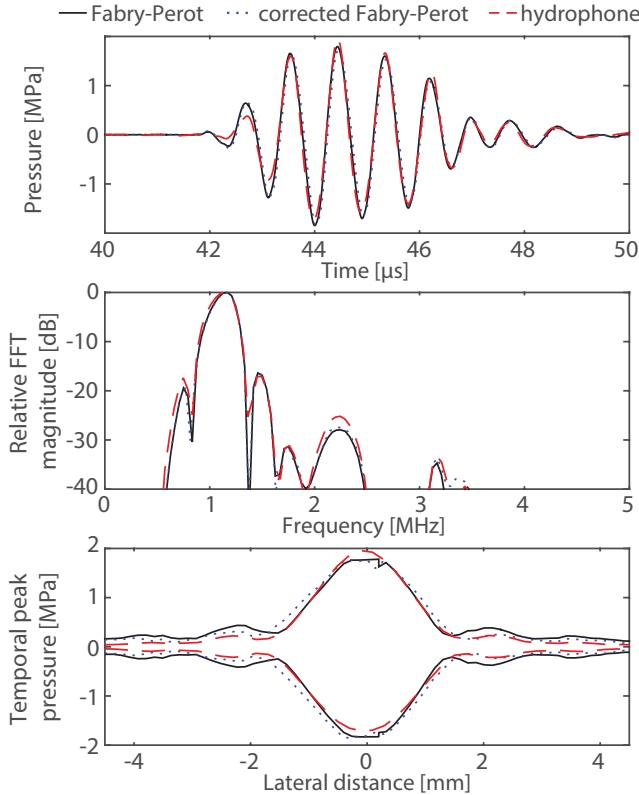


Fig. 4. Focal waveforms, spectra and transverse beam profile of peak positive and peak negative pressure are shown for measurements made using a 0.2 mm PVDF needle hydrophone (red dashed line) and the Fabry-Pérot sensor. The solid black line shows the uncorrected Fabry-Pérot data and the dotted blue line shows the same data corrected for the directional response of the sensor.

Tektronix DPO5034B Digital Phosphor Oscilloscope (Tektronix, UK Ltd., Berkshire, UK). The same oscilloscope was also used to digitise the hydrophone signal with a sampling frequency of 125 MHz and 32 averages. Waveforms were then captured and stored via the scanning tank software. Axial and transverse line scans passing through the focus of the field were made with a step size of 0.2 mm. A bandpass filter was applied to the signals (0.35 - 20 MHz pass band) and the frequency dependent sensitivity of the hydrophone was deconvolved from the measured waveforms to obtain the measured pressure.

A planar scan at the focal distance was then acquired with the Fabry-Pérot scanning system with 16 averages and a step size of 0.1 mm (45×45 points). A line passing through the focal point of the field was then extracted from this measured plane. The signals were bandpass filtered (as above) and the measured directional response and frequency response of the sensor was deconvolved. The focal waveforms, spectra and transverse peak positive pressure profiles are plotted for comparison in Fig. 4.

There are some differences between the beam profiles from the two sets of measurements. The shape of the main focal lobe is well captured by the Fabry-Pérot measurements but there are discrepancies in the side lobes in the uncorrected Fabry-Pérot data. However, it can be seen that correcting for the directional response significantly reduces the differences

in amplitude at the first side lobe to less than 10%. The improvement is not as good in the second side lobe, most likely due to the windowing of the directional response that was applied to suppress noise in the corrected data. The windowing smooths the correction at angles of incidence above the shear wave critical angle of the water to glass interface, and therefore mainly affects measurement of pressure in the side lobes. The implementation of the directional response correction will be improved in future work.

C. Measurement of HIFU fields at higher drive levels

Two advantages of the Fabry-Pérot sensor are the speed with which planar scans can be performed (several orders of magnitude faster than a typical hydrophone scan) and the adjustable measurement range which enables the NEP to be minimised for measurements of both low and high pressures. To demonstrate these capabilities, measurements of the acoustic field were made at three different drive levels (peak-to-peak voltage): 33 V, 160 V, and 280 V. These correspond to pressures at the source of 43 kPa, 211 kPa, and 367 kPa respectively. An area of 9 mm by 9 mm was scanned with a step size of 50 μm (180×180 points) in single acquisition mode (no averaging). The acquisition time was approximately 3 minutes. The waveforms were high pass filtered at 0.35 MHz and corrected for the measured frequency response of the sensor. The waveforms were extracted from the centre of mass of the field distribution, and the temporal peak pressure values were extracted from the waveforms measured along a line passing through this point. Figure 5 shows focal waveforms, spectra, and temporal peak pressure profiles at the three transducer drive levels. The focal waveform becomes increasingly nonlinear as the transducer drive level is increased, with the amplitude of harmonics in the spectrum increasing. The peak positive pressure profile becomes increasingly narrow as the peak pressure increases, while the peak negative pressure profile broadens. The small effective element size of the system (65 μm) limits spatial averaging, which can cause underestimation of the spatial peak pressure in the narrow focal region.

D. Verification of focal pressure

In order to verify the acoustic pressures measured at high transducer drive levels, the field was simulated in water using the Khokhlov-Zabolotskaya-Kuznetsov (KZK) equation. Simulations were performed using the Texas KZK code [34, 35]. The temporal step size was $\Delta\tau = 0.0664$ ($\Delta t = 0.6$ ns, 1500 steps per cycle), the lateral spatial step size was $\Delta\rho = 0.003$ ($\Delta r = 97$ μm) and the axial spatial step size was $\Delta\sigma = 2 \times 10^{-4}$ ($\Delta z = 25$ μm).

The waveform used as the source boundary condition was obtained from near field hydrophone measurements using linear acoustic holography as described in [22]. Briefly, the transducer was driven as described in Sec. IV-A, with a peak to peak drive voltage of 7.3 V. The pressure was measured on a lateral plane in the near field of the transducer, then k-Wave was used to back project the pressure onto the transducer

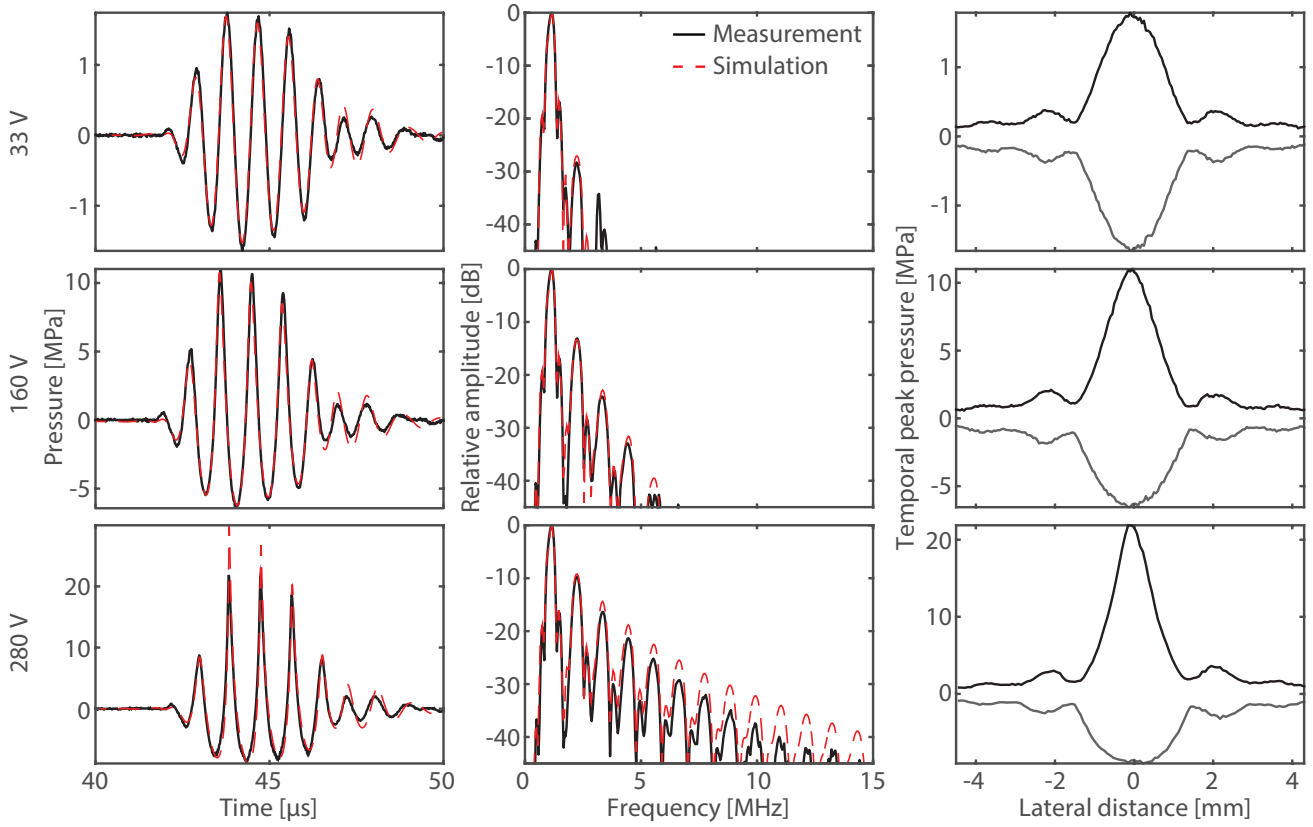


Fig. 5. Focal waveforms, spectra and transverse peak positive and peak negative pressure profiles are shown for three different transducer drive levels. Solid lines show measured waveforms and spectra, dashed lines show waveforms and spectra predicted from KZK simulations.

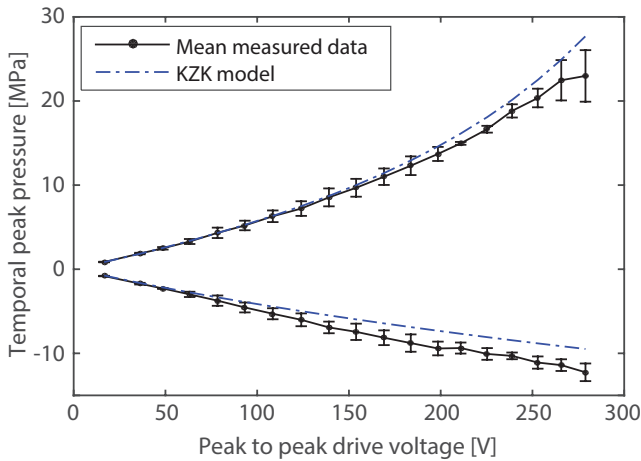


Fig. 6. Change in peak focal pressure with transducer drive level, it is assumed that the source pressure changes linearly with applied drive voltage. The solid line shows measured peak positive and negative focal pressures; error bars show 2 standard deviations of the mean of 3 or 6 repeated measurements. The dotted line shows the peak positive and negative focal pressures modelled using the KZK equation.

surface. The waveform at a point at the centre of the transducer was extracted.

The equivalent source method, used to set the boundary condition to the KZK equation on a plane to model ultrasound fields generated by strongly focused transducers [1, 6, 36], was followed. The effective source aperture, radius of curvature,

and source pressure that minimised the l_2 error between the simulated axial peak pressure and that measured using a 0.2 mm needle hydrophone were determined. The minimisation was performed using the axial peak positive pressure over a region centred on the focus of the field, including the last pre focal lobe, the focal lobe and the beginning of the post focal lobe. This resulted in an effective aperture diameter of 32.6 mm and a radius of curvature of 64.7 mm. Differences between the effective parameters of the boundary condition to the KZK model and the actual parameters of the focused transducer arise due to the parabolic approximation of the model and setting of the boundary condition in the initial plane rather than on the spherical surface [10, 36].

It was then assumed that the source pressure increased linearly with drive voltage. This was verified by simulating the field for 3 different drive levels/source pressure levels for which the field had been measured with a calibrated hydrophone. The field was then simulated for each source pressure for which the field was measured.

Measurements were made with the Fabry-Pérot scanning system over a 3 mm by 3 mm area covering the focal peak of the acoustic field at 19 drive levels (peak-to-peak voltage) between 16.6 V and 278 V, corresponding to source pressures of 22 kPa to 360 kPa. A step size of 50 μm was used and waveforms were acquired with 4 averages. Each scan was acquired in approximately 1.5 minutes. Measurements were repeated 6 times at lower drive levels (up to 200 V) and 3

times at higher drive levels.

The measured waveforms were high pass filtered and the frequency response of the sensor was applied. The spatial-peak temporal-peak positive and negative pressures were then extracted from the data. The means of both the measured and simulated peak focal pressures are plotted in Fig. 6. Error bars show 2 standard deviations of the mean measured value. There is good agreement between the measured and simulated data up to drive levels of approximately 200 V. Above this level, the simulated peak positive pressure increases more rapidly than the measured values, due to increased amplitude of harmonics in the simulation compared to the measurement, as can be observed in Fig. 5. These differences, which reach approximately 10% at the highest drive levels, could arise from several sources. Previously, good agreement was obtained between KZK simulations and measurements of a nominally identical transducer when the bandwidth of the hydrophone was applied to the simulated data [6]. Given the pressures measured here and the bandwidth of the device, the differences are not totally accounted for by the Fabry-Pérot sensor bandwidth. The effects of spatial averaging over the sensor element were also examined using the simulated data. The mean peak positive pressure was calculated over a $65 \mu\text{m}$ area (the effective element size) in the focal plane. At the highest drive level, there was a difference of less than 0.5% from the peak focal value, suggesting that the disagreement is not caused by spatial averaging. Another more probable reason for these differences could be the axial position of the sensor during measurements. The transducer-sensor distance was constant for measurements at all drive levels during a single repeat. The focus of these type of fields has been shown to move as the source pressure is increased, and due to the experimental set up, there is a possibility of small axial offsets between the sensor position and the focus. From the simulations, it was observed that for a change in axial position of 1 mm, there was a change in peak positive pressure of approximately 5%.

The smaller number of measurements at high drive levels was due to the occurrence of cavitation which disrupted beam profiles in some measurements at higher pressure. Following cavitation, there was some damage to the barrier coating on the sensor which rendered that area less sensitive, but not unusable. Subsequent measurements were performed using another region of the sensor. The possibility of eliminating the barrier coating will be investigated in future work.

E. Planar and volumetric mapping of HIFU fields

If a near field planar scan is required as an input for simulation of the acoustic field, an area of at least 1.3 times the beam diameter should be scanned with spatial sampling of less than $\lambda/2$ [23]. For the transducer used here, at a distance of 30 mm from the transducer origin, the beam diameter is 39 mm. The appropriately sized $51 \text{ mm} \times 51 \text{ mm}$ scan plane would require 85×85 points for a step size of 0.6 mm ($\lambda \approx 1.4 \text{ mm}$). For a hydrophone scan acquired at a rate of 1 Hz, it would take 2 hrs to acquire, while it would take only 35 seconds to acquire with the Fabry-Pérot scanning system. While 2 hours is not

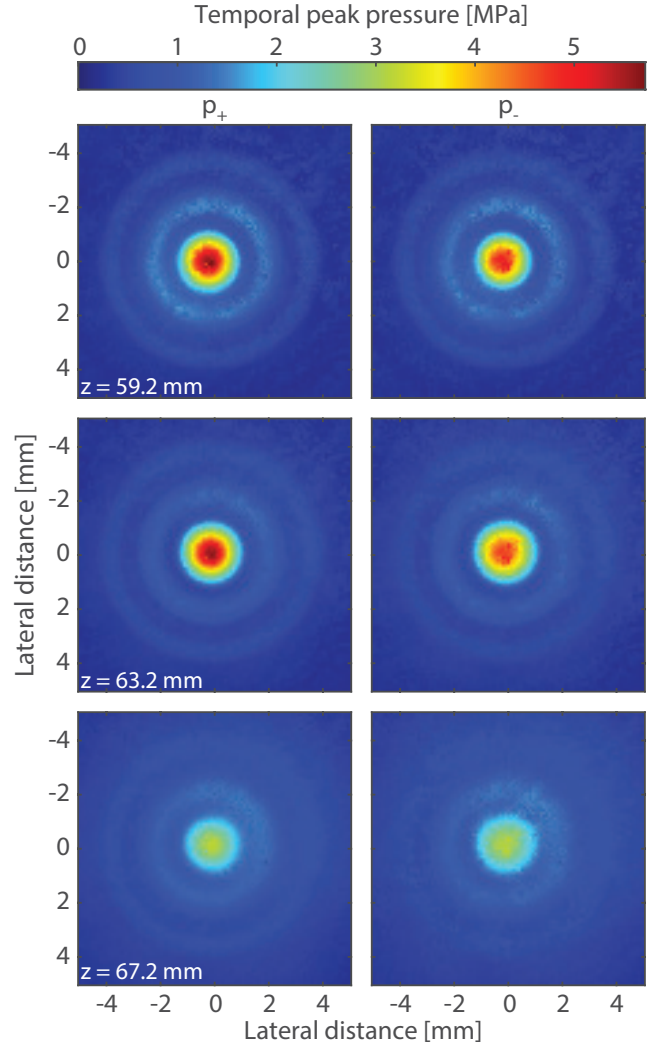


Fig. 7. 2D field maps of temporal peak positive (left) and temporal peak negative pressure (right) at XY planes positioned at distances of 59.2 mm, 63.2 mm (focal plane) and 67.2 mm from the origin of the transducer. Scan parameters: step size $100 \mu\text{m}$, scan area 10 mm by 10 mm, 4 averages, scan time 3 minutes.

an unreasonable scan time, if the transducer was driven at the 3rd harmonic, a step size of 0.2 mm would be appropriate, requiring a scan plane of 255×255 points. This would take approximately 18 hours to scan with a hydrophone, compared to approximately 5.5 minutes with the Fabry-Pérot system. With the short scan times achieved using this technique, it is also feasible to directly measure the acoustic field over a 3D volume.

To illustrate the use of the Fabry-Pérot scanning system as a tool for rapid mapping of ultrasound fields, field scans were performed at the focal plane and on planes 4 mm axial distance either side of this (59.2 mm, 63.2 mm, and 67.2 mm from the source). The transducer to sensor distance was adjusted using a manual translation stage. The transducer was driven with a peak-to-peak voltage of 94 V and an area of 10 mm by 10 mm was scanned with a step size of $100 \mu\text{m}$ (100×100 points) with 4 averages. The scan time was approximately 3 minutes per plane.

Plots of the peak positive and negative pressure on each plane are shown in Fig. 7. The spatial-peak temporal-peak positive pressure at the focal plane was 5.6 MPa while the spatial-peak temporal-peak negative pressure was 4.7 MPa. Side lobes are visible on each of the planes, and differences in their amplitude can be seen as the axial distance is varied. The smallest clearly visible side lobes have an amplitude of approximately 600 kPa. For speed, all three scans were performed with the same interrogation laser power. The NEP for this pressure range was 47 kPa (20 MHz bandwidth) or 80 kPa (125 MHz bandwidth). To maximise the signal to noise ratio, the laser power could also be adjusted from plane to plane or from point to point.

V. DISCUSSION AND CONCLUSIONS

A Fabry-Pérot sensor of all hard dielectric construction was developed and characterised in terms of its frequency response, directivity and NEP and used to make measurements of a nonlinear focused ultrasound field. The main characteristics of the system are reported in Table I, along with the characteristics of other devices applied to measurement of high amplitude focused ultrasound fields. Its suitability and limitations for application to measurement of high acoustic pressure, nonlinear focused ultrasound fields are discussed here.

The main advantage of the system is the acquisition speed. Waveforms were acquired from 200 scan points each second, this is very rapid compared to the usual rate of around 1 scan point per second for conventional hydrophone scans. The acquisition time for each of the 10 mm \times 10 mm scan planes shown in Fig. 7 was approximately 3 minutes, whereas the equivalent hydrophone scans would take almost 3 hours each.

Another advantage of the sensor is the small element size of 65 μm , the smallest of the sensors listed in Table I. While this is an advantage in reducing spatial averaging in the increasingly narrow focal regions of high amplitude fields, it has been shown that greater error in measured focal pressure can arise if the sensor bandwidth is limited [6]. For this sensor, the on axis amplitude frequency response was constant to within 3 dB up to 62 MHz and to within less than 6 dB up to 80 MHz, which was the limit of the frequency content of the acoustic field used to measure the frequency response. The bandwidth is greater than the protected needle and membrane hydrophones (although their effective bandwidth was increased by deconvolution of the complex frequency response) and theoretically, the frequency response is expected to be constant to frequencies of over 100 MHz. This would make the bandwidth comparable with a conventional membrane hydrophone or FOPH and suitable for measurement nonlinear fields containing many harmonics.

The NEP of the system scaled with the pressure measurement range, by adjustment of the interrogating laser power. At the low end of the measurement range (up to 8 MPa) the NEP was 26 kPa over a 20 MHz bandwidth and 49 kPa over the full 125 MHz bandwidth. This compares well with a PVDF needle hydrophone of a similar element size (75 μm) for which the NEP has been quoted as 50 kPa (20 MHz bandwidth) [14].

The NEP for the highest pressures measured in this work was 152 kPa, which is higher than both the conventional and the protected membrane hydrophone but considerably lower than the NEP on the Eisenmenger type FOPH.

In this work, spatial mapping of a focused ultrasound field was achieved with maximum peak positive and negative focal pressures of 25 MPa and -12 MPa, respectively. While lower than the 75 MPa peak positive pressure and 15 MPa peak negative pressure measured using the protected membrane hydrophones [3] and the 100+ MPa peak positive and 18 MPa peak negative pressures measure using the Eisenmenger type FOPH [2], these pressure levels are comparable to the highest reported pressures measured with a conventional membrane hydrophone and protected needle hydrophone. For these three devices, the pressure levels were limited by the onset of cavitation which disrupted the measurements. The PVDF hydrophones suffered damaged to their electrodes which prevented further use. The Fabry-Pérot sensor suffered some damage to the barrier coating rather than the interferometer itself. This damage then made cavitation more likely, probably due to increased surface roughness. The possibility of manufacturing sensors without the barrier coating will be investigated in future work. In most cases exposure of expensive PDVF hydrophones to high pressures would be avoided because of the risk of damage. However, replacement of the Fabry-Pérot sensor head is simple and much less costly so could provide an alternative method of measuring pressure at these levels without risk of damage to expensive equipment.

There are several features of the sensor and the experimental set up for this system that increase the likelihood of cavitation. Reflection of the acoustic field at the large water-sensor interface causes an approximate doubling of the acoustic pressure at the sensor. Because of this, the maximum pressure that can be measured before cavitation occurs will be approximately half of the intrinsic cavitation threshold of deionised water, which is on the order of 24 to 28 MPa at room temperature [37]. During measurements, cavitation always occurred when the peak negative pressure exceeded a level of approximately 13 MPa. In practice, cavitation was also likely below this threshold because of reoxygenation and contamination of the relatively small volume of water in the tank. The sensor also has a large surface area, creating more locations for cavitation nuclei, and it was mounted in the base of the tank so impurities could settle onto the surface and act as cavitation nuclei. These factors are not an issue when, for example, a small fibre-optic hydrophone is used in a large water tank, or with a hydrophone specifically designed to suppress cavitation at the sensitive element.

Comparison with hydrophone measurements at low drive levels showed some discrepancies due to the directional response of the Fabry-Pérot sensor. There was good agreement in the focal lobe of the field, but a higher pressure amplitude was measured in the side lobes. The differences were significantly reduced by deconvolution of the directional response from the measured data. However, application of the deconvolution to the measured data is complicated in practice, due to the low sensitivity at some angles of incidence, and will be the subject of further work. Uncertainties in the measurement of the direc-

Device type	Element diameter [μm]	-6 dB bandwidth [MHz]	Highest reported pressure		NEP (type, bandwidth) [kPa]	Reference
			p_+ [MPa]	p_- [MPa]		
Planar hard dielectric Fabry-Pérot sensor	65	80+	25	12	49 - 152 (3σ , 125 MHz)	
Protected needle hydrophone	400	10	25	9	130 (σ , 20 MHz)	[7], [8]
Conventional membrane hydrophone	200	100	27	10	13 (σ^2 , 500 MHz)	[3]
Protected membrane hydrophone	200	40+	75	15	65 (σ^2 , 500 MHz)	[3]
Eisenmenger type fibre-optic hydrophone	100	100	100 +	18	2000 - 3000 (100 MHz)	[2]

TABLE I

CHARACTERISTICS OF HYDROPHONES APPLIED TO MEASUREMENT OF FOCUSED ULTRASOUND FIELDS

tional response, which could arise from misalignments during its measurement, will propagate through the deconvolution. This is an extra source of uncertainty that is minimal for conventional hydrophones with small element sizes. Another source of uncertainty was the low amplitude of the laser generated ultrasound field used for measurement of on axis frequency response. This could be improved by optimisation of the laser generated ultrasound source to increase its amplitude, or by adapting the mounting of the sensor so a more traditional hydrophone calibration method could be used. At higher drive levels, measurements of focal pressure were compared to KZK simulations. There was good agreement for drive levels of up to about 200 V ($p_0 = 260$ kPa), but above this level the measured peak positive pressure was lower than the simulated value. It seems likely that this was caused at least partly by misalignment of the sensor on the beam axis.

In this work, the transducer was driven with a short pulse, rather than a longer tone burst reaching steady state conditions which would be more representative of a clinical HIFU driving regime. The reason for this was the limited measurement time before interference from reflections from the back of the sensor substrate. In future iterations of the sensor design, the interferometer will be deposited onto a thicker substrate to allow time for measurement of longer toneburst signals.

The measured pressures did not exceed the linear measurement range of the sensor, which was 35 MPa to within 5% and 56 MPa to within 10%. To enable measurement of higher pressures, provided cavitation could be avoided, this could be increased by reducing the finesse of the interferometer by decreasing the reflectivity of the mirrors or reducing the spacer thickness.

In conclusion, the rapid scanning time, small element size, reasonably low NEP, and flat and broad frequency response of the sensor are advantages in the measurement of nonlinear focused ultrasound fields. However, there are currently some limitations in terms of the maximum pressure amplitude and onset of cavitation, and the linear range and free measurement time of the sensor. Overcoming these limitations to extend the measurements to clinical HIFU fields will be investigated as part of future work.

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