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Secure E-voting for Preferential Elections ^{*}

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Abstract. Electronic voting (e-voting) systems can greatly enhance the efficiency, and potentially, the transparency of national elections. However, the security of such systems is an area of on-going research. The literature for secure e-voting is predominantly concerned with 1-out-of- m voting strategies, where m is the number of candidates running for the elections. This paper presents a case study of cryptologic protocols for secure e-voting systems that use preferential voting strategies.

1 Introduction

Many types of voting strategies are employed around the world. Although there has been extensive research for cryptologic protocols for binary voting strategies (yes or no votes), the attention to preferential voting systems [2] is minimal. In such voting systems, each voter is required to rank, provide an order of preference for, the candidates. If no candidate receives a majority, more than half of first preference votes, the candidate with the lowest first preference vote is eliminated. Votes of the eliminated candidate are redistributed to the remaining candidates depending on the second preference. Repeatedly, more candidates are eliminated until one reaches a majority.

A notion of security for e-voting systems can be summarised as the confidentiality service for individual voter-vote relationships. This can be formalised as $Conf(ID, Vote)$, where $Conf(\dots)$ is a confidentiality service, ID is a voter's identity, and $Vote$ is the vote of that voter. Such a security is achieved using one of two techniques, namely $(ID, Conf(Vote))$ or $(Conf(ID), Vote)$. The vote either remains confidential or anonymous even after the end of the elections. This paper will adapt a proposal from each of these two techniques to preferential voting systems and study the resulting efficiency.

2 Preferential Voting using Homomorphic Encryption

This section will discuss the use of homomorphic encryption in secure e-voting systems, which uses the $(ID, Conf(Vote))$ technique, to accommodate a preferential voting strategy.

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When $m = 20$ and $l = 1000$, the size of the modulus is: $|N| = 10 \times 20!$ bits. Clearly, such a size for a modulus is impractical as numerous exponentiation operations are required.

3 Preferential Voting using Mix-Networks

This section will discuss the use of mix-networks in secure e-voting system. It presents an implementation, using the $(Conf(ID), Vote)$ technique, of a robust mix-network for a simple and relatively secure preferential e-voting system.

3.1 Mix-Networks

Let D be a decryption algorithm computable only by the mix-network. Let $\phi : \mathbb{Z}_n \rightarrow \mathbb{Z}_n$ be a randomly chosen secret permutation function. The operation of the mix-network can be described by the following operation: $m_{\phi(i)} = D(c_i)$, where $i \in \mathbb{Z}_n$. The LHS of the previous equation is a random sorted set of plaintexts, $m_{\phi(i)}$, corresponding to the RHS, decryption, D , of a set of input ciphertexts, c_i .

The input to the mix-network could be of the form $(ID, Conf(Vote))$, and the output would be of the form $(Conf(ID), Vote)$. Thus, a mix-network can be viewed as a confidentiality translation service translating the confidentiality service from the vote (or data) to the identity.

Abe [1] proposed a mix-network using ElGamal encryption algorithm in re-encrypting the set of input messages, $I_v = \{c_i | i \in \mathbb{Z}_n\}$, to produce a randomly permuted set of output messages, $O_v = \{m_{\phi(i)} | i \in \mathbb{Z}_n\}$. The next section will use the mix-network by Abe.

3.2 Preferential Voting and Mix-Networks

The mix-network by Abe can be used to construct electronic secret ballot voting schemes. In such schemes, the vote need not be in a special form as the tabulation phase is conducted using the plaintext vote anonymised. In contrast to schemes based upon homomorphic encryption, the size of input messages does not directly affect the efficiency of the mix-network.

In electronic preferential voting employing mix-network, the vote can be of the form an integer ranging from 1 to $m!$, where m is the number of candidates running for the election. Thus, the message size is $\lceil \log_2(m!) \rceil = 62$ bits, where $m = 20$. Let $j \in \mathbb{Z}_l$ be an index into a list of voters, so that l is the number of voters.

We propose a generic e-voting scheme utilising the above mix-network as follows:

Set-up: The election officials publish the parameters for a threshold decryption cryptosystem [4], (E, D) , such that $E^k(\dots)$ is the public encryption function, where k is a random value chosen by the voter, and $D(\dots)$ is a t -out-of- n decryption function.

Vote submission: Each voter j :

1. selects a sequence, $i_j \in \{1, \dots, m!\}$, to represent his/her preference;
2. encrypts the selection, e.g: $E^{k_j}(i_j)$;
3. identifies itself to the vote collecting official to establish its identity, ID ;
and,
4. communicates the encrypted vote, $E(i_j)$, to the vote collecting official.

The voting official verifies the identity of every voter and forwards the set of votes from valid voters, $U = \{E^{k_j}(i_j)\}$, to the mix-network.

Vote mixing: The mix-network permutes and decrypts the objects from the set U and outputs a set of plaintext votes V , such that the correspondence between the objects in U and the objects in V are a secret.

Vote tabulation: The election official electronically processes the plaintext vote in V by using a program for counting the preferences and calculating the elected candidate.

The processing cost is mainly contributed by the mixing operation. The mix-network is composed of a number of gates, and the computational cost for each gate is 23.6 modular exponentiations [1]. Each voter generates exactly one input message to the mix-network. Providing $2 \log_2 l - 1$ delay [1] per input, where $l = 1000$ is the number of inputs to the mix-network, total computational cost of the mix-network is $23.6(2 \log_2 l - 1)t = 448400$ modular exponentiations.

4 Conclusion

The size of the electronic vote for a preferential voting system is inherently larger than a 1-out-of- m voting system, when the number of candidates, m , increases. In preferential voting system, the size of the vote is at least $\log_2(m!)$ bits. Therefore the voting systems using some form of homomorphic encryption [3] tend to be inefficient or impractical.

Voting systems that employ mix-networks, on the other hand, do not require a special form for the electronic vote. The computational complexity is not adversely affected by the number of candidates. Therefore, mix-network based voting systems are ideally suited for preferential voting systems. Future research will be directed towards the design of more efficient robust mix-networks.

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