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## Theoretical and experimental correlations of gas dissolution, diffusion, and thermodynamic properties in determination of gas permeability and selectivity in supported ionic liquid membranes

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### ABSTRACT

Supported ionic liquid membranes (SILMs) has the potential to be a new technological platform for gas/organic vapour separation because of the unique non-volatile nature and discriminating gas dissolution properties of room temperature ionic liquids (ILs). This work starts with an examination of gas dissolution and transport properties in bulk imidazolium cation based ionic liquids [C<sub>n</sub>mim][NTf<sub>2</sub>] (n = 2, 4, 6, 8, 10) from simple gas H<sub>2</sub>, N<sub>2</sub>, to polar CO<sub>2</sub>, and C<sub>2</sub>H<sub>6</sub>, leading to a further analysis of how gas dissolution and diffusion are influenced by molecular specific gas-SILMs interactions, reflected by differences in gas dissolution enthalpy and entropy. These effects were elucidated again during gas permeation studies by examining how changes in these properties and molecular specific interactions work together to cause deviations from conventional solution–diffusion theory and their impact on some remarkably contrasting gas perm-selectivity performance. The experimental perm-selectivity for all tested gases showed varied and contrasting deviation from the solution–diffusion, depending on specific gas-IL combinations. It transpires permeation for simpler non-polar gases (H<sub>2</sub>, N<sub>2</sub>) is diffusion controlled, but strong molecular specific gas-ILs interactions led to a different permeation and selectivity performance for C<sub>2</sub>H<sub>6</sub> and CO<sub>2</sub>. With exothermic dissolution enthalpy and large order disruptive entropy, C<sub>2</sub>H<sub>6</sub> displayed the fastest permeation rate at increased gas phase pressure in spite of its smallest diffusivity among the tested gases. The C<sub>2</sub>H<sub>6</sub> gas molecules “peg” on the side alkyl chain on the imidazolium cation at low concentration, and are well dispersed in the ionic liquids phase at high concentration. On the other hand strong CO<sub>2</sub>-ILs affinity resulted in a more prolonged “residence time” for the gas molecule, typified by reversed CO<sub>2</sub>/N<sub>2</sub> selectivity and slowest CO<sub>2</sub> transport despite CO<sub>2</sub> possess the highest solubility and comparable diffusivity in the ionic liquids. The unique transport and dissolution behaviour of CO<sub>2</sub> are further exploited by examining the residing state of CO<sub>2</sub> molecules in the ionic liquid phase, which leads to a hypothesis of a condensing and holding capacity of ILs towards CO<sub>2</sub>, which provide an explanation to slower CO<sub>2</sub> transport through the SILMs. The pressure related exponential increase in permeations rate is also analysed which suggests a typical concentration dependent diffusion rate at high gas concentration under increased gas feed pressure. Finally the strong influence of discriminating and molecular specific gas-ILs interactions on gas perm-selectivity performance points to future specific design of ionic liquids for targeted gas separations.

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## 1. Background

Research in room temperature ionic liquids (RTILs) started with main focus on exploring the unique and specific solvent and catalytic properties in homogeneous or heterogeneous catalysis [1,2], aiming for greater selectivity, specificity and yield at reduced environmental liabilities. Many ionic liquids also exhibit unique solubility, transport and separation properties [3,4], which led to spreading research in using ionic liquids as a selective separation media for gas separation, enrichment and solvent extraction. There exists a great interest in exploitation of RTILs for CO<sub>2</sub> capture and storage due to its distinctively large solubility in a variety of ionic liquids in comparison to other simple gases. A strong interest has also been developing in olefin–paraffin separation using RTILs where transport is facilitated by partially polarised silver ions [5,6]. On technological and process development, the negligible volatility of ionic liquids makes them a good choice for supported liquid membrane. The main difficulty of conventional supported liquid membrane lies with preparing a stable and immobilized liquids film on a support solid media because the liquids slowly evaporate, destabilising selective properties and flux through the membrane, also causing contamination to feed gas streams [5,7,8]. Non-volatile and selective ionic liquids supported on porous membranes have distinctive advantages because the ionic liquids do not evaporate, and their high viscosity may provide additional stability to pressure displacement from the solid porous support. Most reported studies of SILM used microporous membrane as support, and gas transport/separation studies were conducted in single gas feed system operating under low pressure differential to avoid displacement of ionic liquids [9,10]. These studies succeeded in obtaining information and knowledge in relation to gas solubility, diffusivity and permeability under low gas phase pressure. However, gas solubility and diffusion behaviour in solvent at increased concentration under high gas phase pressure may deviate from the standard dissolution and diffusion behaviour, especially when gas–solvent molecular interactions may further influence the transport process. Previously we reported a study of ionic liquids supported on nano-pore membrane which exhibited extraordinary membrane stability under high gas phase pressure [11]. This work aims to built on the process development by providing a theoretical analysis of gas dissolution and transport in the pressure stable SILMs.

Many recent works on gas permeability and selectivity involve CO<sub>2</sub> because of its strong solubility in most ionic liquids. Park et al. reported gas permeability of CO<sub>2</sub>, H<sub>2</sub>S, and CH<sub>4</sub> in a poly(vinylidene fluorolide) supported [C<sub>4</sub>mim][BF<sub>4</sub>] membrane. Ideal selectivity for the CO<sub>2</sub>/CH<sub>4</sub> gas pair was calculated by single gas permeation at 40 [12]. Bara et al. used poly(ethersulfone) (PES) supported [NTf<sub>2</sub>] ILs containing perfluoroalkyl substituents, and reported the highest selectivity of 19 and 27 for CO<sub>2</sub>/CH<sub>4</sub> and CO<sub>2</sub>/N<sub>2</sub> respectively [13,14]. Sulphur dioxide, which has similar molecular structure of CO<sub>2</sub>, was also studied in a PES SILM using various ILs. Ideal selectivity of SO<sub>2</sub>/CH<sub>4</sub> was found to be 144 in [C<sub>4</sub>mim][BF<sub>4</sub>] at 25 °C [15]. Pennline et al. presented CO<sub>2</sub> removal from fuel gas in membrane gas separation using polyethylsulfone to support two ILs, [C<sub>6</sub>mim][NTf<sub>2</sub>] and [C<sub>4</sub>mim][NO<sub>3</sub>]. Ideal selectivity of CO<sub>2</sub>/H<sub>2</sub> was found to be 6 and 5.20 respectively at 310 K [16]. Similar work was carried out by Myers

et al., who found the selectivity of CO<sub>2</sub>/H<sub>2</sub> in [C<sub>3</sub>NH<sub>2</sub>mim][NTf<sub>2</sub>] SILM increased with increasing temperature from 37 to 85 °C, due to the larger activation energy of complex [17]. Ionic liquids had also been studied in the separation of CO<sub>2</sub> from flue gases emitted from fossil-fuel combustion operations [18], due to its high solubility in ionic liquids. In the CO<sub>2</sub>/H<sub>2</sub> system, a CO<sub>2</sub> selectivity of 30–300 was observed in [C<sub>4</sub>mim][PF<sub>6</sub>] [19].

Scovazzo et al. [5] studied RTIL-membranes made from the water stable anions: bis(trifluoromethanesulfonyl)amide [NTf<sub>2</sub>]<sup>−</sup>, trifluoromethanesulfone [CF<sub>3</sub>SO<sub>3</sub>]<sup>−</sup>, chloride [Cl]<sup>−</sup>, and dicyanamide [dca]<sup>−</sup>. The CO<sub>2</sub> permeability on the SILMs are related to the CO<sub>2</sub> solubilities in ILs. The flux and ideal selectivities for the gas pairs CO<sub>2</sub>/N<sub>2</sub> from 15 (for [[Cl]<sup>−</sup>]) to 61 (for [dca]<sup>−</sup>); and CO<sub>2</sub>/CH<sub>4</sub> ideal selectivities range from 4 (for [[Cl]<sup>−</sup>]) to 20 (for [dca]<sup>−</sup>). Recently, Scovazzo et al. reported long-term continuous mixed gas separation selectivity on SILMs [20]. It was found mixed gas operation did not reduce the advantageous gas separation selectivities, compared with single gas ideal selectivity; membrane continued to give advantageous operations even under dry gas feed conditions; and long-term stability of more than 106 days confirmed in continuous flow operations without any detectable performance loss.

Solution–diffusion theory has been the backbone theory for gas transport through dense nonporous membranes, which has also been intensively evoked for SILM studies. However, uncertainty and discrepancy persist in relating the independently measured gas solubility/diffusivity/thermodynamic data in bulk ILs to observed gas permeation and separation performance in SILMs, which are often complicated by the complex molecular interactions between diffusing gas molecules and molecules of ionic liquids, which are more complex in structure and property performance than simple solvents. This weak link has been largely neglected so far but needs to be addressed more systematically and in depth so as to catch up with the fast research progress in SILM technology and process development. Therefore it is the main aim of this work to provide such a framework analysis of the interrelations between gas dissolution/diffusion properties and gas perm-selectivity in SILMs. It is necessary to state that the scope and accuracy of such an analytical attempt may be constrained and dependent on the availability and experimental accuracy of data on gas solubility and diffusivity. The limited understanding of gas-ionic liquid interactions at molecular level can be another limiting factor, which often leads to non-ideal behaviour of gas dissolution and concentration dependent diffusion.

## 2. Materials and experimental methods

### 2.1. Materials

Thin-film cellulose acetate nanofiltration membrane discs were purchased from Sterlitech Corporation (YMHLS1905). The key relevant membrane parameters are given in Table 1. Scanning electron microscope (JEDL-6400, Link Analytical) showed the membrane has an asymmetric structure and a total thickness of 167 ± 2 μm. The membrane is originally designed for acid purification, alcohol purification, BOD/COD reduction, ethylene glycol purification, heavy metal removal, desalting and sugar fractionation. As a nanofiltration

**Table 1**  
Key membrane parameters and chemical/physical properties of ionic liquids used in this work.

Membrane				
Designation	Thickness ( $\mu\text{m}$ )	Ionic rejection	pH Range at 25 °C	Typical water Flux ( $\text{m}^3/\text{m}^2 \text{ bar}$ )
DK nanofiltration	167 $\pm$ 2	98% $\text{MgSO}_4$	2 – 14	22/100
Ionic liquids properties at T=298K				
Ionic liquids	Viscosity (cP)	Density ( $\text{g cm}^{-3}$ )	Molar volume ( $\text{cm}^3\text{mol}^{-1}$ )	
$[\text{C}_2\text{mim}][\text{NTf}_2]$	54.1	1.52	258.0	
$[\text{C}_4\text{mim}][\text{NTf}_2]$	69.0	1.44	292.0	
$[\text{C}_{10}\text{mim}][\text{NTf}_2]$	124.0	1.27	404.1	
$[\text{C}_4\text{mim}][\text{OTf}]$	93.2	1.29	230.9	
$[\text{C}_4\text{mim}][\text{BF}_4]$	103.0	1.21	189.3	
$[\text{C}_4\text{mim}][\text{PF}_6]$	320.3	1.35	207.8	
Illustration of cation molecular structure $[\text{C}_4\text{mim}]^+$ , $[\text{C}_{10}\text{mim}]^+$ , and anion $[\text{OTf}]^-$ , $[\text{NTf}_2]^-$ , $[\text{BF}_4]^-$				
<p>1-methyl-3-butylimidazolium</p> <p>1-methyl-3-decylimidazolium</p> <p>Bistrifluoromethanesulfonimide</p> <p>Trifluoromethanesulphonate</p> <p>Tetrafluoroborate</p>				

membrane it contains functionalised groups carrying charges on the polymer chains. The membrane is compatible with chemical organic groups aliphatic hydrocarbons, halogenated hydrocarbons, alcohol, and acids, but unstable when in contact with aromatic hydrocarbons, asymmetric halogenated hydrocarbons, ketones, ethers, and esters.

All the ionic liquids used in this study were synthesised in QUILL (Queen's University Ionic Liquid Laboratory) [21]. NMR were used to analyse bromide residual and other impurities as minute amount impurities may have significant influence on thermodynamic and thermo-physical properties of the ionic liquids. The most relevant physical and chemical properties of the ionic liquids used in this work are also presented in Table 1.

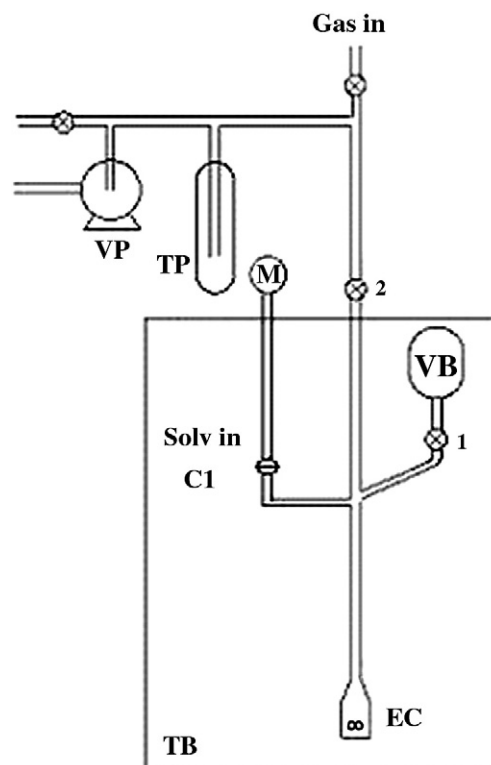
## 2.2. Gas solubility measurement

An isochoric saturation technique was used for gas solubility measurement. Detailed procedures were reported in Ballerat-Busseroles et al. [22,55]. Briefly, a known quantity of gaseous solute is put in contact with a precisely determined quantity of degassed solvent at a constant temperature inside an accurately known volume. When thermodynamic equilibrium is attained, the pressure above the liquid solution is constant and is directly related to the solubility of the gas in the liquid (Fig. 1).

## 2.3. Preparation of supported ionic liquid membranes and their stability

Detailed preparation of the supported ionic liquid membranes was reported previously [11]. Briefly the pristine nanofiltration membranes were soaked in the ionic liquids for 24 h. The excess ILs on the surface of the membrane was carefully removed by clean cotton tissue. The nanofiltration membranes have excellent affinity and wettability in the ionic liquids with 45% of IL weight uptake after soaking. The SILMs are stable under pressure and over long operating time with practically little loss of the ionic liquids.

The stabilising mechanism based on the interactions between cations/anions with the charged NF membrane materials in a nano spatial scale is not entirely clear. It is speculated that strong cationic/



**Fig. 1.** Gas solubility measurement apparatus (TB: thermo bath; EC: equilibrium cell; VB: calibrated gas bulb; M: manometer; TP: cold trap).

anionic interactions with functional groups present at the nanopore walls within a radial dimension of 1–10 Å may form structured arrangement of the cations/anions within the nanopore networks. Such a formation could give rise to unique gas transport and separation properties different to ionic liquids in bulk liquid conditions.

#### 2.4. Gas permeation studies

The experimental apparatus for the gas transport measurement is composed of a gas cylinder, pressure gauge, pressure sensor, gas reservoir, membrane separation cell, cold trap and the vacuum pump, as show in the process diagram in Fig. 2. All cells, tubes and valves are designed for high-pressure application. The flat sheet NF membrane was mounted in a SEPA stainless steel membrane filtration cell (Sterlitech Corporation) with a holding volume of 300 mL and an effective membrane permeation area of 16.9 cm<sup>2</sup>. The SEPA cell is placed in a temperature controlled water bath to maintain a constant temperature during gas permeation. All gas permeation tests were conducted at constant T = 303 K.

### 3. Results and discussion

#### 3.1. Gas solubility in ionic liquids

Since Blanchard et al. firstly reported gas solubilities in ionic liquids in 2000 [23], gas solubilities in many common ionic liquids are reported [24–27]. The literature data obtained from the IUPAC (International Union of Pure and Applied Chemistry) database contains solubility data for fifteen gases in 27 ionic liquids. It is also possible to develop correlations which can be used to predict gas solubility in ionic liquids [28]. Among all gases, carbon dioxide is the most intensively reported due to its outstanding solubility in most ionic liquids. It was generally found that gas molecules with dipole movement such as carbon dioxide, sulphur dioxide, and nitrous oxide have the highest solubilities and strongest interactions with the ionic liquids, followed by ethylene and ethane. Gases such as oxygen, nitrogen, hydrogen, and carbon monoxide have very low solubilities and low interactions with ionic liquids [29,30]. Based on recent experimental, spectroscopic and molecular simulation studies, it transpires that anions dominate the interactions with the gas molecular, with the cations playing a secondary role [31–34]. Gas solubility data

pertinent to many gas separations are still incomplete. For engineering applications, accurately measured gas solubility at a pressure greater than atmosphere pressure is important but difficult to obtain for some experimental methods such as volumetric method and gravimetric method.

Solubility of CO, CO<sub>2</sub>, CH<sub>4</sub>, C<sub>2</sub>H<sub>6</sub> were measured in this work using the isochoric saturation method. Henry's law constant for gas dissolution can be calculated in theory from the mole fraction solubilities as:

$$K_H \equiv \lim_{x_2 \rightarrow 0} \left( \frac{f_2(p_{eq}, T_{eq}, y_2)}{x_2} \right) = \lim_{x_2 \rightarrow 0} \left( \frac{\phi_2(p_{eq}, T_{eq}) p_{eq}}{x_2} \right) \cong \left( \frac{\phi_2(p_{eq}, T_{eq}) p_{eq}}{x_2} \right)$$

Detailed experimental procedure and calculation procedure in relation to the above equation can be found in Anthony et al. [34]. H<sub>2</sub> and N<sub>2</sub> have very low solubility in the ionic liquids, and difficult to measure accurately by the method used in this work. Our literature survey found only one reported H<sub>2</sub> solubility data [35] in [C<sub>4</sub>mim][NTf<sub>2</sub>], and no literature data available at all on N<sub>2</sub> solubility in [C<sub>4</sub>mim][NTf<sub>2</sub>], except in ionic liquids [C<sub>4</sub>mim][BF<sub>4</sub>] [55]. In the absence of experimental data, the thermodynamic model, COSMO-RS, was used for *a priori* prediction of gas solubility in ionic liquids. Briefly, COSMO calculations were performed on each individual ion or molecule using the TURBOMOLE [36] quantum chemistry package. Computations were carried out on the density functional theory (DFT) level, using the BP functional [28,37] with a triple-valence polarised basis set (TZVP) [38] Where applicable, optimised radii [39] were used in the COSMO calculation (H = 1.30, C = 2.00, N = 1.83, O = 1.72, F = 1.72, S = 2.16, Cl = 2.05, Br = 2.16, I = 2.32); otherwise, 1.17 × vdW radii were used. To generate gas solubility calculations, the COSMO files were imported into COSMOthermX software and a ternary system (gas + cation + anion) was used as the basis for the calculations, as recommended by COSMOlogic [40]. The calculated mol fraction of gas in the liquid phase was then converted to mol fraction for a binary system (gas + ionic liquid).

Experimental and predicted Henry constant and gas mole fraction for H<sub>2</sub>, N<sub>2</sub>, CO, CO<sub>2</sub>, CH<sub>4</sub>, C<sub>2</sub>H<sub>6</sub> in ionic liquid [C<sub>4</sub>mim][NTf<sub>2</sub>] are presented in Table 2. The CO<sub>2</sub> solubility is one magnitude higher than other gases, and C<sub>2</sub>H<sub>6</sub> solubility is also one order of magnitude higher than non polar H<sub>2</sub> and N<sub>2</sub>.

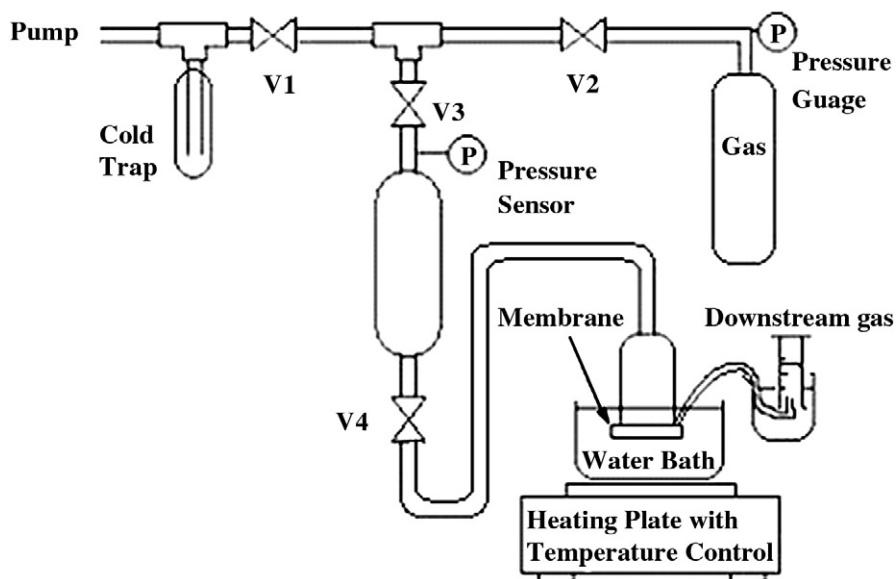


Fig. 2. Flow diagram for gas permeation test through the SILMs.



**Table 2**H<sub>2</sub>, N<sub>2</sub>, CO, CO<sub>2</sub>, CH<sub>4</sub> and C<sub>2</sub>H<sub>6</sub> gas solubilities in [C<sub>4</sub>mim][NTf<sub>2</sub>] expressed as Henry's law coefficient  $K_H$  and mole fraction  $x$ .

T/K	$K_H/10^5\text{Pa}$	$x/10^{-3}$	AAD	T/K	$K_H/10^5\text{Pa}$	$x/10^{-3}$	AAD
[C <sub>4</sub> mim][NTf <sub>2</sub> ] + CO <sub>2</sub> (experimental)				[C <sub>4</sub> mim][NTf <sub>2</sub> ] + C <sub>2</sub> H <sub>6</sub> (experimental)			
303.2	35.46	28.20	0.0%	303.7	105.7	9.465	0.1%
313.1	42.08	23.77	0.1%	313.8	118.3	8.455	0.6%
323.0	49.42	20.23	0.1%	324.2	140.2	7.133	0.1%
332.9	57.35	17.44	0.0%	334.0	165.5	6.042	1.3%
[C <sub>4</sub> mim][NTf <sub>2</sub> ] + CH <sub>4</sub> (experimental)				[C <sub>4</sub> mim][NTf <sub>2</sub> ] + CO (experimental)			
303.2	345.5	2.894	0.8%	303.2	653.8	1.529	4.0%
313.1	369.7	2.705	1.6%	313.1	659.5	1.516	3.0%
323.1	414.2	2.415	2.1%	323.0	732.3	1.366	1.4%
333.1	419.3	2.385	4.3%	333.0	816.8	1.224	0.1%
[C <sub>4</sub> mim][NTf <sub>2</sub> ] + N <sub>2</sub> (COSMO prediction)				[C <sub>4</sub> mim][NTf <sub>2</sub> ] + H <sub>2</sub> (COSMO prediction)			
303.0	537.5	0.19		303.0	2016.1	0.50	
313.0	607.5	0.17		313.0	2140.2	0.47	
323.0	680.1	0.15		323.0	2261.3	0.45	
333.0	754.5	0.13		333.0	2379.2	0.43	

In Table 2, Average Absolute Deviation (AAD) was calculated based on the equation:

$$AAD = 100 \left( \frac{\sum_{i=0}^n \left| \frac{x_i - x_i^{ref.}}{x_i^{ref.}} \right|}{n} \right) = 100 \left( \frac{\sum_{i=0}^n |\delta_i|}{n} \right)$$

An average of ten sample data was measured at each temperature.

CO<sub>2</sub> solubility in other ionic liquids were also measured for [C<sub>4</sub>mim][BF<sub>4</sub>] and [C<sub>4</sub>mim][PF<sub>6</sub>] which possess the same cation but differ in anions, and also in ionic liquids [C<sub>2</sub>mim][NTf<sub>2</sub>], [C<sub>6</sub>mim][NTf<sub>2</sub>] and [C<sub>8</sub>mim][NTf<sub>2</sub>] which all share the same [NTf<sub>2</sub>]<sup>-</sup> anion but differ in the length of the side alkyl chain on the cation [C<sub>n</sub>mim]<sup>+</sup>. Henry's law constant and dissolved gas mole fraction are presented in Table 3 to illuminate the effect of cation and anion on the gas solubility. Anions had strong influence on gas solubility and the results shows that CO<sub>2</sub> solubility in [C<sub>4</sub>mim] cation based ionic liquids followed the order [BF<sub>4</sub>]<sup>-</sup><[PF<sub>6</sub>]<sup>-</sup><[NTf<sub>2</sub>]<sup>-</sup>, similar to data reported by Anthony et al. [29]. Cations difference had a lesser effect, and CO<sub>2</sub> solubility increases slightly with increasing length of the alkyl side chain on the imidazolium ring. It is thought that this may be due to entropic reasons, as there may be more free volume within the longer chain ILs, which corresponds to a proportional relationship with the molar volume of ionic liquids [41,42]. Fig. 3 shows that results obtained from this work corroborates well with data reported in literature employing same or different measurement methods [29,42,43].

### 3.2. Gas diffusivity in bulk ionic liquids and in SILM

Directly measured gas diffusivity in bulk ionic liquids are largely incomplete, partially due to experimental difficulties to ascertain slow gas diffusion rate in highly viscous liquids. A time-lag method [44,45]

**Table 3**CO<sub>2</sub> Henry's law constant and mole fraction in [C<sub>n</sub>mim] cation (n = 2,4,6,8) based ionic liquids. T = 303 K P = 1.013 bar.

Ionic liquid	$K_H/10^5\text{Pa}$	$x/10^{-3}$
[C <sub>4</sub> mim][NTf <sub>2</sub> ]	35.5	0.031
[C <sub>4</sub> mim][BF <sub>4</sub> ]	60.8	0.016
[C <sub>4</sub> mim][PF <sub>6</sub> ]	56.5	0.014
[C <sub>2</sub> mim][NTf <sub>2</sub> ]	39.1	0.027
[C <sub>6</sub> mim][NTf <sub>2</sub> ]	35.0	0.029
[C <sub>8</sub> mim][NTf <sub>2</sub> ]	31.0	0.033

was developed for predicting gas diffusivity through SILMs. Both gas solubility and diffusivity are calculated from the equation below from the same set of flux-time data, which does not distinguish the effect of solubility and transport on the permeation rate.

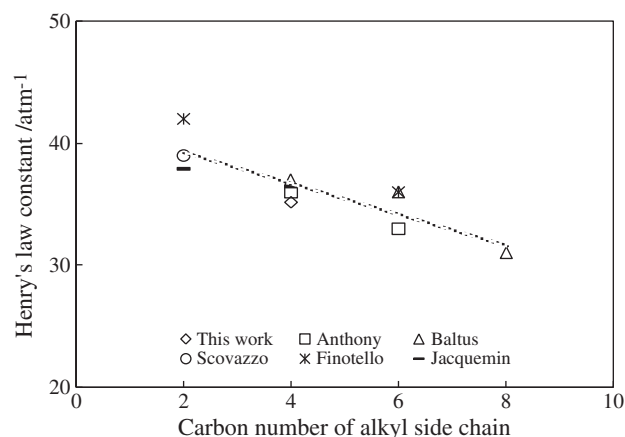
$$\frac{Q_t}{Lc_i} = \frac{Dt}{L^2} - \frac{1}{6} - \frac{2}{\pi} \sum \frac{(-1)^n}{n^2} \exp \left[ \frac{-Dn^2 \pi^2 t}{L^2} \right]$$

where  $c_i$  is the concentration on the feed side and  $n$  is an integer. A curved plot can be observed initially in the transient state but this becomes linear with time as steady-state conditions are attained. When  $t \rightarrow \infty$ , the exponential term can be neglected and it simplifies to:

$$Q_t = \frac{Dc_i}{L} \left( t - \frac{L^2}{6D} \right)$$

If the linear plot of  $Q_t/(Lc_i)$  versus  $t$  is extrapolated to the time axis, the resulting intercept,  $\theta$ , is called the time lag, and the diffusion coefficient can be calculated when the membranes thickness is known.

A number of theoretical prediction of gas diffusivity in liquids is available. The best known Einstein's equation can be applied to molecular diffusion without accounting for interactions between the



**Fig. 3.** Correlation of Henry's law constant for carbon dioxide in [C<sub>n</sub>mim][NTf<sub>2</sub>] (n = 2,4,6,8) ionic liquids.

diffusing molecules and/or with the molecules of the diffusion solvent media.

$$D_{12} = \frac{kT}{n\pi a_1 \mu_2} \quad 4 \leq n \leq 6$$

According to Einstein's equation, the diffusion coefficient of solutes in a liquid is directly proportional to the reciprocal of the molecular radius of the diffusing solute.

The Wilke–Chang expression [46] is one of the widely used empirical correlations for estimating gas diffusion coefficients in liquids which take consideration of molecular interactions and properties of both diffusing molecule and that of the diffusion liquid media.

$$D = [7.48 \times 10^{-8}] \frac{T\sqrt{\alpha M_2}}{\mu_2 \bar{V}_1^{0.6}} \quad \alpha = 0.15$$

whereas,  $\bar{V}_1$  is the molar volume of the gas solute at its normal boiling point,  $\alpha$  is the association constant which accounts for gas-liquid interactions,  $M_2$  refers to the molecular weight of the solvent.

Scheibel correlation [47] modified the Wilke–Chang correlation to eliminate the association factor  $\alpha$ :

$$D_{12} = |C| \frac{T \left( 1 + \left( 3 \frac{\bar{V}_2}{\bar{V}_1} \right)^{2/3} \right)}{\mu_2 \bar{V}_1^{1/3}} \quad C = 8.2 \times 10^{-8}$$

where  $\bar{V}_2$  is the molar volume of the solvent. This equation is developed to eliminate solvent association factor in Wilke–Chang correlation by introducing molar volumes to account for solvent effects.

Although the empirical models have been widely used to predict gas solute diffusivity in water and simple solvents, their applicability and accuracy in predicting gas diffusion coefficient in ionic liquids has yet to be systematically examined. In this work, measured gas diffusivity data for  $O_2$  and  $CO_2$  in bulk ionic liquids from literature [33,45,48] are correlated to the calculated values of diffusivity based on Wilke–Chang and Scheibel model respectively, and the correlation are presented in Figs. 4 and 5. Morgan [45] and Buzzeo's [48] data correlate well with both equations. However, Shiflett's [33] data were around 50% lower than predicted values. The deviation is possibly due to the different methods used for measuring the diffusivity. Morgan and Buzzeo used the time-lag method on a supported ionic liquid membrane, while Shiflett used a one-dimensional diffusion model

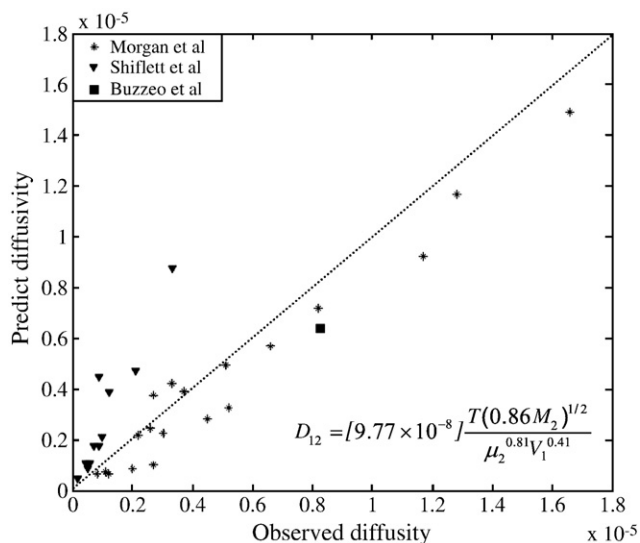


Fig. 4. Diffusion coefficient prediction and correlation using Wilke–Chang correlation.

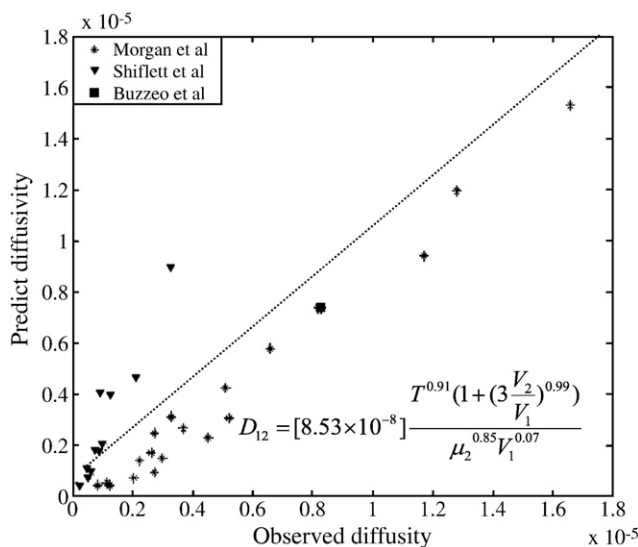


Fig. 5. Diffusion coefficient prediction and correlation using Scheibel correlation.

based on mass transfer [49]. The model in Shiflett's work used the following assumptions: (1) gas concentration in ionic liquid is a very low, so the thermophysical properties of the solution do not change; (2) temperature and pressure kept constant during dissolution; (3) thermodynamic equilibrium is instantly established on the boundary thin layer with a saturation concentration, which the concentration is constant all the time; (4) gas dissolves in one-dimensional diffusion process. These assumptions are reasonable for non polar gas species ( $H_2$ ,  $N_2$ ,  $O_2$ , and  $CO$ ) which have low solubility and low interactive solvation enthalpy and entropy. Also Shiflett's data were measured across a much wide temperature and pressure range from 283.15 to 348.15 K and from 0.10 to 20.0 bar, whilst Morgan and Buzzeo's data can only be obtained at atmospheric pressure because of the pressure instability of their SILMs supported on micron-pore membranes.

Based on the knowledge of ionic liquid viscosity and molar volume presented in Table 1, the Wilke–Chang and Scheibel correlations were used to calculate gas diffusion coefficients for  $H_2$ ,  $N_2$ ,  $CH_4$ ,  $C_2H_6$  and  $CO_2$  in a number of ionic liquids. Liquid molar volume and molecular diameter of the gas species are also presented in the table for reference [50].

The calculated values of the diffusion coefficients followed the order:  $H_2 > N_2 > CO_2 > CH_4 > C_2H_6$  within all three ionic liquids. This order of diffusivity value is in agreement with Einstein predictions based on molecular weight/size. In comparison to diffusion coefficient values in solid polymers reported in literature [51–54], the values of these diffusion coefficients in bulk ionic liquids are one order of magnitude higher than in polyethylene, two order high than in PVC and polyimide, but one order of magnitude lower than some new novel polymers such as PDMS and PTMSP.

### 3.3. Permeation and selectivity of $H_2$ , $N_2$ , $CO_2$ , $CH_4$ , $C_2H_6$

Steady state permeability of hydrogen, carbon dioxide, nitrogen, methane and ethane through the  $[C_4mim][NTf_2]$  supported ionic liquid membrane are presented in Fig. 6. The steady state permeability were obtained after an initial “time lag” stage during which the SILM was saturated with gases before the onset of gas permeation which was observed to be steady with time. The high stability of the SILM supported on the nano-pore membrane enabled steady flux at high pressures relevant to industrial applications. Gas permeability increased exponentially for all five gases with increasing gas feed pressure, with ethane leading the faster increase followed by nitrogen,

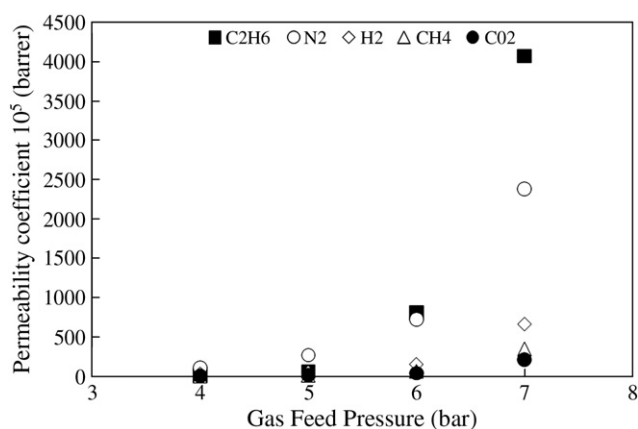


Fig. 6. Steady state gas flux through [C<sub>4</sub>mim][NTf<sub>2</sub>] SILM membrane.

hydrogen, methane and carbon dioxide. The higher ethane permeability is rather remarkable given ethane has the lowest diffusivity and a solubility 3 times less than CO<sub>2</sub>. It is also interesting to note N<sub>2</sub> and H<sub>2</sub> permeates faster than CO<sub>2</sub> in spite of very low solubility in the ionic liquid.

The calculated separation factor or selectivity based on single gas flux rate is calculated for gas pairs N<sub>2</sub>/CO<sub>2</sub>, C<sub>2</sub>H<sub>6</sub>/CO<sub>2</sub>, CH<sub>4</sub>/CO<sub>2</sub>, CH<sub>4</sub>/N<sub>2</sub>. The gas pairs exhibit best separation ratio at lower pressure with the two exceptions all involving C<sub>2</sub>H<sub>6</sub>. The selectivities are compromised when gas fluxes increased, a typical scenario associated with gas separation by most polymeric membranes. CO<sub>2</sub> exhibits the best selectivity against other gas with a maximum N<sub>2</sub>/CO<sub>2</sub> selectivity 31.2 at 4 bar, followed by C<sub>2</sub>H<sub>6</sub>/CO<sub>2</sub> selectivity 21.2 at a different pressure 6 bar.

The solution–diffusion mechanism is an established theory in describing transport through dense nonporous membranes. The theory works well where interactions between the diffusing molecules and the membrane media have negligible effects on permeation and selectivity. Under ideal conditions, the gas permeation rate  $J_i$  (flux) and selectivity  $\alpha_{i,j}$  can be reliably predicted based on the knowledge of gas solubility and diffusivity in the transporting medium:

$$J_i = \frac{S_i D_i}{L} \Delta P = \frac{P_i}{L} \Delta P$$

$$\alpha_{i,j} = \frac{P_i}{P_j} = \frac{S_i D_i}{S_j D_j}$$

Using the gas solubility and diffusivity data presented in Tables 2 and 4, the permeability and theoretical solution–diffusion selectivity

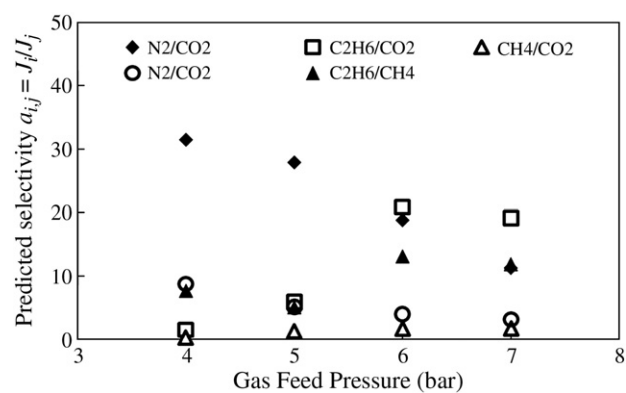


Fig. 7. Predicted selectivity based on single gas permeation measurement for gas pair N<sub>2</sub>/CO<sub>2</sub>, C<sub>2</sub>H<sub>6</sub>/CO<sub>2</sub>, CH<sub>4</sub>/CO<sub>2</sub>, CH<sub>4</sub>/N<sub>2</sub> based on experimental gas permeation data.

for the 5 gas pairs in Fig. 7 are calculated and listed in Table 5, alongside the selectivity value calculated from the experimental permeation data. The value of gas solubility  $S_i$  is the reciprocal value of Henry's law constant adjusted for pressure unit from atm to mmHg.

Data in Table 5 presented a remarkable difference between the theoretically predicted perm-selectivity and the calculated perm-selectivity based on experimental gas flux data. There appears a diverse pattern of deviation from simple H<sub>2</sub>, N<sub>2</sub> to CO<sub>2</sub> and C<sub>2</sub>H<sub>6</sub>, suggesting permeation and gas separation by SILM is strongly specific to the gas-ionic liquids combinations. The permeability of simple H<sub>2</sub> and N<sub>2</sub> is much faster than predicted values despite the two gases have very low solubility in the ionic liquid, suggesting transport of smaller, non-interactive gases are more likely diffusion controlled and less dependent on solubility. CO<sub>2</sub> has smaller observed permeation rate than the predicted values. The slow CO<sub>2</sub> diffusion is more likely influenced by strong CO<sub>2</sub>-ILs interaction which impeded the motion of CO<sub>2</sub> molecules in the ionic liquid. The predicted and experimental permeation rate for CH<sub>4</sub> are very close considering the uncertainty associated with the absolute accuracy of the solubility data. CH<sub>4</sub> is non polar and considered non-interactive with the ionic liquid. Its permeation rate is influenced by combined gas dissolution and diffusion. It is the only gas molecule in this work which has experimental permeability value similar to the predicted value by the solution diffusion model. In contrast to CO<sub>2</sub>, permeation of C<sub>2</sub>H<sub>6</sub> is faster despite it has the smallest diffusion coefficient and a strong interactions with the ionic liquids, reflected by large dissolution enthalpy and entropy which is to be elaborated in the following section. However, the strong C<sub>2</sub>H<sub>6</sub>-IL interactions facilitated C<sub>2</sub>H<sub>6</sub> transport rather than impeded the motion of the gas molecule, especially at increased gas phase pressure.

Table 4

Calculated gas diffusion coefficients based on Wilke–Chang and Scheibel model correlations in three ionic liquids ( $D \times 10^{-6} \text{ cm}^2 \text{ s}^{-1}$ ).

Gas	CO <sub>2</sub>	C <sub>2</sub> H <sub>6</sub>	CH <sub>4</sub>	N <sub>2</sub>	H <sub>2</sub>
Ionic liquid	[C <sub>4</sub> mim][NTf <sub>2</sub> ]				
Wilke–Chang [46]	3.55	2.97	3.48	3.61	4.13
Scheibel [47]	3.96	2.63	3.78	4.13	5.68
Gas molar volume (cm <sup>3</sup> /mol) [51]	94.07	145.50	98.60	90.10	65.00
Gas molecular diameter (nm) [51]	0.399	0.439	0.378	0.367	0.291
Ionic liquid	[C <sub>10</sub> mim][NTf <sub>2</sub> ]				
Wilke–Chang	2.01	1.68	1.97	2.05	2.34
Scheibel	2.66	1.74	2.54	2.78	3.85
Ionic liquid	[C <sub>4</sub> mim][OTf]				
Wilke–Chang	1.95	1.63	1.92	1.99	2.27
Scheibel	2.02	1.36	1.93	2.10	2.87



**Table 5**  
Corroboration and comparison of gas permeation rate and selectivity based on experimental permeation data and predictive calculations by solution–diffusion theory using independently measured gas solubility and diffusivity in [C<sub>4</sub>mim][NTf<sub>2</sub>] at T = 303 K.

Gas	CO <sub>2</sub>	C <sub>2</sub> H <sub>6</sub>	CH <sub>4</sub>	N <sub>2</sub>	H <sub>2</sub>
Molecular diameter (nm)	0.399	0.439	0.378	0.367	0.291
Measured gas solubility $S_i \times 10^5$ (mol mol <sup>-1</sup> cm Hg <sup>-1</sup> )	36.84	3.82	1.45	0.93	0.24
Scheibel gas diffusivity $D_{ij} \times 10$ (cm <sup>2</sup> /s)	3.96	2.63	3.78	4.13	5.68
Predicted solution–diffusion permeability (barrer) $P_i = S_i \times D_i$	14.58	1.04	0.55	0.38	0.14
Experimental permeability (barrer) $P_i = \frac{I \Delta p}{L}$	2.3	3.4	0.43	72.6	20.1
Gas pairs	C <sub>2</sub> H <sub>6</sub> /CH <sub>4</sub>	C <sub>2</sub> H <sub>6</sub> /CO <sub>2</sub>	CH <sub>4</sub> /CO <sub>2</sub>	N <sub>2</sub> /CO <sub>2</sub>	H <sub>2</sub> /CO <sub>2</sub>
Predictive solution–diffusion selectivity $\alpha_{i,j} = \frac{P_i}{P_j} = \frac{S_i D_i}{S_j D_j}$	1.89	0.022	0.098	0.026	0.0096
Experimental based selectivity $\alpha_{i,j} = \frac{I_i}{I_j}$	7.35	1.45	0.19	31.57	8.16

For separation analysis, in the case of N<sub>2</sub>/CO<sub>2</sub> pairs, a rather contrasting reversal of the predicted selectivity ( $\ll 1.0$ ) is found to the observed experimental selectivity ( $\gg 1.0$ ). Similar reversal of selectivity is also found for other gases pairing with CO<sub>2</sub>. The molecular specific interactions between the diffusing gas molecules and the ionic liquid underpins the level of deviations from the solution–diffusion mechanism. On a comparative and qualitative understanding, the nature and strength of gas–ionic liquid interactions for simple (H<sub>2</sub>, N<sub>2</sub>, and CH<sub>4</sub>), polar (H<sub>2</sub>O, and CO<sub>2</sub>) and more organic C<sub>2</sub>H<sub>6</sub> can be revealed by examining the thermodynamic properties of gas dissolution enthalpy and entropy.

The Gibbs energy of solvation ( $\Delta G_{solv}^\infty$ ) is given by:

$$\Delta G_{solv}^\infty = \Delta H_{solv}^\infty - T \Delta S_{solv}^\infty$$

The variation with temperature of the solubility, expressed in Henry's law constant, is directly related to the thermodynamic properties of solvation. In the case of gaseous solutes at low pressure, it is practically identical to the thermodynamic properties of solution.

$$\Delta G_{solv}^\infty = RT \ln \left( \frac{K_H}{p^0} \right)$$

Therefore, the partial enthalpy ( $\Delta H_{solv}^\infty$ ) and entropy ( $\Delta S_{solv}^\infty$ ) between the two states can be calculated from the partial derivative of

the Henry's law constants with respect to temperature at constant pressure:

$$\Delta_{solv} H^\infty = -RT^2 \frac{\partial}{\partial T} \left[ \ln \left( \frac{K_H}{p^0} \right) \right]$$

$$\Delta_{solv} S^\infty = -RT \frac{\partial}{\partial T} \left[ \ln \left( \frac{K_H}{p^0} \right) \right] - R \ln \left( \frac{K_H}{p^0} \right)$$

The calculated values of gas dissolution enthalpy and entropy are presented in Table 6.

Dissolution enthalpy and entropy for H<sub>2</sub> and N<sub>2</sub> in [C<sub>4</sub>mim][NTf<sub>2</sub>] have not been found in literature. H<sub>2</sub> and N<sub>2</sub> has reported [55] solvation enthalpy  $-3.24$  and  $-4.80$  Jmol<sup>-1</sup> K<sup>-1</sup> (T = 293 K) respectively in ionic liquid [C<sub>4</sub>mim][BF<sub>4</sub>]. Carbon dioxide has stronger interactions at molecular level with [C<sub>4</sub>mim][NTf<sub>2</sub>], elicited from the greater dissolution enthalpy value of  $-13.86$  kJ mol<sup>-1</sup> (strong exothermic dissolution process), and large entropy of  $-75.29$  Jmol<sup>-1</sup> K<sup>-1</sup>. C<sub>2</sub>H<sub>6</sub> also has an exothermic dissolution enthalpy and large entropy at  $-62.22$  Jmol<sup>-1</sup> K<sup>-1</sup>. The exothermic dissolution enthalpy value suggests that it has good affinity with the ionic liquids, derived from attractive van der Waal force between ethane and the alkyl chain on the cation. On the other hand, the entropic ethane can be disruptive to the order of cation–anion distribution. Low diffusivity and affinitive C<sub>2</sub>H<sub>6</sub>–IL interactions underlie a comparatively smaller C<sub>2</sub>H<sub>6</sub> permeability at low gas phase pressure. The trend reversed, however, when C<sub>2</sub>H<sub>6</sub> concentration increased inside the ionic liquid phase which led fastest

**Table 6**  
Gibbs energy of solvation ( $\Delta G_{solv}^\infty$ ), partial enthalpy ( $\Delta H_{solv}^\infty$ ) and entropy ( $\Delta S_{solv}^\infty$ ).

T/K	dG/kJ mol <sup>-1</sup>	dH/kJ mol <sup>-1</sup>	dS/J mol <sup>-1</sup> K <sup>-1</sup>	T/K	dG/kJ mol <sup>-1</sup>	dH/kJ mol <sup>-1</sup>	dS/J mol <sup>-1</sup> K <sup>-1</sup>
[C <sub>4</sub> mim][BF <sub>4</sub> ] + CO <sub>2</sub>				[C <sub>4</sub> mim][NTf <sub>2</sub> ] + CO <sub>2</sub>			
303	10.45	-14.42	-82.10	303	8.971	-13.79	-75.13
313	11.28	-14.62	-82.75	313	9.721	-13.67	-74.74
323	12.11	-14.81	-83.33	323	10.47	-13.56	-74.39
333	12.95	-14.98	-83.87	333	11.21	-13.46	-74.08
[C <sub>4</sub> mim][BF <sub>4</sub> ] + C <sub>2</sub> H <sub>6</sub>				[C <sub>4</sub> mim][NTf <sub>2</sub> ] + C <sub>2</sub> H <sub>6</sub>			
303	14.72	-9.21	-78.97	303	11.72	-7.13	-62.22
313	15.53	-10.75	-83.97	313	12.40	-10.96	-74.64
323	16.40	-12.19	-88.51	323	13.21	-14.54	-85.92
333	17.30	-13.55	-92.65	333	14.12	-17.92	-96.20
[C <sub>4</sub> mim][BF <sub>4</sub> ] + CO				[C <sub>4</sub> mim][NTf <sub>2</sub> ] + CO			
303	19.23	-6.92	-86.3	303	16.22	-5.59	-71.98
313	20.20	-13.46	-107.5	313	16.96	-6.89	-76.22
323	21.37	-19.60	-126.8	323	17.75	-8.11	-80.06
333	22.73	-25.37	-144.4	333	18.56	-9.26	-83.56

exponential increase in fluxes with pressure. It is thought that  $C_2H_6$  molecules are well dispersed in the ionic liquids phase by “pegging” on the alkyl chains on the imidazolium cations, leading to dispersed phase and being disruptive to cation–anion distributions. The dispersed distribution of  $C_2H_6$  molecules would have led to the fast permeation increase when  $C_2H_6$  concentration inside the ionic liquids phase increased under high pressure, especially after the ionic liquids became saturated with no free “pegging” sites available for retention of the  $C_2H_6$  molecules.

### 3.4. Ionic liquids specific gas selectivity

The pressure dependence of  $N_2/CO_2$  selectivity is more pronounced in ionic liquid  $[C_4mim][NTf_2]$ . However, gas feed pressure had almost no effect on  $N_2/CO_2$  selectivity in ionic liquids  $[C_4mim][OTf]$  (Fig. 8) which shares the same cation but differs in anion. Contrasting to declining  $N_2/CO_2$  selectivity with pressure in  $[C_4mim][NTf_2]$ , the  $N_2/CO_2$  selectivity showed a slight increase with pressure in  $[C_{10}mim][NTf_2]$  which has a larger cation and greater liquid free volume due to extended alkyl chain length. The results presented in Fig. 8 clearly points to molecular specific gas-ILs interactions leading to contrasting perm-selectivity performance in different gas-ILs combinations. It also suggest a discriminating gas selectivity based on molecular structure of ionic liquids and the molecular properties of the diffusing gas, suggesting a targeted approach to specific ionic liquid design for specific gas separations.

### 3.5. Further discussion on the special case of $CO_2$

$CO_2$  possess the highest solubility and a comparable diffusion coefficient among the five gases studied for permeation performance. It also has large dissolution enthalpy and entropy. If the prognosis, put forward previously to explain enhanced  $C_2H_6$  permeation at high pressure, is applicable to the case of  $CO_2$  transport through the SILM, then a greater  $CO_2$  permeability than all other gases at high pressure is expected. In contrast, the  $CO_2$  flux increase with pressure is much less pronounced, and its permeability remain the lowest at the high pressure range (Fig. 6). This reversed correlation between higher solubility and lower permeability at comparable diffusivity values suggests that  $CO_2$  has different and specific molecular interactions with the ionic liquids.

$CO_2$  dissolution in the ionic liquids increases with pressure as shown by data from Anthony et al. [29] presented in Fig. 9. Although the increased  $CO_2$  concentration in IL phase led to a higher  $CO_2$  permeation, the increase is not strong enough to reverse the  $N_2/CO_2$  selectivity. It is hypothesised that ionic liquids possess a condensing and holding capacity towards  $CO_2$  which has a relatively low critical

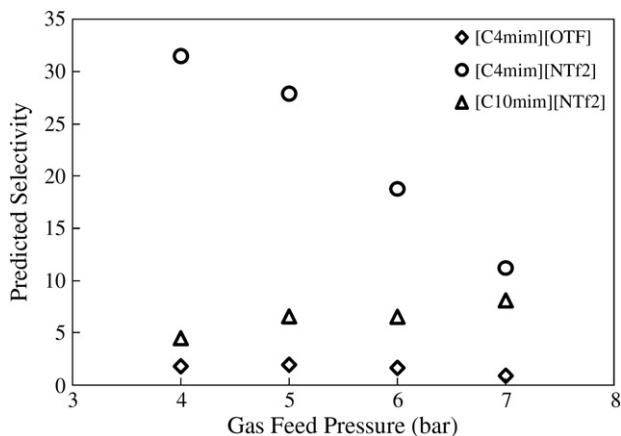


Fig. 8. Effects of three different ionic liquids on predicted  $N_2/CO_2$  selectivity in SILMs.

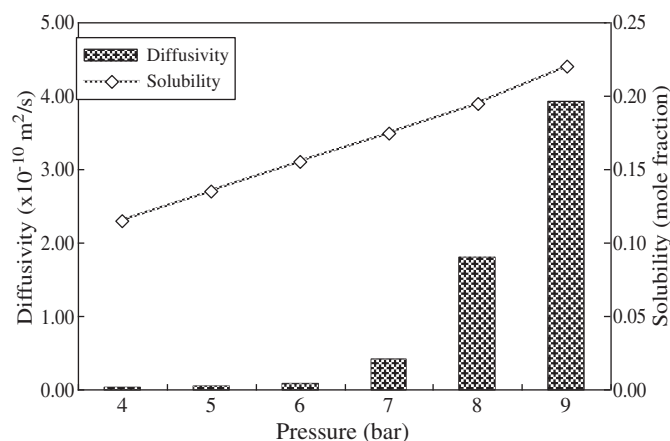


Fig. 9. Concentration dependence of solubility [courtesy of Anthony et al. Ref 29] and exponential increase of  $CO_2$  diffusion coefficient in  $[C_4mim][NTf_2]$  SILM.

pressure of condensation in comparison to other simple gases, regardless the interactions with ILs. The high  $CO_2$  solubility inside ionic liquids could be consequential effects of both chemo-sorption and partial condensation. This hypothesis leads to an interesting question of the state of existence of the accumulating  $CO_2$  molecules in ionic liquids phase. By employing techniques for studying molecular dynamics, Hong et al. reported [56] that the partial radial distribution functions for the cation–anion distribution in  $[C_2mim][NTf_2]$  in the absence and presence of 20 mol% of acetonitrile have the same value which indicates that acetonitrile dissolved in IL within existing channels, and thus did not break the cation–anion structure. This was suggested to be due to the dipole movement of acetonitrile, and therefore could be the same for the carbon dioxide with quadrupole movement. The analysis implies that high concentration of  $CO_2$  in the SILM phase at elevated pressure does not necessarily leads to greater homogeneous dispersion of  $CO_2$  in the ionic liquids phase, which is responsible for faster permeability according to the conventional solution diffusion theory. Rather, the residence of highly concentrated  $CO_2$  molecules in the supported ionic liquids occupies the interstitial and hole free volume in the SILM structure, typified by voids or holes existed in glassy polymer structures. Moreover, it is speculated that pockets of concentrated  $CO_2$  in the ionic liquid phase may be created by the condensing power of the ionic liquids which leads to formation of localized reservoirs of critical  $CO_2$  fluids under a partial pressure much lower than the critical pressure required at the same temperature in gas phase.

When considering the diffusion coefficient in this SILM, it is necessary to point out the differences between dense polymer membrane and supported ionic liquid membrane. Since many reports revealed that ionic liquids possess properties of both a solid and a liquid [57], one may speculate a transformation of ILs from liquid to solid state might happen when the ILs are confined to nanoscale pores surrounded by functionalised polymers with high surface charge, which can exerts strong binding force on the cations and anions. Chen et al. [58] found that  $[C_4mim][PF_6]$  performs a fully different phase transition and crystal formation when confined in multiwalled nanotubes. It could be the similar situation in our NF membranes, that high electric charge density between the NF membrane materials and ionic liquids shorten the intermolecular spacing, thereby forming a more stable structure. The quadrupole movement of  $CO_2$  in this semi-solid membrane could be different as in bulk ionic liquids, and which could be another key factor leading to deviation from the solution diffusion theory based on solubility and diffusivity data obtained in bulk ionic liquid phase. The phase state of the ionic liquids after immobilisation inside the nano-scale pores surrounded by charged polymer groups is unclear, but it is an important issue for future SILM research.

### 3.6. Concentration dependence of diffusivity in SILMs

When gas transport through the SILM is governed by diffusion, Fick's second law dictates:

$$\frac{P_i}{RT} \frac{dV}{Adt} = -\frac{\phi}{\tau} D_i \frac{dc_i}{dx}$$

where  $\phi$  is the porosity of a membrane, and  $\tau$  is the membrane tortuosity factor. By applying gas law and performing integration, the diffusion coefficient can be calculated from:

$$V_t = D_i S_i \frac{ART}{L} \frac{\phi}{\tau} \frac{P_{i,F} - P_{i,P}}{P_i} (t - t_0)$$

Given a constant pressure and assuming membrane porosity 0.05 and tortuosity 1.55, by using the independently measured CO<sub>2</sub> solubility in [C<sub>4</sub>mim][NTf<sub>2</sub>] at different pressure by Anthony et al. [29], the change in CO<sub>2</sub> diffusion coefficient with changing feed gas pressure can be calculated from the gradient in plotting the linear relation between accumulated permeating gas volume  $V_t$  with time.  $t_0$  is the experimentally observed lag time for the SILM to become saturated by the permeating gas before the onset of steady gas flux. The results shown in Fig. 9 demonstrate that the diffusion coefficient increases in an exponential fashion with increasing CO<sub>2</sub> concentration in the SILM phase, in contrast to the linear increase of CO<sub>2</sub> diffusion coefficient in pure ionic liquids [C<sub>4</sub>mim][BF<sub>4</sub>] and [C<sub>4</sub>mim][PF<sub>6</sub>] as reported in literature [44,45], which used the time lag method for the calculation of both gas solubility and diffusivity without independently measured values of both.

## 4. Conclusion

A framework analysis is put forward to address the interrelations between gas solubility, diffusivity and thermodynamic properties in ionic liquids to observed gas permeation and separation performance in SILMs, which are often complicated by the complex gas-ILs molecular interactions, leading to non-ideal behaviour and deviations from conventional solution–diffusion theory. SILMs by ionic liquids supported on nano-pore membranes possess high pressure stability unmatched by other SIMs or SILMs supported on micron-pore membranes. It offers opportunity to operate SILM at industrial relevant high pressure for gas separations, and allowed analysis of permselectivity performance which showed very different behaviour at high pressure to those reported for SILMs operating under atmospheric pressure. Increased gas concentration in the ionic liquids phase led to changes in transport properties, which are gas concentration dependent in the ionic liquid phase.

The permeability of CO<sub>2</sub>, N<sub>2</sub>, H<sub>2</sub>, CH<sub>4</sub> and C<sub>2</sub>H<sub>6</sub> increases in an exponential fashion with increasing gas feed pressure, with C<sub>2</sub>H<sub>6</sub> showing the largest increase despite it has the lowest diffusivity in the ionic liquids. The affinitive molecular interaction between C<sub>2</sub>H<sub>6</sub> and ionic liquids, demonstrated by exothermic dissolution enthalpy and cation–anion order disruptive entropy, contributed to the fastest increase in permeation rate with increased pressure. A hypothesis was put forward that C<sub>2</sub>H<sub>6</sub> molecules could peg on the side alkyl chains on the imidazolium [C<sub>n</sub>mim] cation because of high chemical affinity between the hydrocarbons. Unlike CO<sub>2</sub> which aggregates inside ionic liquid phase, C<sub>2</sub>H<sub>6</sub> molecules could be well dispersed throughout the ionic liquid phase. When ionic liquids were saturated with the C<sub>2</sub>H<sub>6</sub> molecules at high pressure, they lost “binding” capacity to hold on to gas molecules, and the permeation rate showed explosive increase, a typical pattern for concentration-dependent transport.

Independently measured gas solubility and diffusivity in ionic liquids were applied to analysing gas permeation and separation through supported ionic liquids by the conventional solution–diffusion theory,

and attempt was made to corroborate the theoretically predicted permeability and selectivity to experimentally observed gas permeation rate and separation factor. The analysis revealed a large and varied deviation between the theory and experimental outcome, and the deviation is specific to gas-IL combinations which determine the nature of gas-IL interactions. Permeation for simple non-polar gases H<sub>2</sub> and N<sub>2</sub> appears to be diffusion controlled. CO<sub>2</sub> has the lowest permeability and a reversed N<sub>2</sub>/CO<sub>2</sub> selectivity in spite of CO<sub>2</sub> possessing the highest solubility, comparable diffusivity and a large exothermic dissolution enthalpy and entropy. This leads to an understanding that the nature of CO<sub>2</sub>-ILs interactions is very different to that of ethane and other simple gases. The large CO<sub>2</sub> dissolution in the SILM and its increased solubility coefficient with pressure may be a consequence of a special condensing and “holding capacity” for CO<sub>2</sub> by the ionic liquids. The residing state of CO<sub>2</sub> in [C<sub>4</sub>mim][NTf<sub>2</sub>] is not homogeneously dispersive. Unlike C<sub>2</sub>H<sub>6</sub>, dissolved CO<sub>2</sub> may not peg on the alkyl chains, and not as disruptive to cation–anion distributions. Rather it exists in pockets of aggregated CO<sub>2</sub> molecules in between the well coordinated and structured cation–anion groups. Compared to the linear increase of CO<sub>2</sub> solubility with pressure, effective diffusivity was found to increase in an exponential fashion, suggesting CO<sub>2</sub> diffusion coefficient in the membrane phase is not constant but also concentration dependent.

The experimental results for gas permeation through the SILMs using three different ionic liquids, typified by different N<sub>2</sub>/CO<sub>2</sub> selectivity performance in ionic liquids [C<sub>4</sub>mim][NTf<sub>2</sub>], [C<sub>4</sub>mim][OTF] and [C<sub>10</sub>mim][NTf<sub>2</sub>], also demonstrate that ionic liquids possess discriminating properties towards gas dissolution and transport due to molecular specific interactions. The transport and separation by molecular specific nature could be explored for targeted approach to ionic liquid design for future gas separations.

### Nomenclature

$\alpha_{i,j}$	gas selectivity/separation factor	
$a_1$	radius of the solute	(cm)
$c_i$	gas mole fraction in SILMs	
$D_i$	diffusivity	(cm <sup>2</sup> s <sup>-1</sup> )
$\Delta C_{solv}^{\infty}$	The Gibbs energy of solvation	(Jmol <sup>-1</sup> K <sup>-1</sup> )
$\Delta H_{solv}^{\infty}$	partial enthalpy of solvation	(Jmol <sup>-1</sup> K <sup>-1</sup> )
$J_i$	Gas permeation rate/flux	(cm <sup>3</sup> s <sup>-1</sup> cm <sup>-2</sup> )
$k$	Boltzmann's constant	(J K <sup>-1</sup> )
$K_H$	Henry's law constant	(atm/mmHg)
$L$	membrane thickness	(cm)
$M_i$	molecular weight	(g mol <sup>-1</sup> )
$P_i$	permeability	(barrer)
$p$	pressure	(bar)
$S_i$	solubility	(mol mol <sup>-1</sup> cmHg <sup>-1</sup> )
$\Delta S_{solv}^{\infty}$	partial entropy of solvation	(Jmol <sup>-1</sup> K <sup>-1</sup> )
$T$	temperature	(K)
$\bar{V}_1$	molar volume of gas solute	(cm <sup>3</sup> mol <sup>-1</sup> )
$V_{bulb}$	volume of gas bulb	(cm <sup>3</sup> mol <sup>-1</sup> )
$\mu_2$	solution viscosity	(mPa s)
$\phi_2$	fugacity coefficient	
$\delta$	deviation	

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