# Artificial Gravity and Abort Scenarios via Tethers for Human Missions to Mars 

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#### Abstract

Minimum-mass tether designs are developed for a spinning human transport that not only provides artificial gravity, but also the potential for free-return aborts. The investigation reveals that severing the tether can provide a propellant-free boost to return astronauts to Earth in the event of an aborted landing on Mars. Earth-Mars-Earth, Earth-Mars-Venus-Earth, and Earth-Venus-Mars-Earth trajectories requiring little, or no, velocity change after departure from Earth, are examined. The investigation covers trajectories with launch opportunities between 2014 and 2030 , launch hyperbolic excess speeds of up to $4.5 \mathrm{~km} / \mathrm{s}$ and total flight times of less than 1000 days. We identify propellant-free abort scenarios in every Earth-Mars synodic period ( $\mathbf{2} .14$ years) with mission configurations that closely match NASA's design reference mission.


|  | Nomenclature |
| :---: | :---: |
| $A_{x, C}$ | $=$ tether cross-sectional area at location $x$ between the center of mass and the countermass, $\mathrm{m}^{2}$ |
| $A_{x, H}$ | $=$ tether cross-sectional area at location $x$ between the center of mass and the habitat module, $\mathrm{m}^{2}$ |
| $a_{\text {max }}$ | $=$ maximum acceleration, $\mathrm{m} / \mathrm{s}^{2}$ |
| $m_{C}$ | $=$ countermass, kg |
| $m_{H}$ | $=$ habitat module mass, kg |
| $m_{P}$ | $=$ propellant mass, kg |
| $m_{T}$ | $=$ tether mass, kg |
| $V_{C}$ | $=$ countermass velocity relative to the system center of mass, m/s |
| $V_{\text {char }}$ | $=$ material characteristic velocity, m/s |
| $V_{H}$ | $=$ habitat velocity relative to the system center of mass, $\mathrm{m} / \mathrm{s}$ |
| $V_{\infty}$ | $=$ hyperbolic excess speed, m/s |
| $V^{*}$ | $=$ nondimensional velocity |
| $x$ | $=$ distance along the tether from the center of mass, m |
| $\Delta V$ | $=$ change in velocity, $\mathrm{m} / \mathrm{s}$ |
|  | $=$ tether material density, $\mathrm{kg} / \mathrm{m}^{3}$ |
|  | $=$ tether material tensile strength, Pa |

## Introduction

0NE possible configuration of the tether transport facility is depicted in Fig. 1. The transport facility spins, so that the astronauts in the habitat module experience an acceleration similar to the gravitational acceleration they normally experience on Earth. The momentum of the rotating tether system might be used to provide a propellant-free boost for returning the astronauts to Earth after an aborted Mars landing.

Space-based tethered transportation systems can eliminate or reduce the need for expendable propellant. ${ }^{1-9}$ Cosmo and Lorenzini ${ }^{4}$ present an excellent overview of potential tether applications. For

[^0]space-based systems, tapered tether designs minimize the mass and the structural loads ${ }^{1-5,9}$ Puig-Suari et al. ${ }^{3}$ discuss the importance of minimization of the mass for a tether sling transportation system. Jokic and Longuski ${ }^{9}$ extend this work by designing tether slings stationed on Phobos for human transportation systems between Earth and Mars.

Possible scenarios for human missions to Mars are widely discussed in the literature. ${ }^{10-35}$ The work by Lyne and Townsend ${ }^{25}$ details a powered swingby scenario to return astronauts safely to Earth in the event of an aborted Mars landing. Okutsu and Longuski ${ }^{35}$ present an investigation of possible free-return trajectories (requiring no propellant expenditure after launch). Their work identifies a potential Earth-Mars-Venus-Earth (E-M-V-E) trajectory with desirable mission parameters in 2014.

In this paper, we develop minimum-mass designs for the tether in a human transport with artificial gravity. We outline a general methodology for the design of a minimum-mass tethered system in a configuration consisting of two end masses connected by a tether, as shown in Fig. 1. We then discuss trajectories with abort capabilities for human missions to Mars. Our analysis identifies some potential trajectories that can use the momentum of the spinning tethered transport to provide the necessary boost to transfer astronauts back to Earth without expending propellant.

## Abort Scenarios for Human Missions to Mars

Our investigation aims to identify abort options for human missions to Mars for a worst-case scenario. Ideally, a mission to Mars will be configured to enable the astronauts to return to Earth without requiring an engine to provide a velocity change. Unfortunately, free-return trajectories do not conform to the needs of human missions for all potential launch years. We examine how a spinning tether transportation system might be able to provide the necessary velocity change to return astronauts to Earth. One role of the tethered system is to generate an artificial gravity environment. By spinning the tethered transport, the astronauts in the habitat module experience a centripetal acceleration equal in magnitude to the gravitational acceleration people would normally experience on Earth. Figure 2 shows how a spinning tethered transport system can provide the velocity change required for an Earth-Mars-Earth (E-M-E) abort trajectory. The tether connecting the habitat and countermass modules is severed near apoapsis, so that the habitat has the velocity needed to return the astronauts to Earth. The specific abort scenario depicted in Fig. 2 is one of the solutions we examine in this paper.

We refer to NASA's design reference mission (DRM) to define elements of the tethered transport's mass. Some of the masses

Table 1 System masses for human missions to Mars ${ }^{24}$

| System | Mass, kg |
| :--- | :---: |
| Crew-lander-entry mass | 60,806 |
| Crew-lander NTR system | 26,600 |
| Crew-lander TMI propellant | 50,000 |
| Cargo-lander-entry mass | 66,043 |
| Cargo-lander NTR system | 23,400 |
| Cargo-lander TMI propellant | 45,300 |

Fig. 1 Possible configuration of space transport with artificial gravity.


Fig. 2 Aborted mission to Mars with a $\Delta V$ achieved by severing the tether.
specified in the DRM are shown in Table 1. In our analysis, the crew-lander-entry mass is the habitat module. We assume that the tethered transport's countermass is the crew-lander, nuclear thermal rocket (NTR) system. One possible alternative tethered transport design might consist of the crew-lander-entry mass tethered to the cargo-lander-entry mass. The emphasis of our examination is on propellant-free abort options that represent worst-case scenarios where the engines on the descent stage fail. If the systems associated with the decent engines do not fail, the masses specified in the DRM suggest that a velocity change of $0.77 \mathrm{~km} / \mathrm{s}$ is possible. The E-M-E abort trajectory depicted in Fig. 2 requires a $0.5-\mathrm{km} / \mathrm{s}$ velocity change near apoapsis to return the habitat module to Earth. Our tether transport design does not require the descent engines to return the habitat module to Earth, but the engines are also capable of producing a $0.5-\mathrm{km} / \mathrm{s}$ boost.

## Minimum Tether Mass Designs for Artificial Gravity <br> Design Methodology

Our design methodology for the minimum-mass configuration of the tethered transport begins with a specified value for the speed of
the habitat module, relative to the system's center of mass $V_{H}$. The characteristic velocity of a tether material is defined as ${ }^{3}$

$$
\begin{equation*}
V_{\text {char }}=\sqrt{2 \sigma} / \rho \tag{1}
\end{equation*}
$$

which represents the maximum tip speed that a uniform (nontapered) tether can support before failure. When the tether is tapered, there is no theoretical maximum tip speed (within practical limits). We define the nondimensional velocity of the habitat module as

$$
\begin{equation*}
V_{H}^{*}=V_{H} / V_{\text {char }} \tag{2}
\end{equation*}
$$

The length of the tether from the transport's center of mass to the habitat module is determined by constraint of the acceleration and specification of $V_{H}$ :

$$
\begin{equation*}
L_{H}=V_{H}^{2} / a_{\max } \tag{3}
\end{equation*}
$$

where $a_{\text {max }}$ is the maximum acceleration experienced by astronauts in the habitat. For the case where the countermass is equal to the habitat mass, the total length of the tether is simply twice the length $L_{H}$. In general, however, the end masses are not equal, and the length $L_{C}$ is dependent on $L_{H}, V_{H}$, and $m_{C}$. To determine $L_{C}$, we apply the definition of the center of mass for collinear mass elements, with the center of mass defined at the origin

$$
\begin{align*}
& m_{H} L_{H}+\int_{0}^{L_{H}} \rho A_{x, H} x \mathrm{~d} x-m_{C} L_{C} \\
& \quad-\int_{0}^{L_{C}} \rho A_{x, C} x \mathrm{~d} x=\sum_{i=1}^{n} x_{i} m_{i}=0 \tag{4}
\end{align*}
$$

The minimum cross-sectional areas of the tether needed at a distance $x$ from the system center of mass along the lengths $L_{C}$ and $L_{H}$ are found from ${ }^{3}$

$$
\begin{align*}
A_{x, C} & =A_{L, C} \exp \left[\left(\rho V_{C}^{2} / 2 \sigma\right)\left(1-x^{2} L_{C}^{-2}\right)\right]  \tag{5}\\
A_{x, H} & =A_{L, H} \exp \left[\left(\rho V_{H}^{2} / 2 \sigma\right)\left(1-x^{2} L_{H}^{-2}\right)\right] \tag{6}
\end{align*}
$$

respectively. The cross-sectional areas at the attachment points of the habitat module and countermass are

$$
\begin{align*}
& A_{L, C}=m_{C}\left(V_{C}^{2} / \sigma L_{C}\right)  \tag{7}\\
& A_{L, H}=m_{H}\left(V_{H}^{2} / \sigma L_{H}\right) \tag{8}
\end{align*}
$$

Our minimum-mass tether design is tapered from a maximum cross-sectional area at the center of mass to minimum crosssectional areas at the ends. By evaluation of the integrals and performance of the necessary algebra, Eq. (4) becomes

$$
\begin{equation*}
m_{H} L_{H} \exp \left(V_{H}^{* 2}\right)=m_{C} L_{C} \exp \left(V_{H}^{* 2} L_{C}^{2} / L_{H}^{2}\right) \tag{9}
\end{equation*}
$$

Rearranging for $L_{C}$ produces

$$
\begin{equation*}
L_{C}=m_{H} L_{H} / m_{C} \exp \left\{V_{H}^{* 2}-1 / 2 W\left[2 V_{H}^{* 2} m_{H}^{2} \exp \left(V_{H}^{* 2}\right) / m_{C}^{2}\right]\right\} \tag{10}
\end{equation*}
$$

where $W(z)$ is the Lambert $W$ function ${ }^{36}$ defined as the solution of

$$
\begin{equation*}
z=W(z) e^{W(z)} \tag{11}
\end{equation*}
$$

With $L_{C}$ determined, the velocity of the countermass relative to the transport's center of mass is calculated by

$$
\begin{equation*}
V_{C}=\left(V_{H} / L_{H}\right) L_{C} \tag{12}
\end{equation*}
$$

and the nondimensional velocity of the countermass is determined from

$$
\begin{equation*}
V_{C}^{*}=V_{C} / V_{\text {char }} \tag{13}
\end{equation*}
$$

The masses associated with the tether lengths $L_{H}$ and $L_{C}$ are defined in terms of the nondimensional velocities and the error function $\mathrm{as}^{3}$

$$
\begin{align*}
m_{T, H} & =m_{H} \sqrt{\pi} V_{H}^{*} \exp \left(V_{H}^{* 2}\right) \operatorname{erf}\left(V_{H}^{*}\right)  \tag{14}\\
m_{T, C} & =m_{C} \sqrt{\pi} V_{C}^{*} \exp \left(V_{C}^{* 2}\right) \operatorname{erf}\left(V_{C}^{*}\right) \tag{15}
\end{align*}
$$

respectively. Hence, the total minimum mass of the tether is found by the addition of the mass of the two sections

$$
\begin{equation*}
m_{T}=m_{T, H}+m_{T, C} \tag{16}
\end{equation*}
$$

Substitution of Eq. (10) into Eq. (12) reveals that $V_{C}$ depends on $V_{H}^{*}, m_{C}$, and $m_{H}$. Therefore, we note from Eqs. (14) and (15) that the tether mass does not depend on the length of the tether, but only on the end masses, tip velocity, and characteristic velocity. Equation (3) indicates that (for a given tip velocity) the length is determined by the maximum acceleration we select for the habitat module.

## Mass Performance

We now examine how the countermass-to-habitat-mass ratio and the relative velocity of the habitat $V_{H}$ affect the mass of the tether. The material selected for the analysis is Zylon, which has a tensile strength of 5.8 GPa and a density of $1560 \mathrm{~kg} / \mathrm{m}^{3}$. Substitution of these properties into Eq. (1) reveals that the characteristic speed of Zylon is $2.7 \mathrm{~km} / \mathrm{s}$. One of our metrics for selecting suitable transport designs is the ratio of the tether-mass-to-propellant-mass $\left(m_{T} / m_{P}\right)$ needed for the deep space maneuver (DSM). We determine the (hypothetical) propellant mass to produce the required change in the habitat module's velocity (DSM) using a single-stage rocket model with an $I_{\text {sp }}$ of 379 s .

Figure 3 shows $m_{T} / m_{P}$ for a range of habitat throw velocities and ratios of counter-mass-to-habitat-mass $\left(m_{C} / m_{H}\right)$. The mass of the tether is highly dependent on the desired habitat throw velocity, and so $m_{T} / m_{P}$ increases very quickly with increasing throw velocity. As expected, higher values of $m_{C} / m_{H}$ for a particular habitat throw velocity produce smaller tether masses and, subsequently, smaller $m_{T} / m_{P}$. Ideally, $m_{T} / m_{P}$ should be less than unity, so that the mass of the tether is less than the propellant required to complete a particular abort trajectory. For an $m_{C} / m_{H}$ value of 0.5 , this condition requires that the habitat throw velocity must be less than about $0.36 \mathrm{~km} / \mathrm{s}$. An $m_{C} / m_{H}$ of 0.3 requires a change in velocity of less than $0.26 \mathrm{~km} / \mathrm{s}$ to keep the $m_{T} / m_{P}$ ratio less than one. If the mass available for the tether transport is assumed to match the Mars DRM, $m_{C} / m_{H}$ is about 0.44 . A value of $m_{T} / m_{P}$ greater than one is not necessarily a reason to dismiss a design because the system has the added benefit of generating artificial gravity and reducing the entry velocity of the habitat for aerobraking. The habitat module's entry velocity is reduced when the tether is severed, so that the module is released in the opposite direction to the transport's flight path. A lower entry velocity decreases the mass


Fig. 3 Tether-mass-to-propellant-mass ratio vs required habitat velocity.
required for heat shielding. In our analysis, we consider designs with $m_{T} / m_{P}$ values of up to three as advantageous to human Mars missions.

The ratio of the tether-mass-to-habitat-mass $\left(m_{T} / m_{H}\right)$ is also investigated as a function of the habitat throw velocity and $m_{C} / m_{H}$. Figure 4 contains curves that show the dependence of $m_{T} / m_{H}$ on the required habitat throw velocity. For $m_{C} / m_{H}$ values of 0.5 and 0.3 , the tether mass remains less than one half of the habitat mass ( $m_{T} / m_{H}<0.5$ ) for habitat throw velocities less than 0.82 and 0.75 $\mathrm{km} / \mathrm{s}$, respectively. The performance of the tethered transport, in terms of mass, is highly dependent on the required habitat throw velocity $V_{H}$, the strength-to-weight ratio of the tether material, and the ratio of the end masses $m_{C} / m_{H}$.

## Abort Options via Tethers

We seek trajectories in which a small $\Delta V$ can return astronauts to Earth in an acceptable time of flight. If the $\Delta V$ is small enough, then our tether design can achieve the maneuver with minimal mass. The spinning tether system has the added benefit of generating an artificial gravity environment. We only allow the $\Delta V$ to occur after the tether transport reaches Mars. The restriction of the time of the DSM in this way is consistent with a worst-case scenario in which the decision to abort is made near Mars. For our analysis, we design the tether transport so that the acceleration experienced by the astronauts in the habitat is equal to the acceleration on the surface of the Earth ( $1 g$ ).

Table 2 (Refs. 22, 35, and 37) contains some of our constraints for identifying acceptable abort options. We use the conditions to examine E-M-E, E-M-V-E and Earth-Venus-Mars-Earth (E-V-$\mathrm{M}-\mathrm{E}$ ) trajectory paths between 2014 and 2030. The constraints listed are in decreasing order of priority. The $V_{\infty}$ and the times of flight are presented in the literature as practical design limits for Mars missions. Because the tether serves a dual purpose (of providing artificial gravity and an abort option) we select $m_{T} / m_{P} \leq 3$ as a useful design criterion. Short times of flight minimize the exposure of astronauts to high-energy galactic cosmic radiation and solar particle events that can have a significant detrimental effect on the health of the astronauts. ${ }^{23,25,35}$

Table 2 Human mission constraints listed in order of decreasing priority

| Mission variable | Constraint |
| :--- | ---: |
| Launch $V_{\infty}{ }^{\text {a }}$ | $\leq 4.5 \mathrm{~km} / \mathrm{s}$ (Ref. 22) |
| Mars arrival $V_{\infty}$ | $\leq 7.1 \mathrm{~km} / \mathrm{s}$ (Ref. 37) |
| Earth arrival $V_{\infty}$ | $\leq 9.3 \mathrm{~km} / \mathrm{s}$ (Ref. 37) |
| $m_{T} / m_{P}$ | $\leq 3$ |
| TOF, E-M | $\leq 180$ days (Ref. 35) |
| Total TOF | $\leq 800$ days (Ref. 35) |

${ }^{\text {a }}$ DRM in 2014 requires $3.32 \mathrm{~km} / \mathrm{s}$ (Ref. 35). Value based on requirement for the 2024 180-day transfer and DRM vehicle masses.


Fig. 4 Tether-mass-to-habitat-mass ratio vs required habitat velocity.

Table 3 E-M-E abort options with a DSM

| Launch date, <br> yyyy/mm/dd | Launch <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Mars arrival <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Earth arrival <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ |  | TOF to <br> DSM, km/s | TOF to <br> DSM, days <br> Mars, ${ }^{\text {a }}$ days | TOF to <br> Earth, ${ }^{\text {b }}$ days |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2014 / 01 / 07$ | 3.79 | 8.30 | 4.68 | 1.25 | 451 | 158 | 770 |
| $2016 / 02 / 27$ | 3.59 | 8.13 | 4.77 | 1.12 | 496 | 140 | 780 |
| $2018 / 05 / 10^{\text {c }}$ | 3.90 | 7.09 | 5.06 | 0.71 | 491 | 187 | 759 |
| $2020 / 07 / 27^{\text {c }}$ | 4.50 | 5.59 | 5.01 | 0.50 | 418 | 134 | 742 |
| $2022 / 09 / 12^{\text {c }}$ | 4.52 | 4.94 | 4.90 | 1.01 | 443 | 171 | 753 |
| $2024 / 10 / 17^{\text {c }}$ | 4.56 | 6.07 | 4.86 | 1.12 | 448 | 180 | 753 |
| $2026 / 11 / 21$ | 4.51 | 7.83 | 4.85 | 0.91 | 443 | 172 | 747 |
| $2028 / 12 / 23$ | 3.97 | 8.22 | 4.69 | 1.22 | 433 | 147 | 765 |

${ }^{\text {a }}$ TOF to Mars is the TOF for E-M. ${ }^{\mathrm{b}}$ TOF to Earth is the TOF for E-M-E. ${ }^{\mathrm{c}}$ Option conforms to all mission constraints.

Table 4 Tether designs for E-M-E abort options

| Launch date, <br> yyyy/mm/dd | $\mathrm{DSM}, \mathrm{km} / \mathrm{s}$ | $m_{C} / m_{H}$ | Tether mass <br> $\left(m_{T}\right), \mathrm{Mg}$ | Tether length <br> $\left(L_{C}+L_{H}\right), \mathrm{km}$ | $m_{T} / m_{H}$ | $m_{T} / m_{P}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | ---: |
| $2014 / 01 / 07$ | 1.25 | 0.44 | 72.3 | 417 | 1.2 | 3.0 |
| $2016 / 02 / 27$ | 1.12 | 0.44 | 57.8 | 341 | 0.95 | 2.7 |
| $2018 / 05 / 10^{\mathrm{a}}$ | 0.71 | 0.44 | 24.2 | 150 | 0.40 | 1.9 |
| $2020 / 07 / 27^{\mathrm{a}}$ | 0.50 | 0.44 | 12.5 | 77.8 | 0.21 | 1.4 |
| $2022 / 09 / 12^{\mathrm{a}}$ | 1.01 | 0.44 | 47.4 | 284 | 0.78 | 2.5 |
| $2024 / 10 / 17^{\mathrm{a}}$ | 1.12 | 0.44 | 58.1 | 343 | 0.96 | 2.7 |
| $2026 / 11 / 21$ | 0.91 | 0.44 | 38.8 | 236 | 0.64 | 2.3 |
| $2028 / 12 / 23$ | 1.22 | 0.44 | 69.1 | 400 | 1.1 | 2.9 |

${ }^{\text {a }}$ Option conforms to all mission constraints.

## E-M-E Trajectories

Patel et al. ${ }^{27}$ examine potential E-M-E free-return trajectories in some detail. Our investigation, however, allows for a small $\Delta V$ in the trajectory to ensure that the conditions of Table 2 are met. Table 3 contains the E-M-E options obtained for launch years between 2014 and 2028 , where we find the minimum total $\Delta V$ from the trajectory optimization program MIDAS. ${ }^{38}$ By restricting the mission times of flight, we are able to manipulate the MIDAS output to conform to our constraints (in some cases). There are no free-return solutions for the conditions of Table 2. We note that 2018, 2020, 2022, and 2024 contain launch opportunities that closely match the mission constraints. In all of these cases, the required DSMs can be achieved by severing the tether. Figure 2 shows the 2020 abort scenario. As we noted earlier, the $0.5-$ and $0.71-\mathrm{km} / \mathrm{s}$ DSMs can be achieved when the propellant stored on the transport for descent to the surface of Mars is expended. In all of the cases presented, the time of flight (TOF) to return to Earth is less than the imposed 800-day limit.

Table 4 shows the tether designs needed to achieve the DSMs of the E-M-E abort trajectories. The mass ratio $m_{T} / m_{P}$ for the 2018 and 2020 cases are 1.9 and 1.4 , respectively. Only the opportunities identified in 2018 and 2020 have a tether mass that is less than half the habitat mass $\left(m_{T} / m_{H}<0.5\right)$. Our 2018 and 2020 solutions require tether lengths of 150 and 77.8 km . If the maximum acceleration in Eq. (1) is set to equal the acceleration on the surface of Mars $(0.38 g)$ these lengths increase to 394 and 205 km . The tether lengths in both cases are similar to other tether transfer systems. ${ }^{3,6,8}$ For a specified tip velocity, the mass ratios are not affected by a change in the assumed maximum acceleration. We also identified opportunities in 2016, 2026, and 2028, which meet our mass ratio limit for the tether, but the arrival velocities at Mars are larger than the established $7.1-\mathrm{km} / \mathrm{s}$ constraint.

## E-M-V-E Trajectories

We searched for possible $\mathrm{E}-\mathrm{M}-\mathrm{V}-\mathrm{E}$ abort trajectories using STOUR, ${ }^{39}$ a patched-conic propagator. Figure 5 presents the trajectories found between 2014 and 2031 with a launch $V_{\infty}$ equal to $4.5 \mathrm{~km} / \mathrm{s}$, a maximum DSM between Mars and Venus of $0.8 \mathrm{~km} / \mathrm{s}$, and a minimum flyby altitude of 200 km . We searched for viable trajectories, which require a launch $V_{\infty}$ between 3.4 and $4.6 \mathrm{~km} / \mathrm{s}$, using an increment of $0.1 \mathrm{~km} / \mathrm{s}$. The cases with a launch $V_{\infty}$ of


Fig. 5 E-M-V-E trajectories (2014-2031) with maximum TOF $\leq 1000$ days.
$4.5 \mathrm{~km} / \mathrm{s}$ are represented in Fig. 5 because this is the upper limit determined for the DRM configuration and to ensure clarity. Despite the large number of solutions available in 2014, an allowance for small $\Delta V$ does not result in opportunities in all launch years. Our search does not reveal any potential trajectories in 2022. A large number of trajectories requiring little, or no, $\Delta V$ are shown in Fig. 6. All of the trajectories shown in Fig. 6 meet our design requirements, including the $V_{\infty}$ at Earth and Mars. We selected our final solutions from the STOUR output by displaying the data in graphs such as those in Figs. 5 and 6.

Table 5 contains our best options for $\mathrm{E}-\mathrm{M}-\mathrm{V}-\mathrm{E}$ abort trajectories between 2014 and 2031. We found opportunities in 2014 and 2020, that meet our design constraints. The 2014 abort option is a freereturn scenario, which is in agreement with the solution found by Okutsu and Longuski. ${ }^{35}$ Whereas the remaining trajectories listed in Table 5 violate the design constraints, the opportunity identified in 2024 only significantly exceeds the limits in the total time of flight ( 881 days). Table 6 lists the tether transport designs corresponding to the reported $\mathrm{E}-\mathrm{M}-\mathrm{V}-\mathrm{E}$ abort trajectories. There are no design requirements based on the 2014 trajectory because it represents a

Table 5 E-M-V-E abort options with a DSM

| Launch date, <br> yyyy/mm/dd | Launch <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Mars arrival <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Earth arrival <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | DSM, km/s | TOF to <br> Mars, ${ }^{\text {a }}$ days | TOF to <br> Earth,b days |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $2014 / 01 / 13^{\mathrm{c}}$ | 3.6 | 6.98 | 4.81 | 0.00 | 170 | 800 |
| $2016 / 06 / 14$ | 4.5 | 6.11 | 6.84 | 0.80 | 370 | 935 |
| $2018 / 06 / 13$ | 4.5 | 4.75 | 5.04 | 0.15 | 262 | 925 |
| $2020 / 06 / 24^{\text {c }}$ | 4.5 | 4.43 | 5.86 | 0.76 | 168 | 800 |
| $2024 / 10 / 16$ | 4.5 | 5.91 | 7.52 | 0.38 | 184 | 881 |
| $2026 / 10 / 07$ | 4.3 | 4.35 | 8.63 | 0.79 | 263 | 835 |
| $2029 / 04 / 23$ | 4.5 | 8.27 | 5.52 | 1.22 | 388 | 941 |
| $2031 / 03 / 01$ | 4.5 | 7.07 | 5.32 | 0.48 | 380 | 912 |

${ }^{\text {a }}$ TOF to Mars is the TOF for E-M. ${ }^{\text {b }}$ TOF to Earth is the TOF for E-M-E. ${ }^{\mathrm{c}}$ Option conforms to all mission constraints.

Table 6 Tether designs for E-M-V-E abort options

| Launch date, <br> yyyy/mm/dd | $\mathrm{DSM}, \mathrm{km} / \mathrm{s}$ | $m_{C} / m_{H}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | | Tether mass |
| :---: |
| $\left(m_{T}\right), \mathrm{Mg}$ |$\quad$| Tether length |
| :---: |
| $\left(L_{C}+L_{H}\right), \mathrm{km}$ |$m_{T} / m_{H}$| $m_{T} / m_{P}$ |
| :--- |
| $2014 / 01 / 13^{\mathrm{a}}$ |
| $2016 / 06 / 14$ |

${ }^{\text {a }}$ Option conforms to all mission constraints.
${ }^{\mathrm{b}}$ There are no geometric requirements for the tether when the DSM is zero.


Fig. 62014 E-M-V-E trajectory opportunities with TOF < 810 days.
free-return option. The 2020 trajectory requires a $\Delta V$ of $0.76 \mathrm{~km} / \mathrm{s}$, which corresponds to a tether with a length of 170 km and a mass ratio $m_{T} / m_{P}$ of 2 .

## E-V-M-E Trajectories

Our search of E-V-M-E trajectories between 2014 and 2031 uncovered numerous launch opportunities. Figure 7 shows potential trajectories with a launch $V_{\infty}$ equal to $4.5 \mathrm{~km} / \mathrm{s}$, a minimum flyby altitude of 200 km , and a maximum DSM between Mars and Earth of $0.9 \mathrm{~km} / \mathrm{s}$. As with the E-M-V-E cases, we searched for trajectories with launch $V_{\infty}$ between 3.4 and $4.6 \mathrm{~km} / \mathrm{s}$ using an increment of $0.1 \mathrm{~km} / \mathrm{s}$. We see in Fig. 7 that trajectories exist with a TOF less than 800 days in 2015, 2016, 2017, 2021, and 2023. A more detailed representation of the 2021 family of trajectories is shown in Fig. 8. A number of trajectories exist in 2021, that require little, or no, $\Delta V$. Unfortunately, the TOF to Mars for these trajectories exceeds the 180-day limit. Because of the flyby of Venus occurring before arrival at Mars, the E-V-M-E trajectory option always has a longer TOF to Mars than the 180 -day constraint. Unlike the E-M-V-E trajectory option, the flyby of Venus is a compulsory element of


Fig. $7 \quad$ E-V-M-E trajectories (2014-2031) with maximum TOF $\leq 1000$ days.


Fig. 8 E-V-M-E trajectory options for 2021 with TOF < $\mathbf{6 0 0}$ days.

Table 7 E-V-M-E abort options with a DSM

| Launch date, <br> yyyy/mm/dd | Launch <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Mars arrival <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Earth arrival <br> $V_{\infty}, \mathrm{km} / \mathrm{s}$ | DSM, km/s | TOF to <br> Mars, ${ }^{\text {a }}$ days | TOF to <br> Earth, ${ }^{\text {b }}$ days |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $2015 / 06 / 12^{\text {c }}$ | 4.5 | 5.20 | 9.30 | 0.90 | 352 | 588 |
| $2016 / 08 / 03$ | 4.5 | 6.23 | 7.42 | 0.42 | 662 | 757 |
| $2017 / 03 / 29^{\text {c }}$ | 4.5 | 5.33 | 8.03 | 0.00 | 367 | 681 |
| $2018 / 06 / 11$ | 4.5 | 6.08 | 6.20 | 1.08 | 725 | 973 |
| $2020 / 02 / 29$ | 4.5 | 6.66 | 4.62 | 0.24 | 589 | 961 |
| $2021 / 11 / 22^{\text {c }}$ | 4.5 | 5.42 | 6.48 | 0.00 | 323 | 582 |
| $2023 / 01 / 30$ | 4.5 | 7.17 | 7.52 | 0.00 | 630 | 766 |
| $2024 / 09 / 25$ | 3.6 | 6.99 | 8.11 | 0.76 | 599 | 930 |
| $2026 / 07 / 31$ | 4.5 | 12.5 | 13.10 | 0.00 | 521 | 886 |
| $2028 / 02 / 23$ | 4.5 | 8.62 | 15.89 | 1.23 | 586 | 770 |
| $2029 / 06 / 14$ | 4.5 | 4.70 | 8.18 | 0.00 | 650 | 868 |

${ }^{\text {a }}$ TOF to Mars is the TOF for E-M. ${ }^{\text {b }}$ TOF to Earth is the TOF for E-M-E. ${ }^{c}$ Option conforms to all mission constraints.

Table 8 Tether designs for E-V-M-E abort options

| Launch date, yyyy $/ \mathrm{mm} / \mathrm{dd}$ | DSM, km/s | $m_{C} / m_{H}$ | Tether mass $\left(m_{T}\right), \mathrm{Mg}$ | Tether length $\left(L_{C}+L_{H}\right), \mathrm{km}$ | $m_{T} / m_{H}$ | $m_{T} / m_{P}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2015/06/12 ${ }^{\text {a }}$ | 0.90 | 0.44 | 38.0 | 231 | 0.62 | 2.3 |
| 2016/08/03 | 0.42 | 0.44 | 8.94 | 55.9 | 0.15 | 1.2 |
| 2017/03/29 ${ }^{\text {a }}$ | 0.00 | 0.44 | ${ }^{\text {b }}$ | ${ }^{\text {b }}$ | $\square^{\text {b }}$ | b |
| 2018/06/11 | 1.08 | 0.44 | 54.0 | 320 | 0.89 | 2.6 |
| 2020/02/29 | 0.24 | 0.44 | 3.15 | 19.7 | 0.05 | 0.76 |
| 2021/11/22 ${ }^{\text {a }}$ | 0.00 | 0.44 | $\square{ }^{\text {b }}$ | $\square{ }^{\text {b }}$ | $\square{ }^{\text {b }}$ | $\square{ }^{\text {b }}$ |
| 2023/01/30 | 0.00 | 0.44 | b ${ }^{\text {b }}$ | [ b | [ ${ }^{\text {b }}$ | b |
| 2024/09/25 | 0.76 | 0.44 | 27.8 | 171 | 0.46 | 2.0 |
| 2026/07/31 | 0.00 | 0.44 | [ ${ }^{\text {b }}$ | [b | $\square^{\text {b }}$ | - b |
| 2028/02/23 | 1.23 | 0.44 | 70.4 | 407 | 1.2 | 2.9 |
| 2029/06/14 | 0.00 | 0.44 | - ${ }^{\text {b }}$ | $\square^{\text {b }}$ | _b | - ${ }^{\text {b }}$ |

${ }^{\text {a }}$ Option conforms to all mission constraints. ${ }^{\text {b }}$ There are no geometric requirements for the tether when the DSM is zero.

Table 9 Selected abort options (with a DSM) for human missions to Mars

| Launch date, yyyy $/ \mathrm{mm} / \mathrm{dd}$ | Path | Launch $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Mars arrival $V_{\infty}, \mathrm{km} / \mathrm{s}$ | Earth arrival $V_{\infty}, \mathrm{km} / \mathrm{s}$ | DSM, km/s | $m_{T} / m_{P}$ | TOF to <br> Mars, days | TOF to <br> Earth, days |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2014/01/13 ${ }^{\text {a }}$ | E-M-V-E | 3.60 | 6.98 | 4.81 | 0.00 | b | 170 | 800 |
| 2015/06/12 | E-V-M-E | 4.50 | 5.20 | 9.30 | 0.90 | 2.3 | 352 | 588 |
| 2016/02/28 ${ }^{\text {a }}$ | E-M-E | 3.59 | 8.13 | 4.77 | 1.12 | 2.9 | 140 | 780 |
| 2018/05/10 ${ }^{\text {a }}$ | E-M-E | 3.90 | 7.09 | 5.06 | 0.71 | 1.9 | 187 | 759 |
| 2020/07/27 ${ }^{\text {a }}$ | E-M-E | 4.50 | 5.59 | 5.01 | 0.50 | 1.4 | 134 | 742 |
| 2021/11/22 | E-V-M-E | 4.50 | 5.42 | 6.48 | 0.00 | [ ${ }^{\text {b }}$ | 323 | 582 |
| 2022/09/12 ${ }^{\text {a }}$ | E-M-E | 4.52 | 4.94 | 4.90 | 1.01 | 2.5 | 171 | 753 |
| 2024/10/17 ${ }^{\text {a }}$ | E-M-E | 4.56 | 6.07 | 4.86 | 1.12 | 2.7 | 180 | 753 |
| 2026/11/21 ${ }^{\text {a }}$ | E-M-E | 4.51 | 7.83 | 4.85 | 0.91 | 2.3 | 172 | 747 |
| 2028/12/28 ${ }^{\text {a }}$ | E-M-E | 3.97 | 8.22 | 4.69 | 1.22 | 2.9 | 147 | 765 |

${ }^{\mathrm{a}}$ Option conforms to all mission constraints. ${ }^{\mathrm{b}}$ There are no geometric requirements for the tether when the DSM is zero.
the mission to Mars in the E-V-M-E path.The crew's exposure to potential radiation hazards during the transfer to Mars is increased by adopting the $\mathrm{E}-\mathrm{V}-\mathrm{M}-\mathrm{E}$ trajectory.

The best options for the E-V-M-E abort trajectories are listed in Table 7. Many of the options are free returns that do not require a $\Delta V$. Note that only 2018 and 2028 require a $\Delta V$ greater than $1 \mathrm{~km} / \mathrm{s}$. From the trajectories listed in Table 7, we identify the 2015, 2017, and 2021 opportunities as potential abort options. Although the TOFs to Mars are all over 300 days, the total TOF to arrive at Earth for these trajectories are all less than 700 days. The 2021 opportunity is the best E-V-M-E alternative with a TOF to Mars of 323 days and a TOF to return to Earth of only 582 days. Table 8 presents the tether designs needed for the E-V-M-E abort trajectories. There are no geometric constraints for the tether transport facility in the five free-return options. We note that in all of the cases presented, $m_{T} / m_{P}<3$.

## Discussion

Table 9 contains our best abort scenario trajectory options between 2014 and 2030. Opportunities that closely match our mission
constraints exist in every Earth-Mars synodic period (approximately 2.14 years). Although the 2016, 2026, and 2028 options have Mars arrival $V_{\infty}>7.1 \mathrm{~km} / \mathrm{s}$, we have accepted the opportunities because their relatively high DSMs are useful: the spinning tether can reduce the magnitude of the arrival $V_{\infty}$ at Mars so that the entry conditions achieve the mission constraints. The E-M-E trajectories recommended for 2018 and 2020 require DSMs of 0.71 and $0.5 \mathrm{~km} / \mathrm{s}$, which can be achieved by using the descent engines. Although the DSMs of the remaining E-M-E options are too large for the descent engines alone, the DSMs might be realized via a combination of the tether rotation and descent engines. The final preferred case in 2014 is a free-return trajectory and, therefore, the tethered transport's geometry is independent of the trajectory.

We note that most of the trajectory options listed in Table 9 follow the E-M-E path. The only E-M-V-E case listed occurs in 2014, and E-V-M-E cases are suggested for 2015 and 2021. As noted earlier, the E-V-M-E trajectory options violate the TOF design limits and increase the radiation risk for astronauts. We present free-return trajectory options for 2014 and 2021. The most difficult years for abort scenarios that meet our design constraints appear to be 2016,

2026, and 2028. A logical approach to reduce the mass of the tether for our preferred trajectory options is to combine the spinning tether system with the descent stage engines. Of course, this would prevent the abort scenarios from being propellant free.

## Conclusions

A minimum-mass, spinning tether transport can facilitate the propellant-free return of astronauts to Earth in the event of an aborted landing on Mars. We have identified abort scenarios in every EarthMars synodic period between 2014 and 2030 that closely match the mission parameters of NASA's DRM. Most of our recommended abort options follow an Earth-Mars-Earth path with a small DSM. Our minimum-mass tether design methodology enabled us to develop transport configurations for the abort scenarios with a tether-mass-to-propellant-mass ratio of less than 3 . Relaxation of the constraints for human missions to Mars and improvements in tether strength-to-weight ratios may produce more abort options. Further investigation of potential transport configurations is needed to determine practical design limits for the tether mass ratios. The abort scenarios and artificial-gravity tether transports presented in this paper have the potential to play an important role in missions to Mars.

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